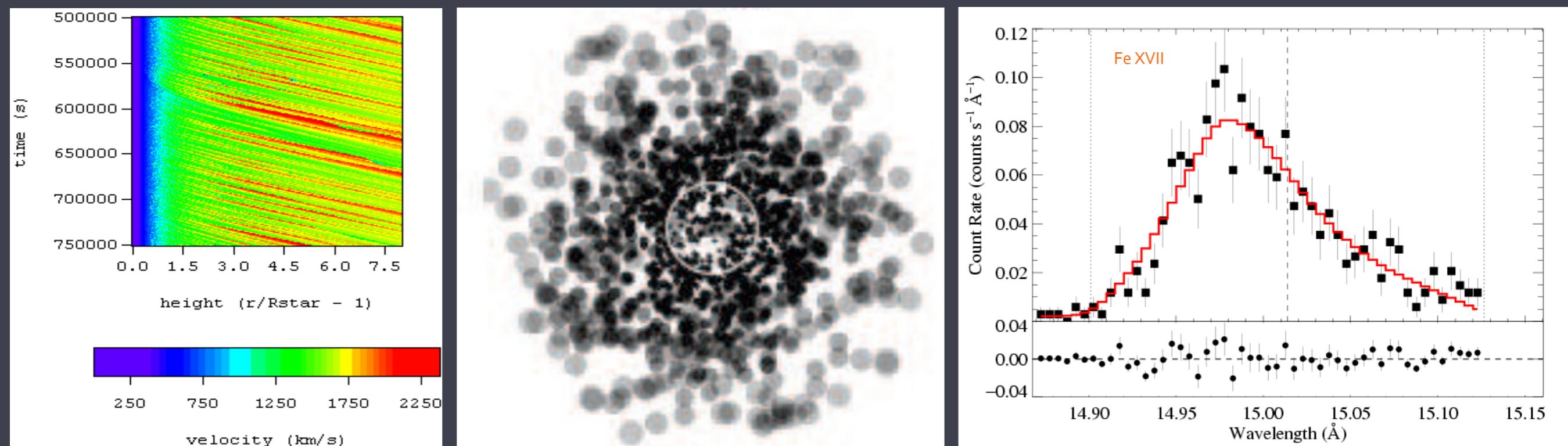


# Clumping and Porosity in Massive Star Winds and How They Affect the Observed X-ray Emission

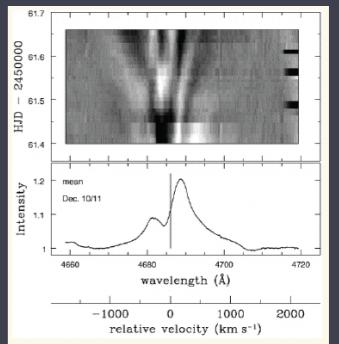
David Cohen  
Swarthmore College

with Stan Owocki & Jon Sundqvist (U. Delaware) and Maurice Leutenegger (GSFC)

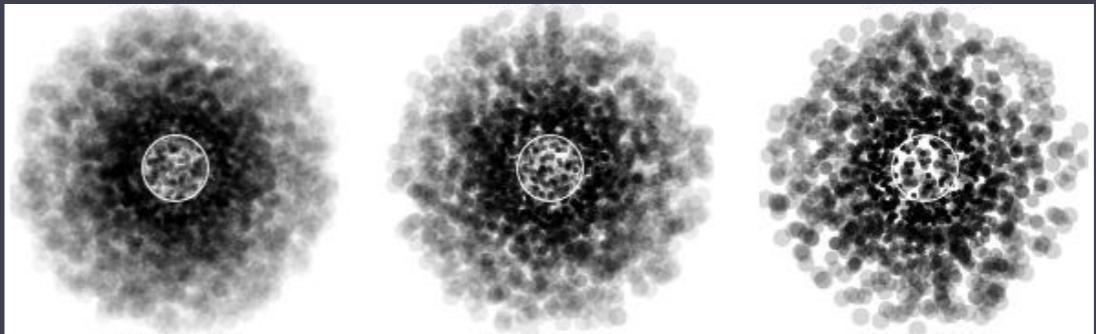


# Outline: clumping and porosity

- Evidence for **clumping** in massive star winds



- Clumped winds are only **porous** if individual clumps are optically thick



- The **porosity length** quantifies the effect of porosity  
$$h \equiv (n_{\text{cl}} A_{\text{cl}})^{-1} = L^3 / \ell^2 = \text{mean free path}$$
 between clumps
- If the porosity length is greater than  $h \sim 1 R_\star$ , the overall transparency of the wind increases

# Outline: clumping and porosity

## X-ray line profiles

- For spherical clumps (**isotropic porosity**), porosity mimics a reduced mass-loss rate
- For flattened clumps (**anisotropic porosity**), porosity leads to distinctive X-ray line profile shapes
- Observed X-ray profiles can place constraints on porosity, clumping, and the wind mass-loss rate

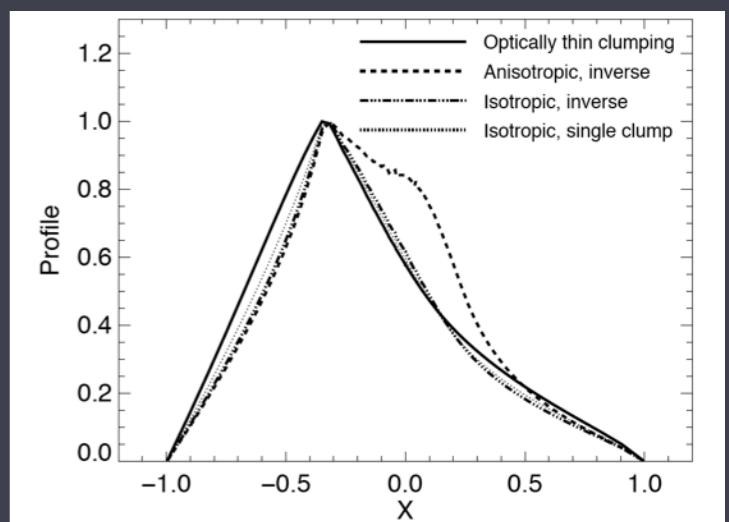
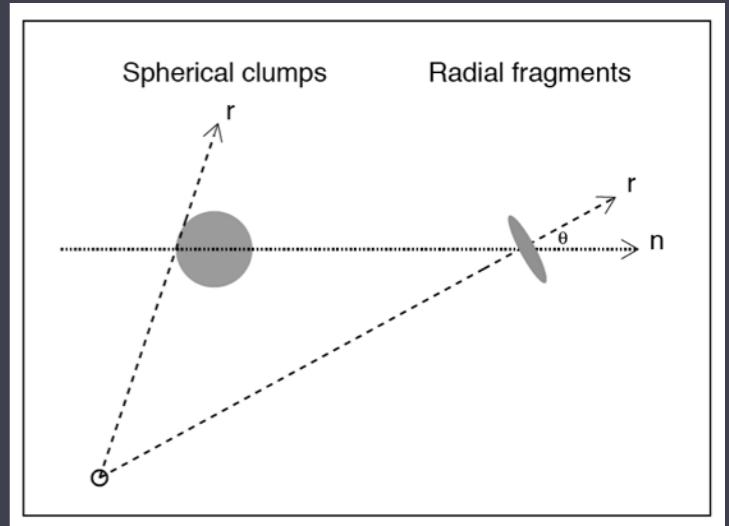
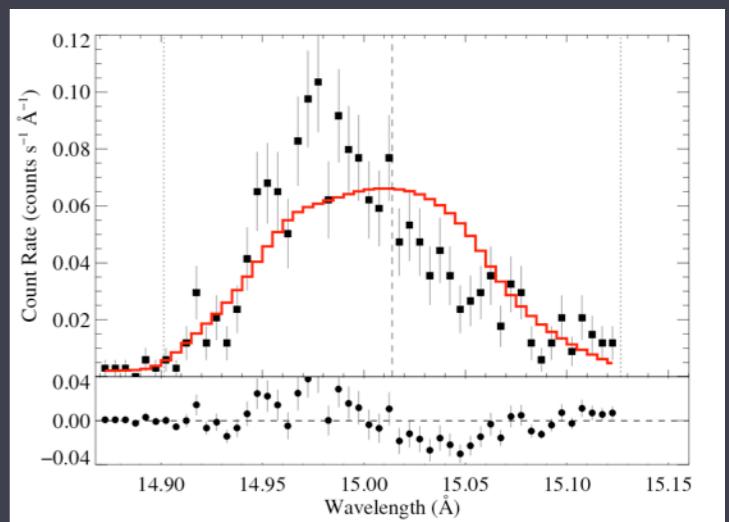


Figure 5. Line profiles for  $h_\infty/R_\star = 1.0$  and  $\tau_\star = 2.5$ , using different effective opacity laws, as labelled.



# Evidence for clumping in massive stars

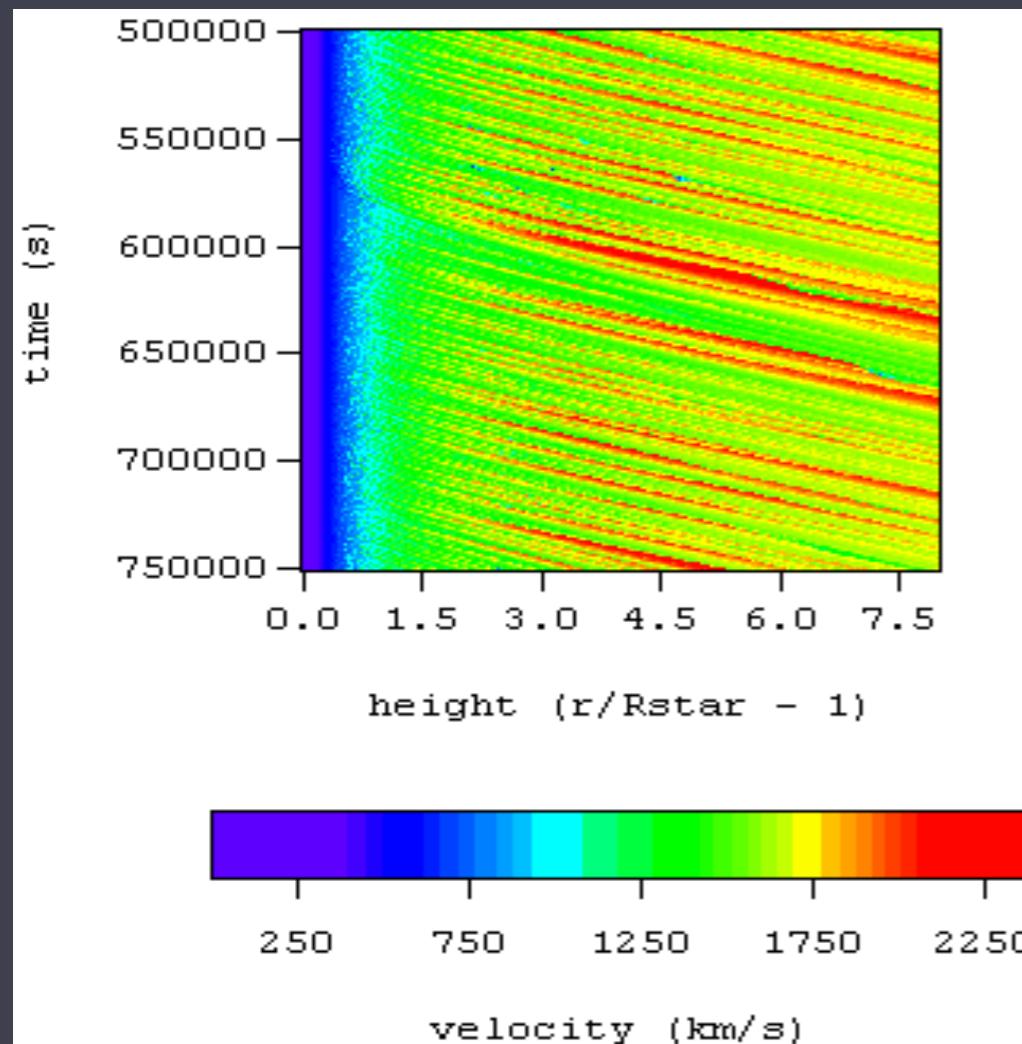
- theoretically expected from simulations of the line-driving instability (LDI)
- line profile variability
  - optical emission lines
  - UV absorption lines
  - polarization
- black troughs in UV resonance lines
- electron scattering wings
- UV doublet ratios
- different diagnostics, with different clumping sensitivities, give different mass-loss rates for the same star if clumping is neglected

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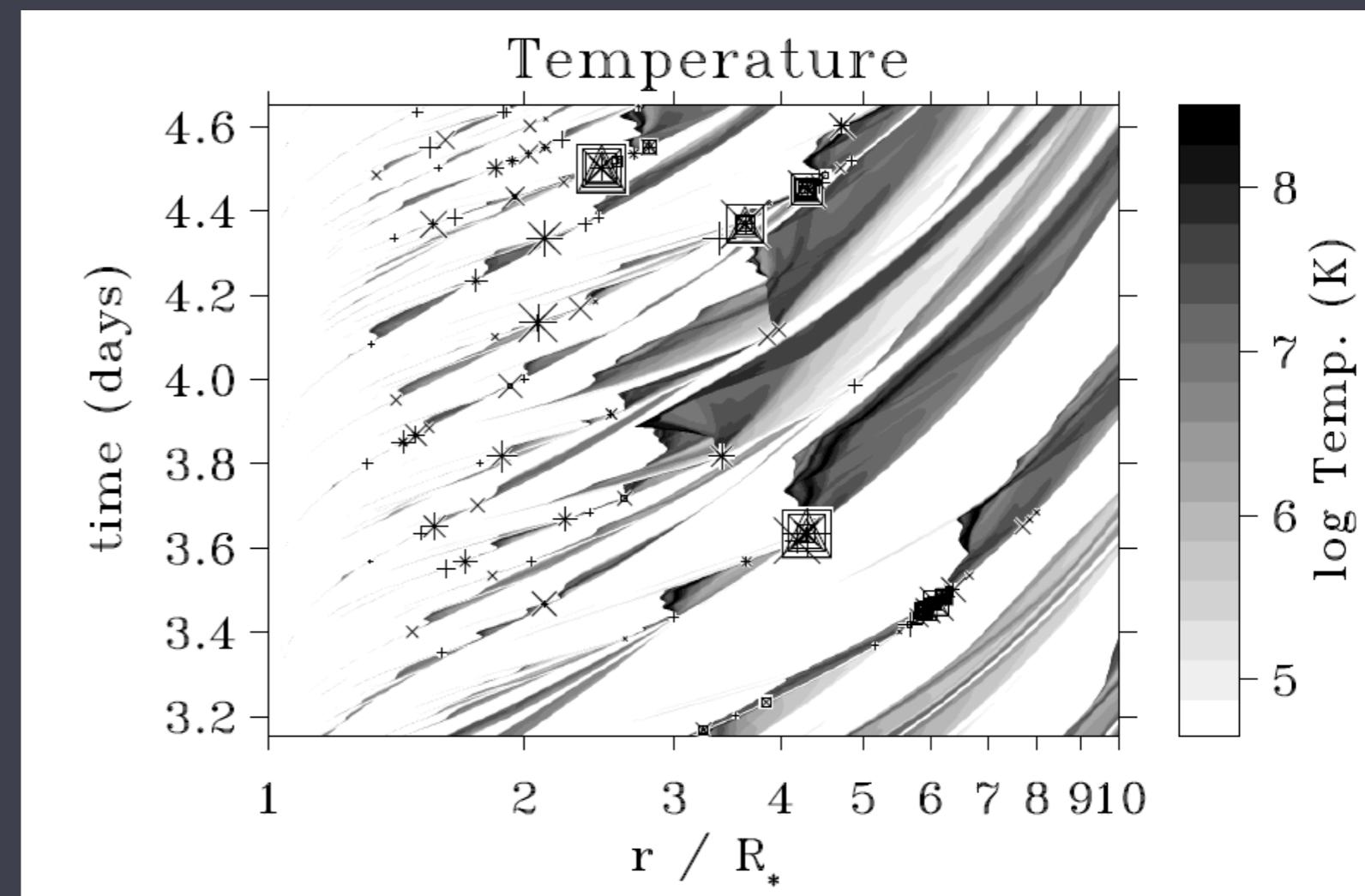
# Numerical simulations of the line-driving instability (LDI)

self-excited instability



Owocki, Cooper, Cohen 1999

excited by turbulence at the wind base

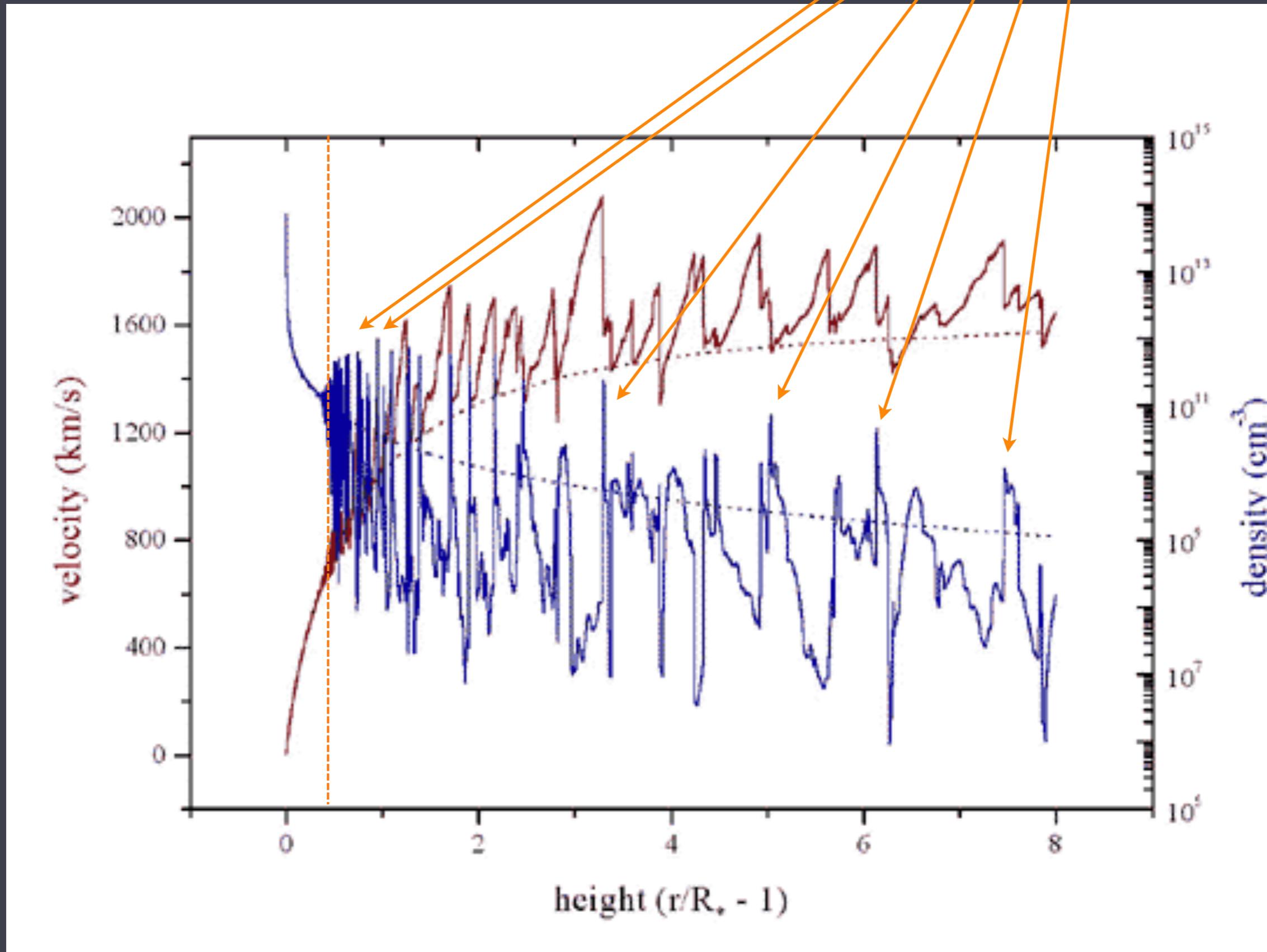


Feldmeier, Puls, & Pauldrach 1997

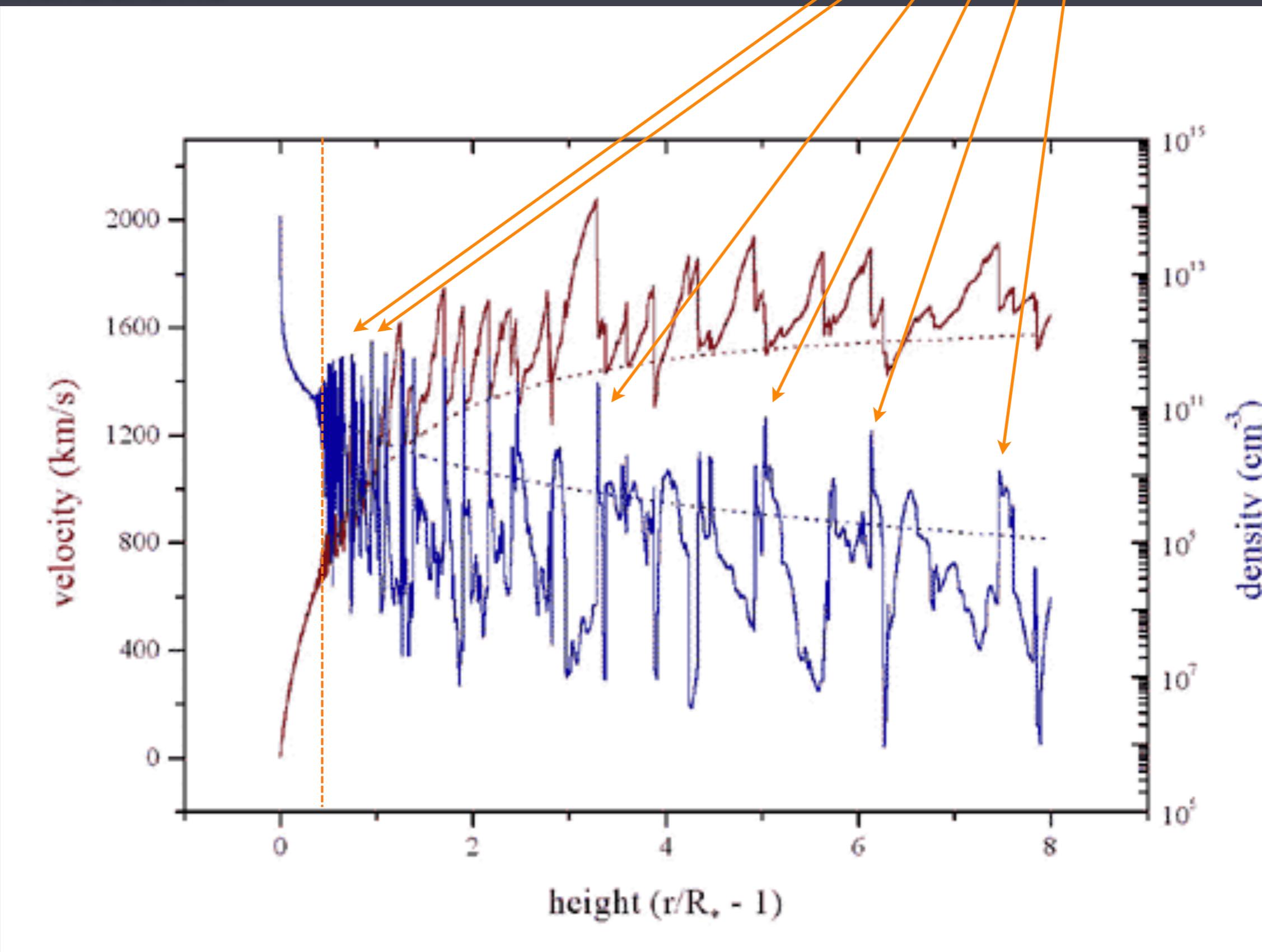
Dense clumps/shells form and advect through  
the wind

from a single time snap-shot

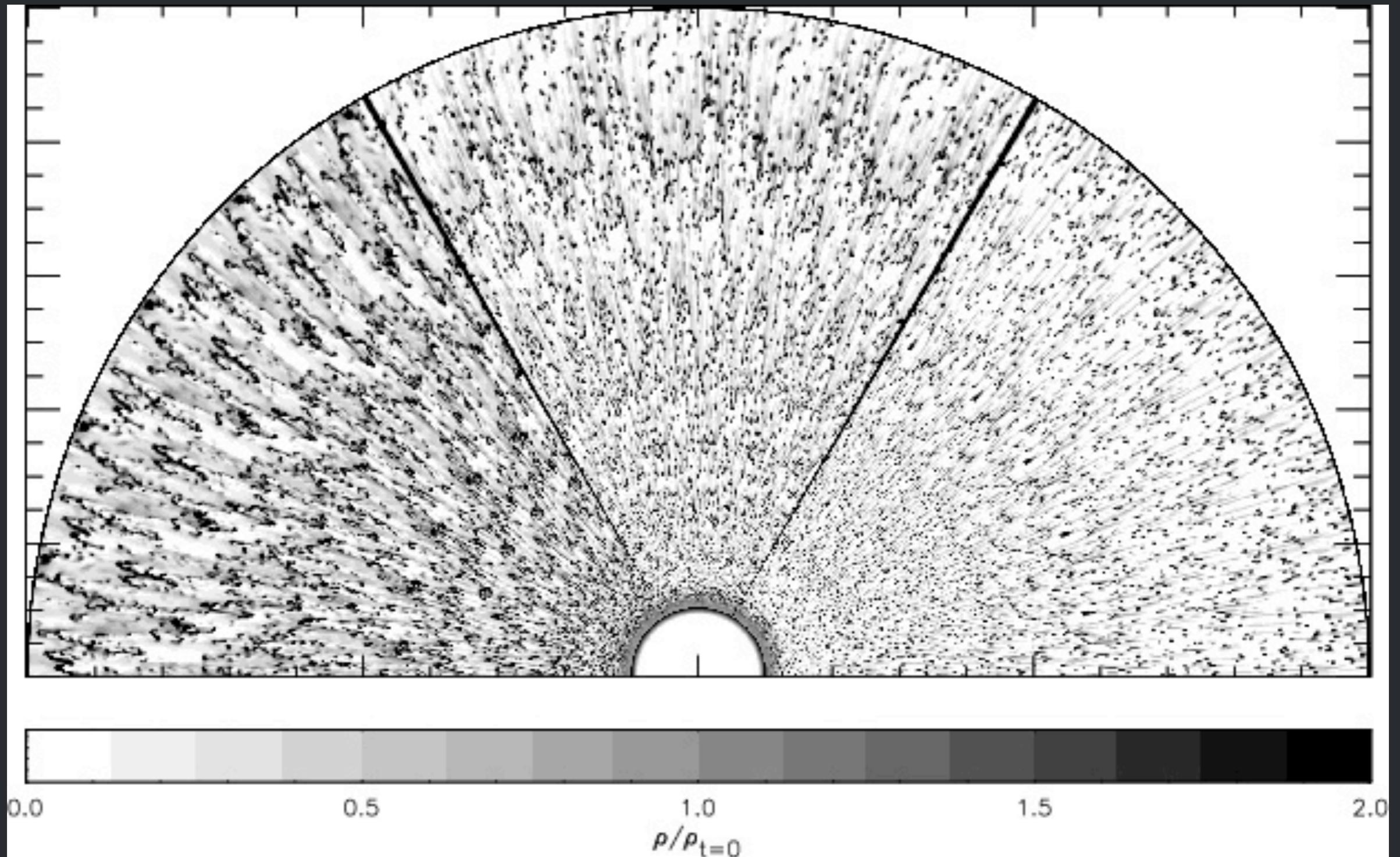
clumps



but keep in mind, limitations of 1-D **clumps**  
simulations



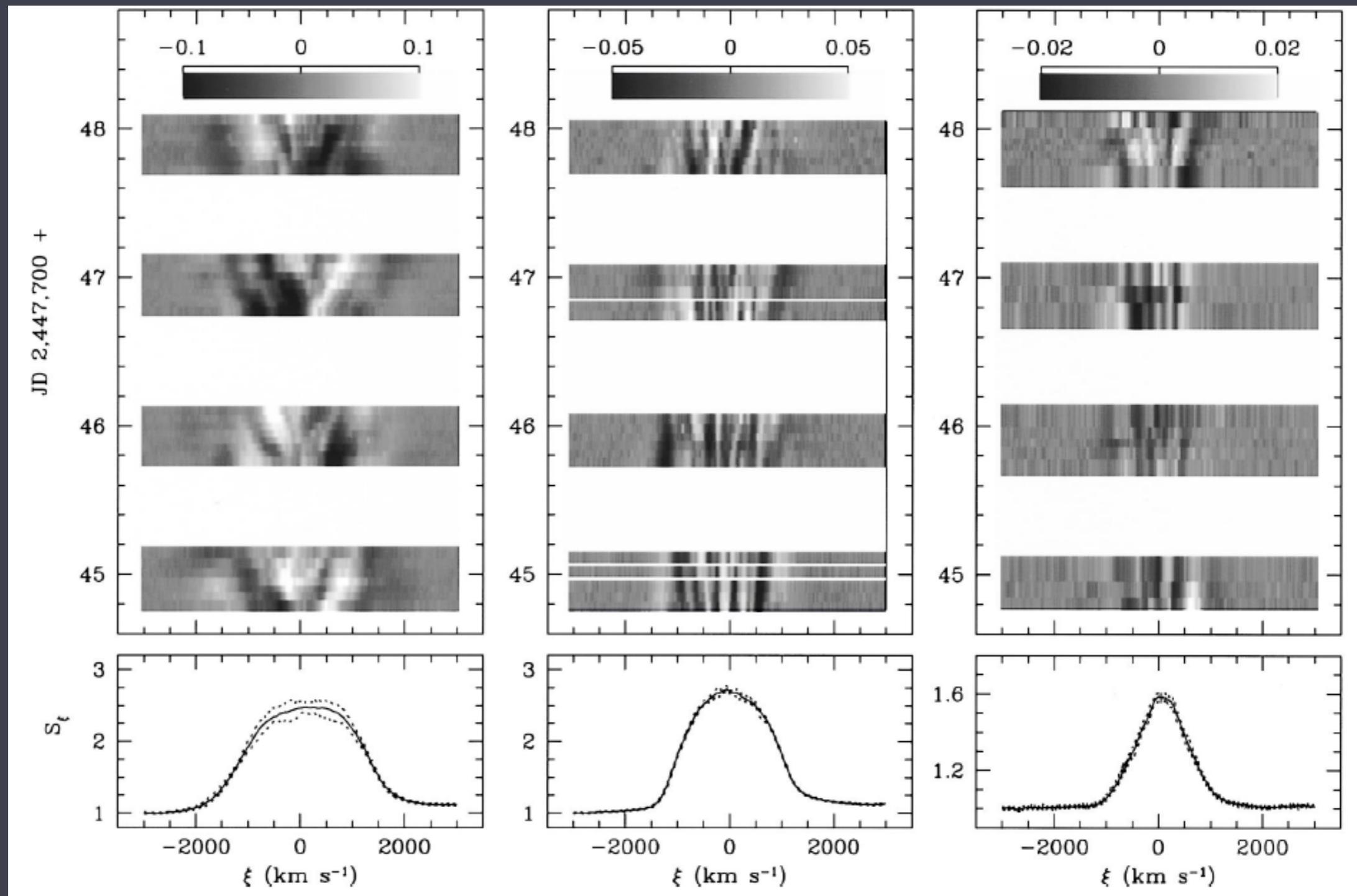
# More realistic 2-D simulations: R-T like break-up; structure on quite small scales



# Evidence for clumping in massive stars

- theoretically expected from simulations of the line-driving instability (LDI)
- line profile variability
  - optical emission lines
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  - polarization
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- different diagnostics, with different clumping sensitivities, give different mass-loss rates for the same star if clumping is neglected

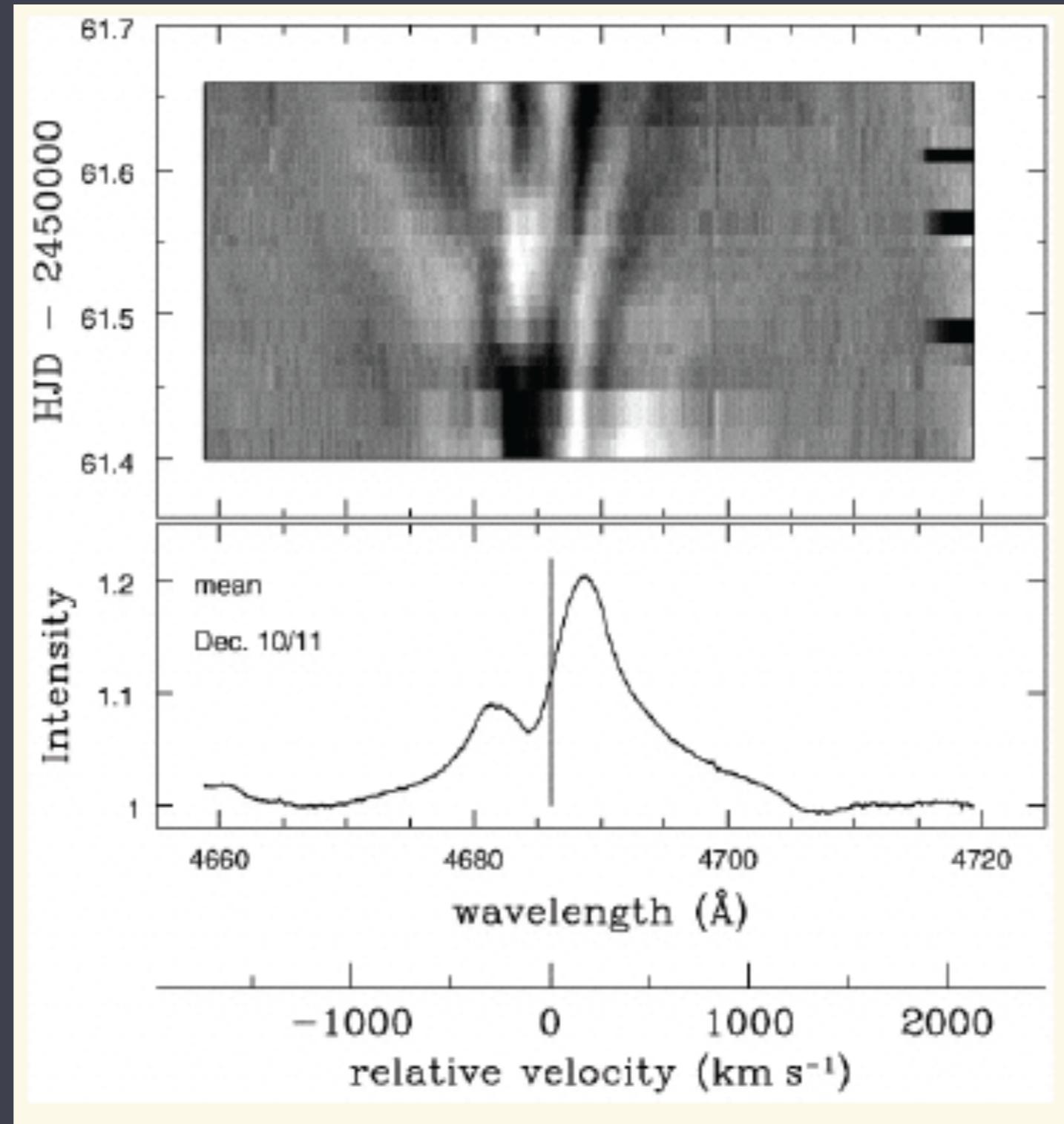
# H $\alpha$ variability - moving bumps - in WR stars



WR 134, 136, 138, from Lépine & Moffat 1999

# and in $\zeta$ Pup (O4If)

moving spectral subpeaks



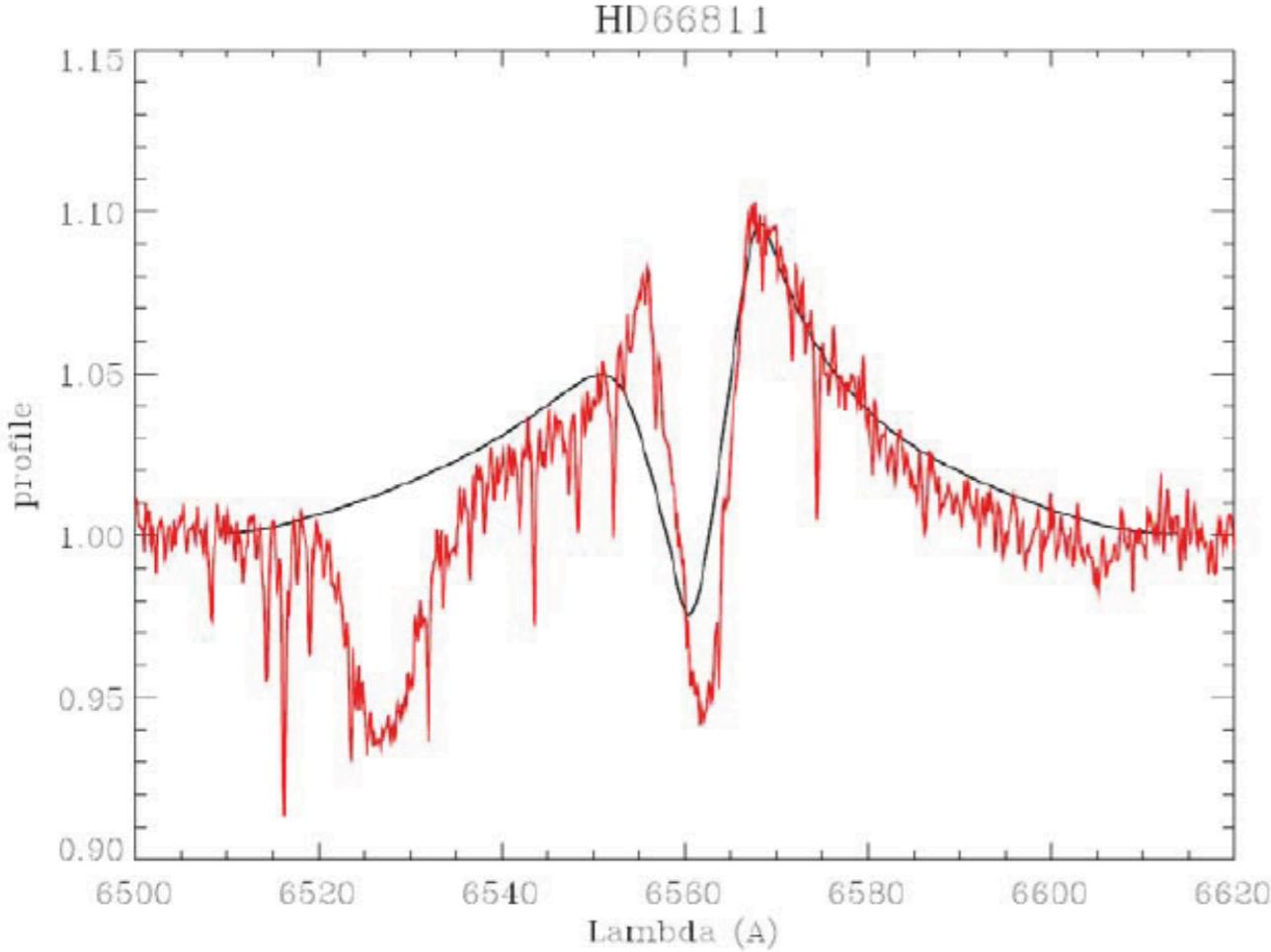
# Evidence for clumping in massive stars

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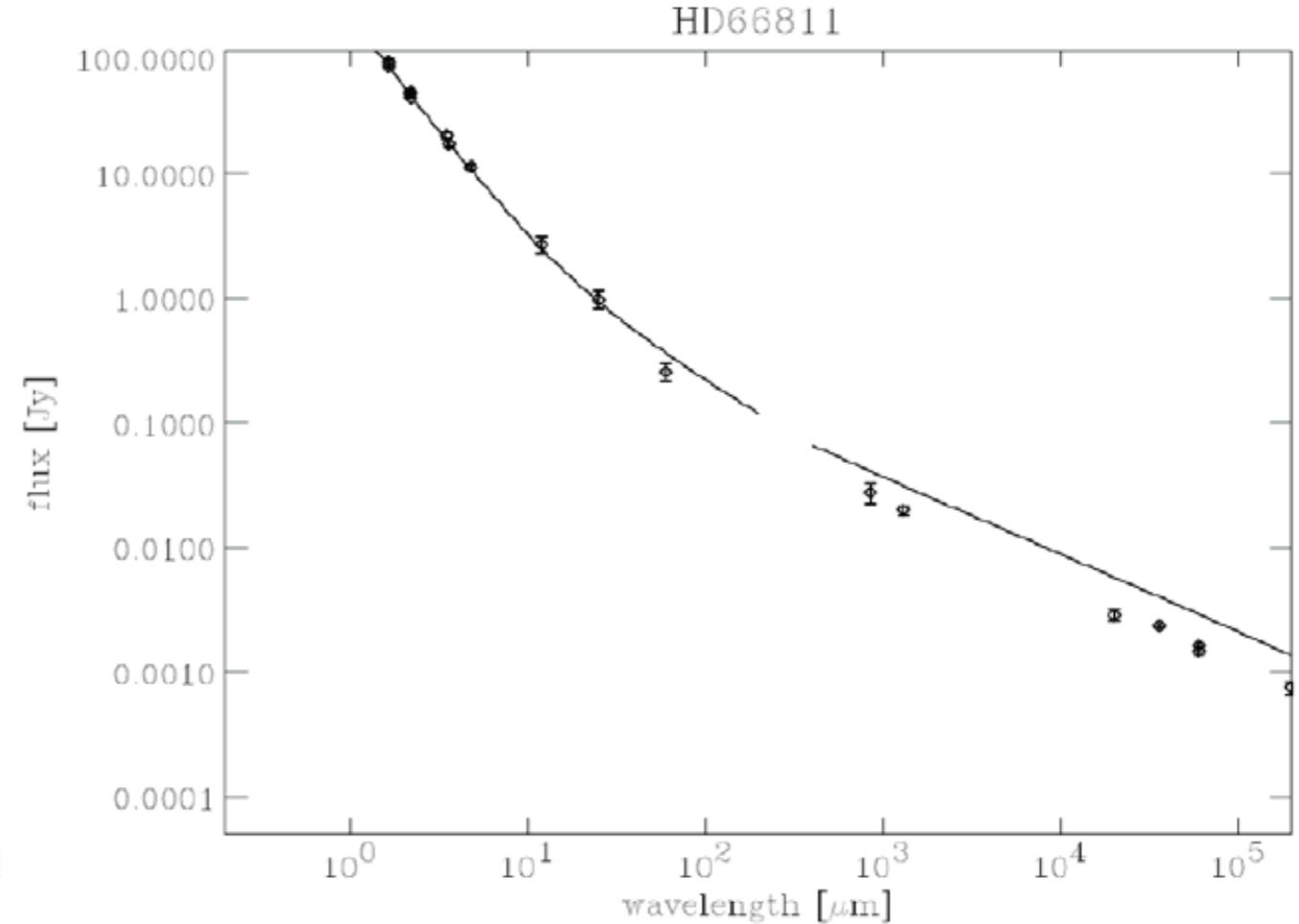
# $\zeta$ Pup: without clumping, $\dot{M}$ discrepancies

for  $\dot{M} = 7 \times 10^{-6} M_{\text{sun}}/\text{yr}$

H $\alpha$



IR

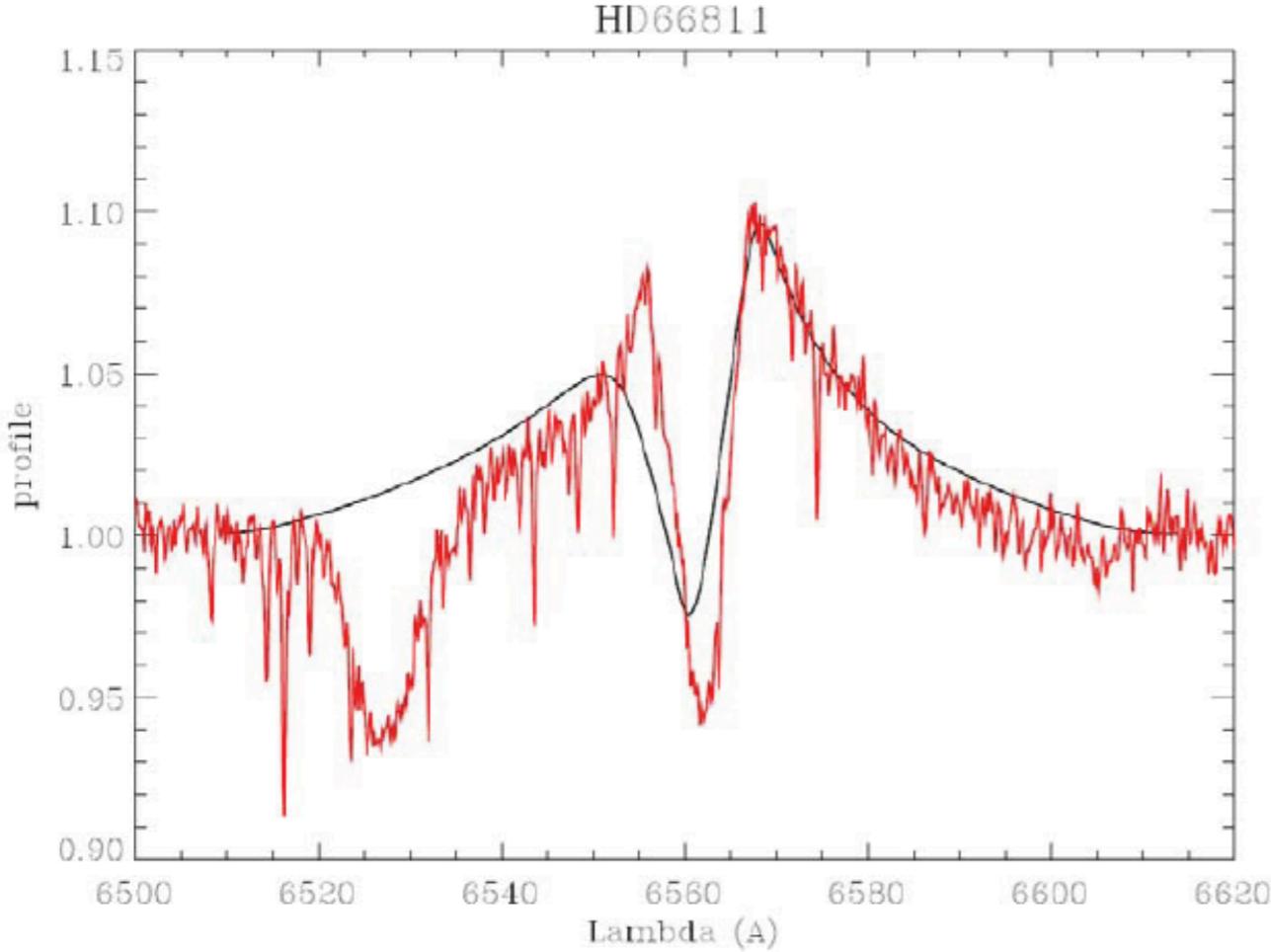


radio

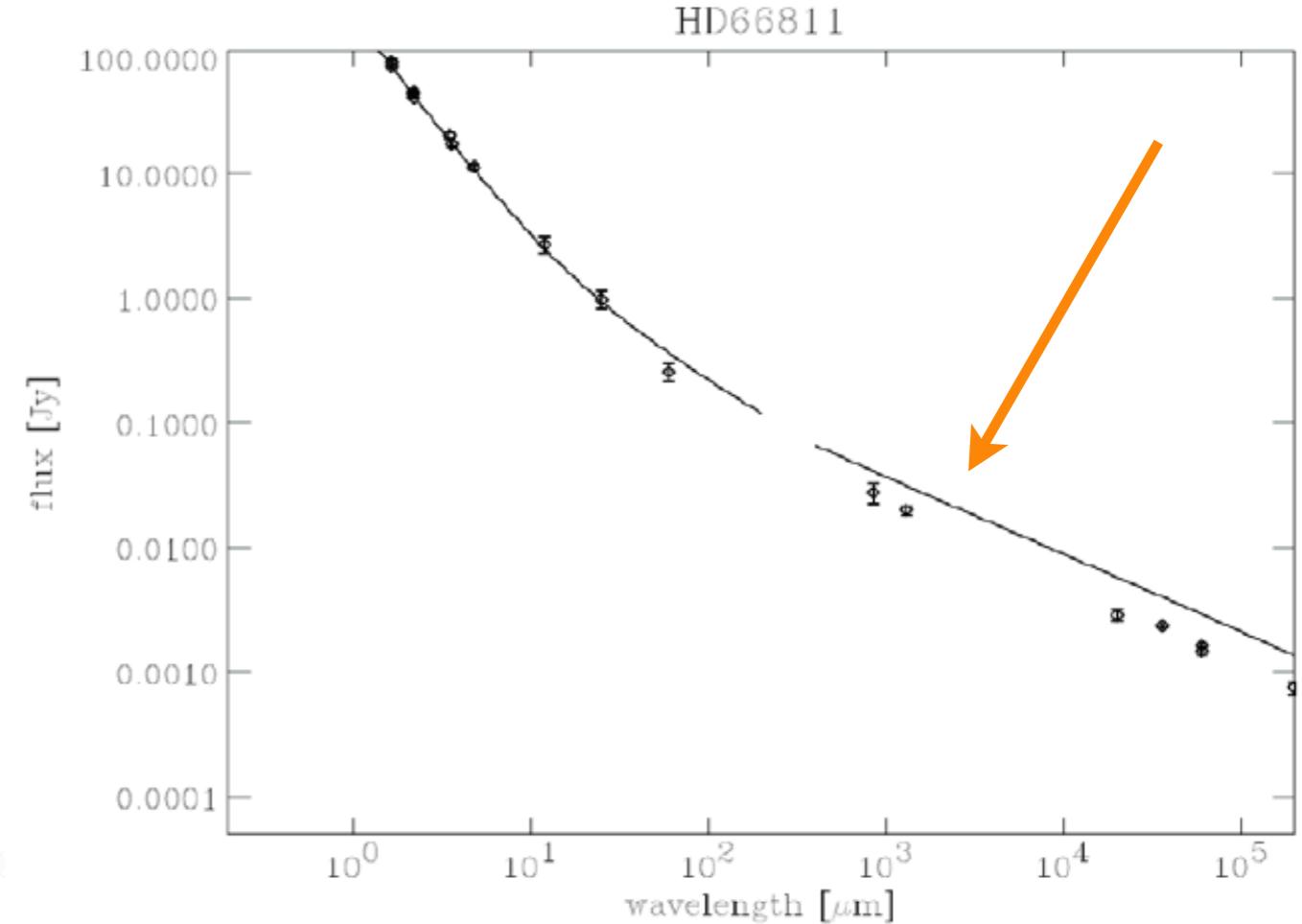
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for  $\dot{M} = 7 \times 10^{-6} M_{\text{sun}}/\text{yr}$

H $\alpha$



IR

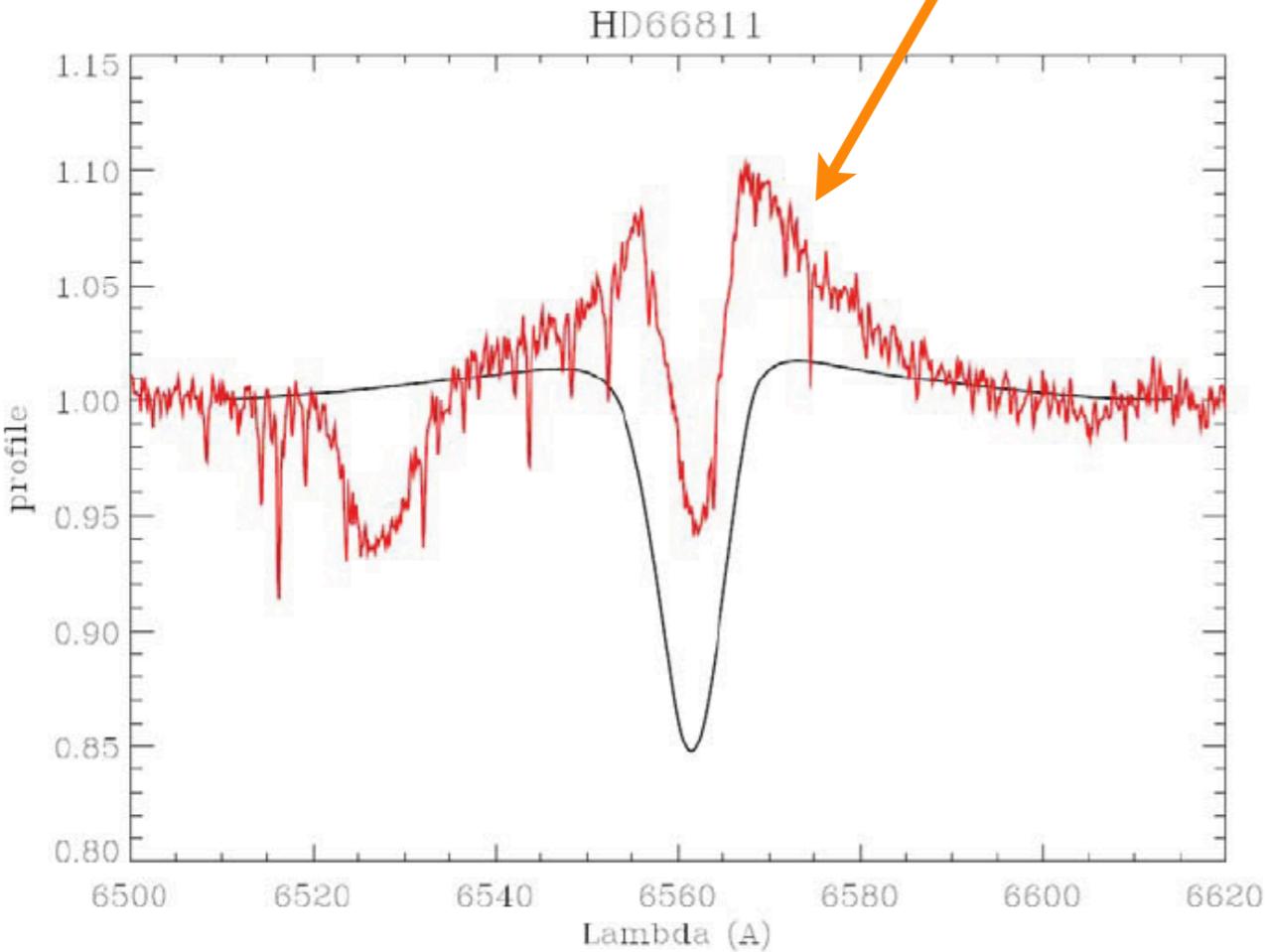


radio

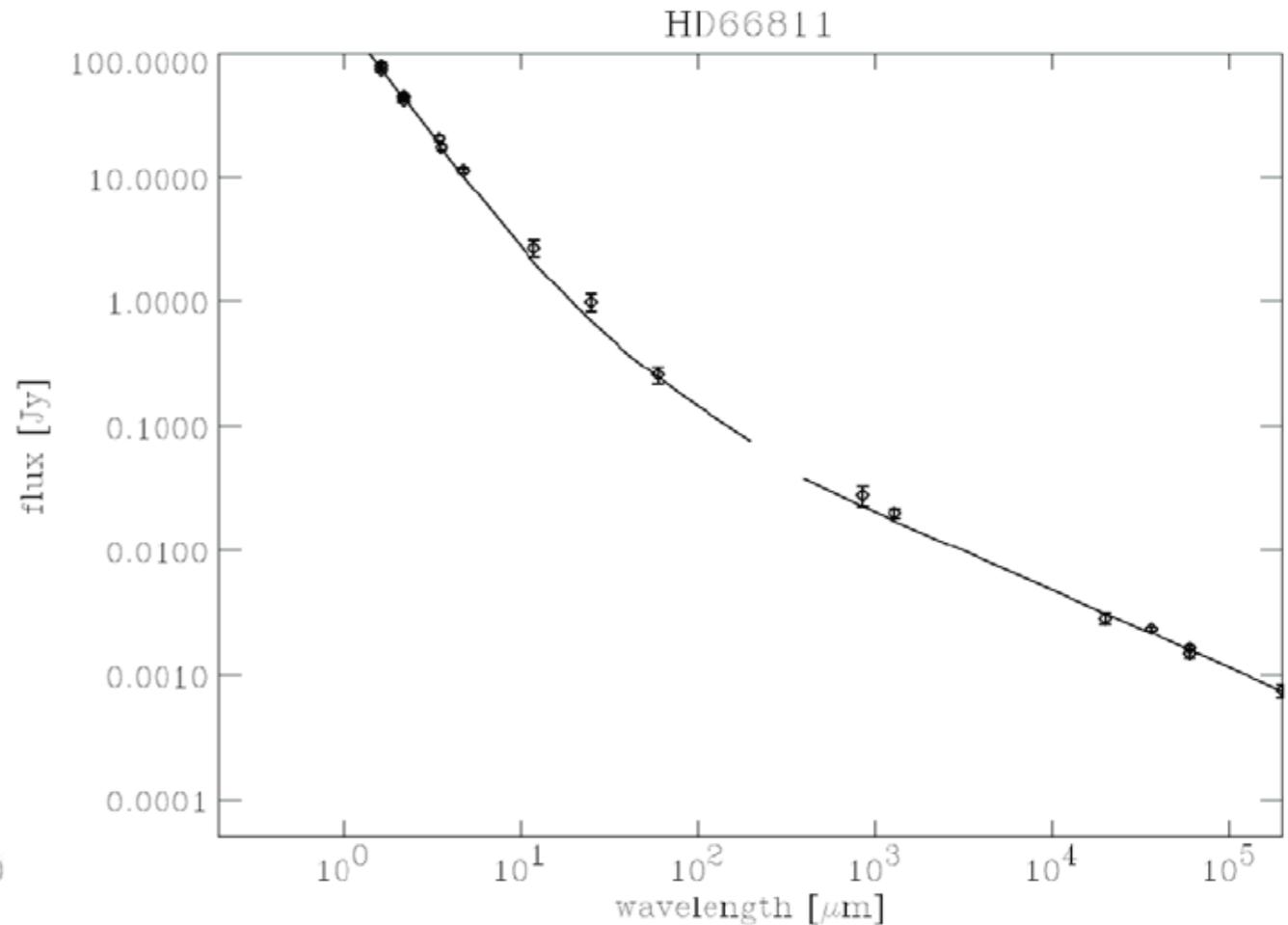
# $\zeta$ Pup: without clumping, $\dot{M}$ discrepancies

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

H $\alpha$



IR



radio

# Clumping's effect

*assumptions:* optically thin clumps,  
void interclump medium

$$f_{\text{cl}} \equiv \langle \rho^2 \rangle / \langle \rho \rangle^2$$

$$f_{\text{cl}} \equiv f_{\text{vol}}^{-1}$$

volume filling factor,  
 $f_{\text{vol}}$

$$\rho_{\text{cl}} = f_{\text{cl}} \langle \rho \rangle$$

$$\dot{\mathcal{M}}_{\text{cl}} \equiv \dot{\mathcal{M}}_{\text{smooth}} / f_{\text{cl}}^{0.5}$$

ignoring clumping overestimates mass-loss rates  
by a factor of  $\sqrt{f_{\text{cl}}}$

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ignoring clumping overestimates mass-loss rates  
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for *density squared* diagnostics

## Aside/explanation

collisional processes (e.g. recombination ( $H\alpha$ ) or free-free (IR, radio excess)) have intensities that scale as  $\rho^2 * \text{Volume}$

if clumps fill a fraction of the volume, the density of clumps exceeds the mean density by the same fraction, and the intensity scales as:

$$(\rho/f_{\text{vol}})^2 \times (f_{\text{vol}} \text{Volume}) \propto I/f_{\text{vol}} = f_{\text{cl}}$$

and since  $\dot{M} \propto \rho$  and measured intensity  $\propto \rho^2$  then  $\dot{M}$  will be overestimated by a factor of  $\sqrt{f_{\text{cl}}}$  if clumping is ignored in the analysis of density-squared diagnostics

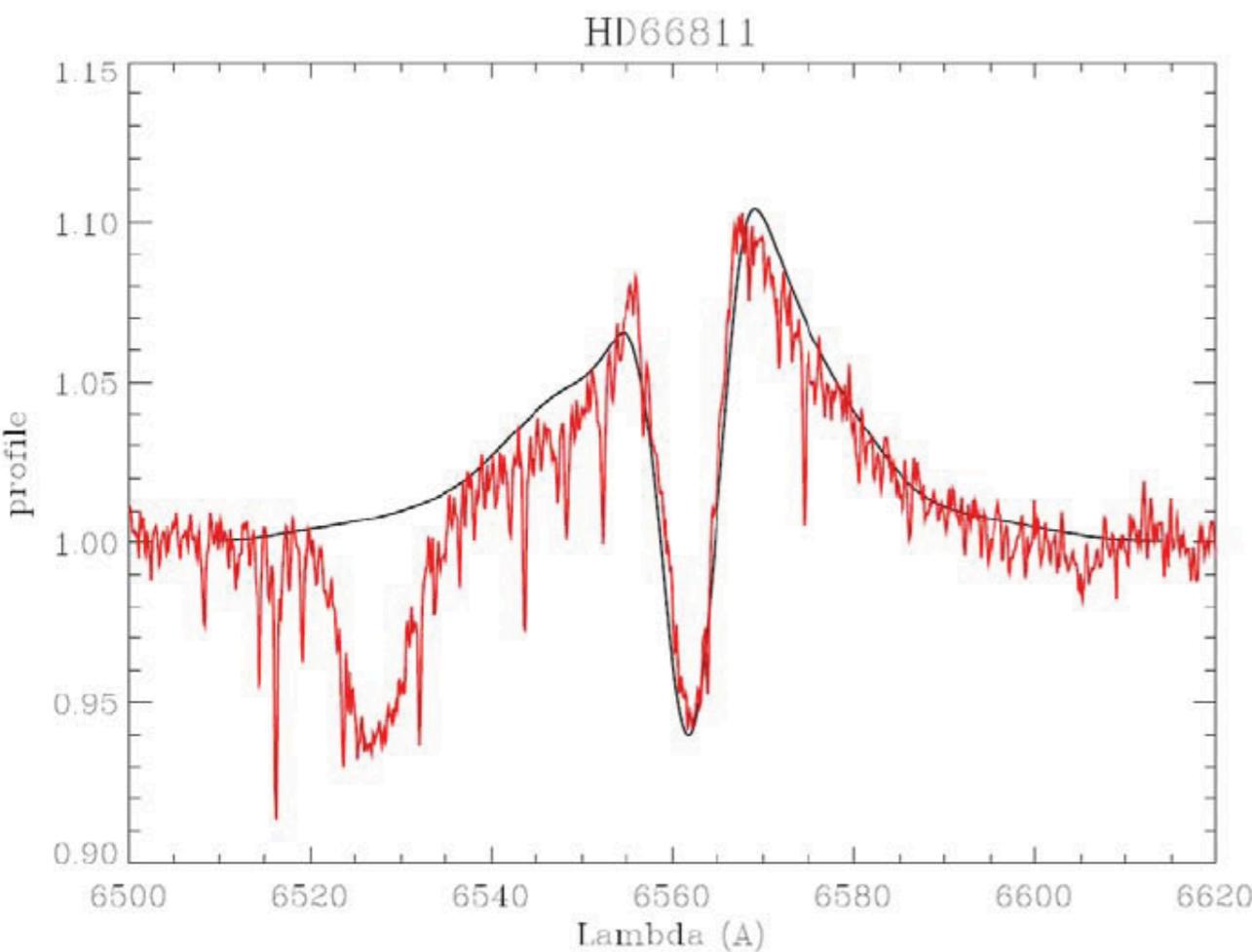
# $\zeta$ Pup: with clumping

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

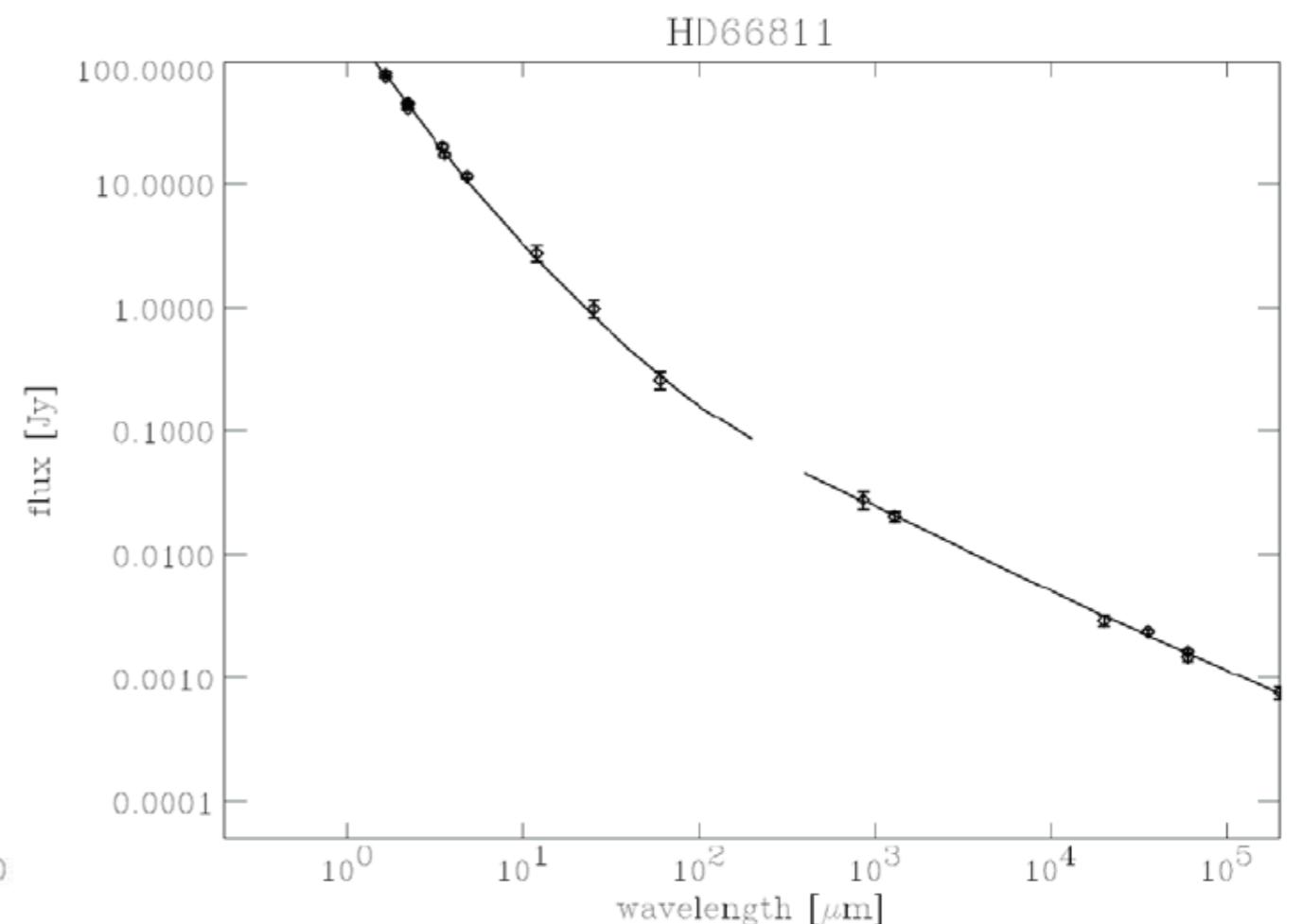
and no clumping in the radio regime ( $> 10 R_{\star}$ )

but with clumping in the H $\alpha$  regime ( $< 1.5 R_{\star}$ )

H $\alpha$



IR



radio

# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

$$f_{\text{cl}} = 1 \text{ @ } r < 1.12 R_{\ast}$$

$$f_{\text{cl}} = 5.5 \text{ @ } 1.12 < r < 1.5 R_{\ast}$$

$$f_{\text{cl}} = 3.1 \text{ @ } 1.5 < r < 2 R_{\ast}$$

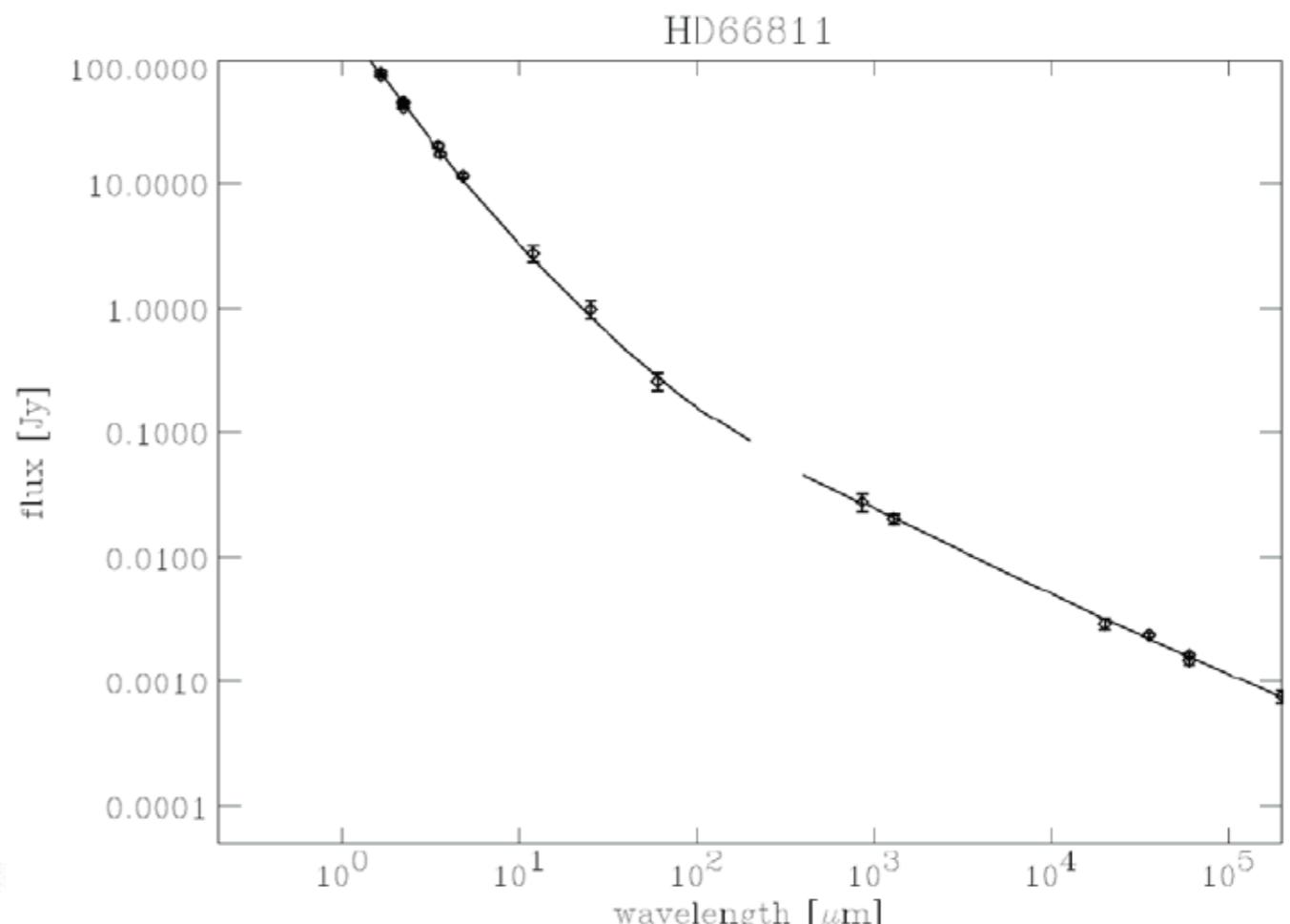
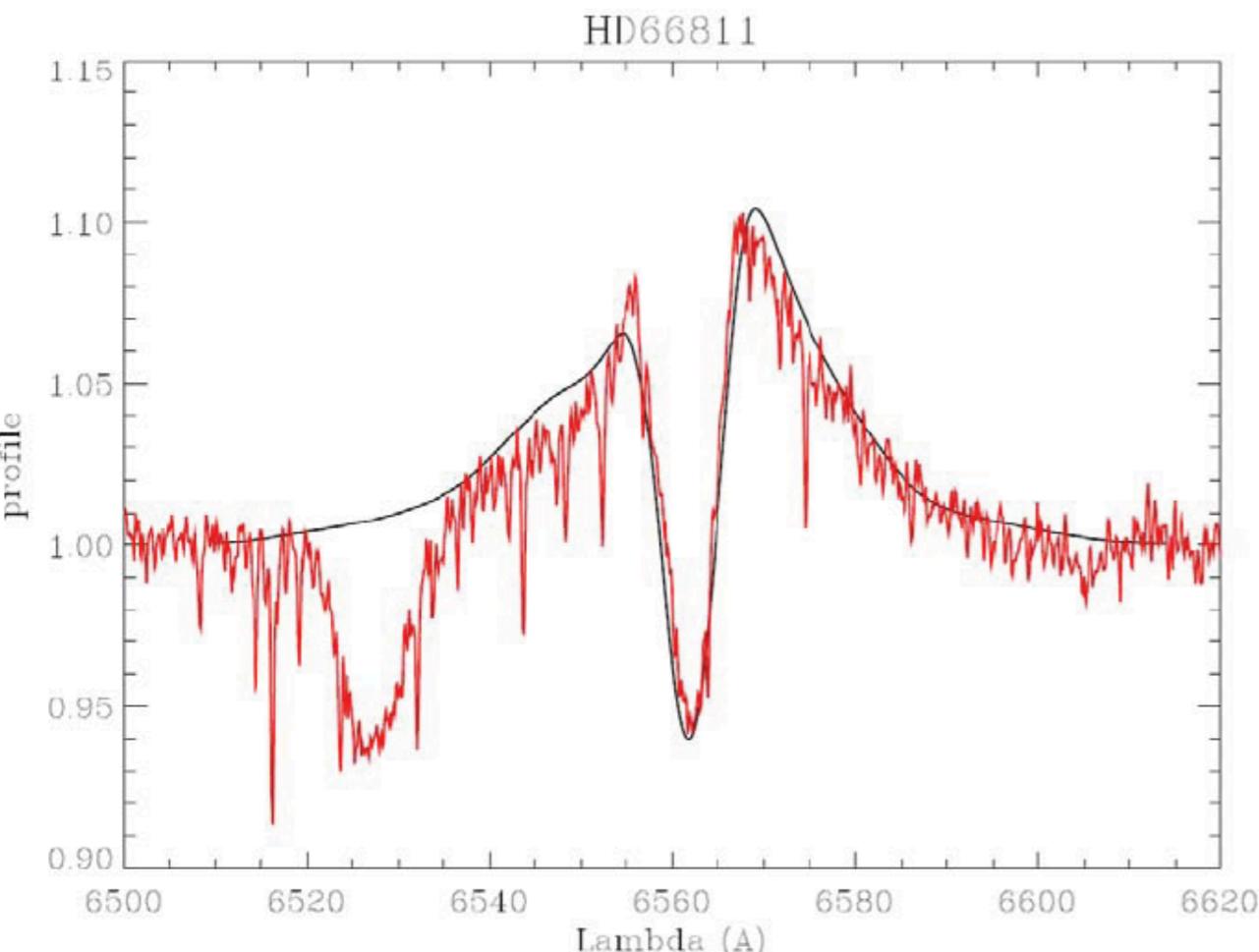
$$f_{\text{cl}} = 2 \text{ @ } 2 < r < 15 R_{\ast}$$

$$f_{\text{cl}} = 1 \text{ @ } r > 15 R_{\ast}$$

H $\alpha$

IR

radio



# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

$$f_{\text{cl}} = 1 \quad @ r < 1.12 R_*$$

$$f_{\text{cl}} = 5.5 \quad @ 1.12 < r < 1.5 R_*$$

$$f_{\text{cl}} = 3.1 \quad @ 1.5 < r < 2 R_*$$

$$f_{\text{cl}} = 2 \quad @ 2 < r < 15 R_*$$

$$f_{\text{cl}} = 1 \quad @ r > 15 R_*$$

Note: one *family* of solutions; all  $f_{\text{cl}}$  can be scaled up by the same factor (and  $\dot{M}$  scaled down, accordingly)

so  $\dot{M} \leq 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

$$\begin{aligned}f_{\text{cl}} &= 1 @ r < 1.12 R_* \\f_{\text{cl}} &= 5.5 @ 1.12 < r < 1.5 R_* \\f_{\text{cl}} &= 3.1 @ 1.5 < r < 2 R_* \\f_{\text{cl}} &= 2 @ 2 < r < 15 R_* \\f_{\text{cl}} &= 1 @ r > 15 R_*\end{aligned}$$

Also: this is a general trend - clumping factors decrease with radius

# Clumping

Key point: as long as the clumps are optically thin, only the clumping factor (their over-density) matters.

*Their size scale, shape, etc are irrelevant!*

Column density based diagnostics (e.g. some UV abs lines, X-ray emission lines and X-ray SEDs) are *unaffected by optically thin clumping*.

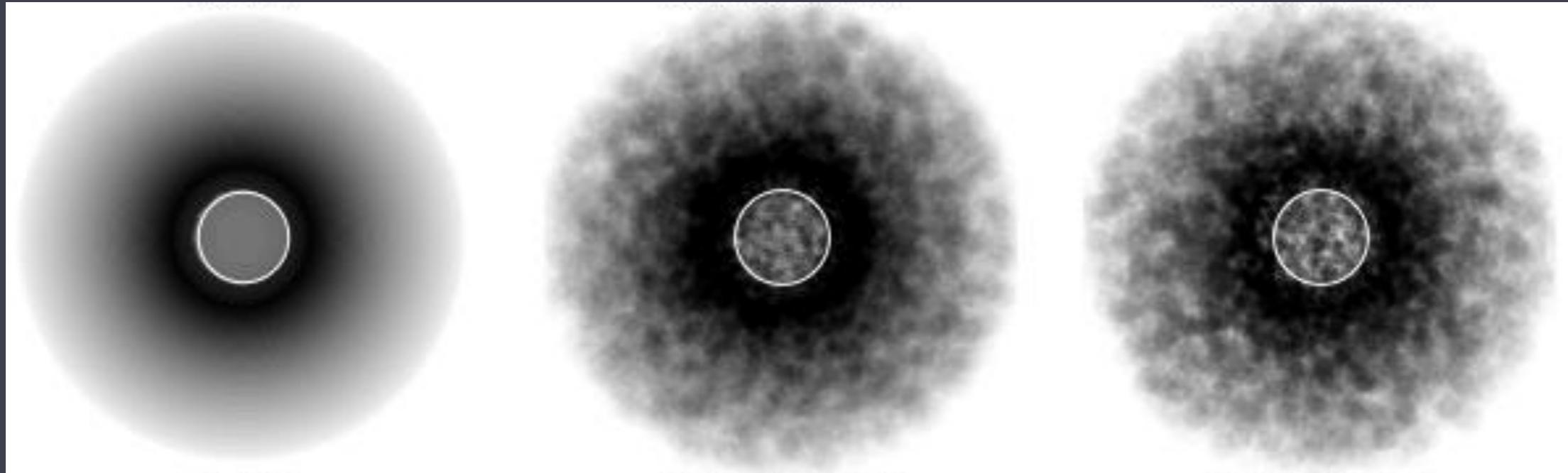
# Visualizations of clumped winds

all have clump sizes  $\ell = 0.1 R_\star$  (at surface; increasing as  $r$ )

$$f_{\text{cl}} = 1$$

$$f_{\text{cl}} \approx 2.5$$

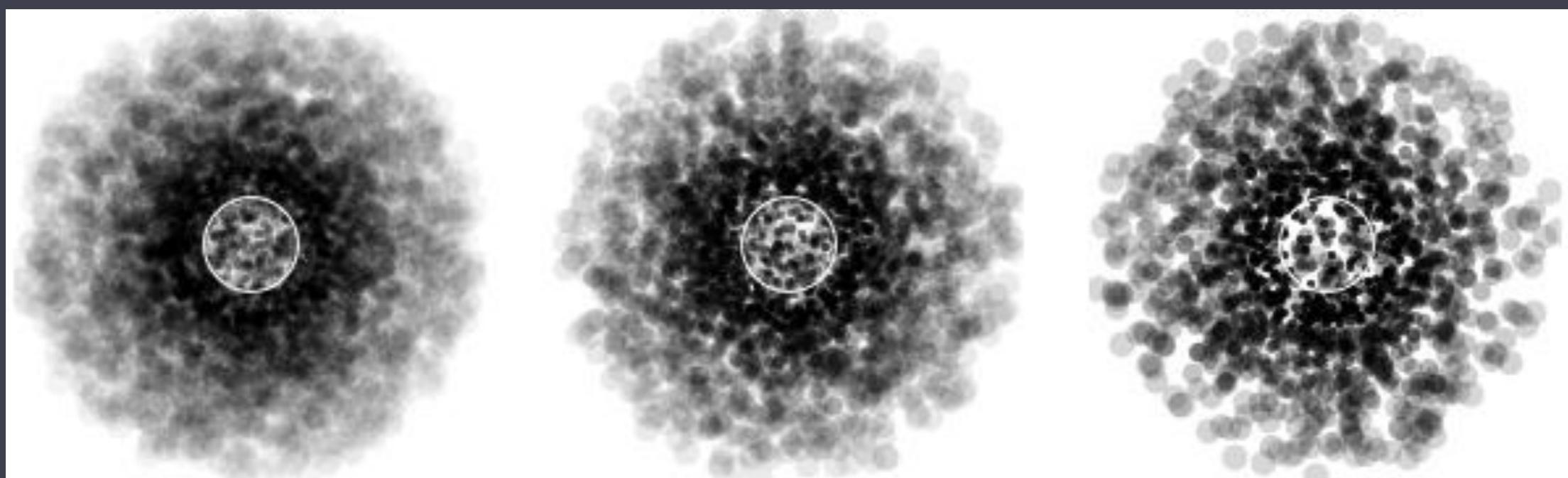
$$f_{\text{cl}} \approx 5$$



$$f_{\text{cl}} \approx 10$$

$$f_{\text{cl}} \approx 20$$

$$f_{\text{cl}} \approx 40$$



# Visualizations of clumped winds

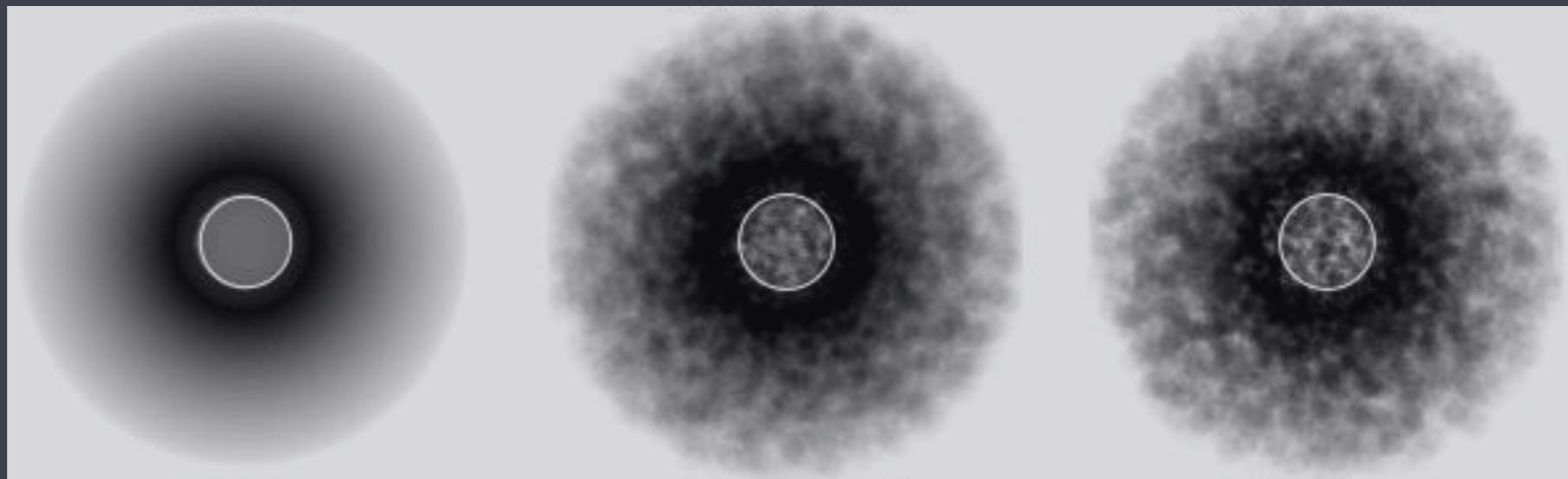
all have same clump sizes

bigger clumping factors = bigger volume over which matter in each clump is collected = more empty space

$f_{\text{cl}} = 1$

$f_{\text{cl}} \approx 2.5$

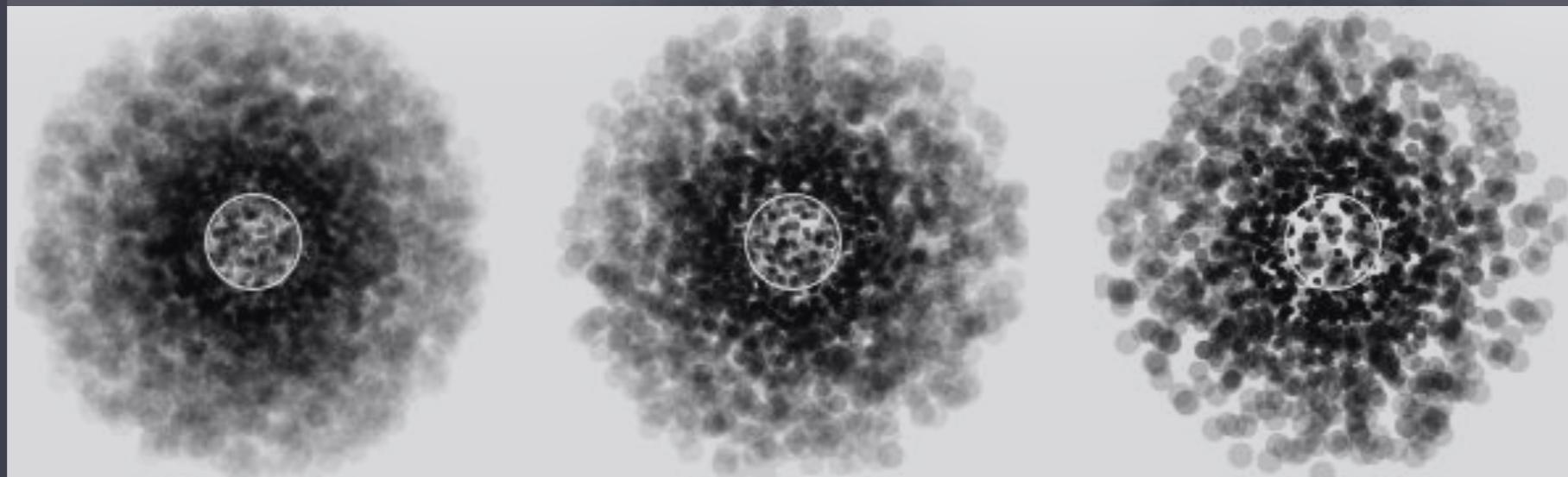
$f_{\text{cl}} \approx 5$



$f_{\text{cl}} \approx 10$

$f_{\text{cl}} \approx 20$

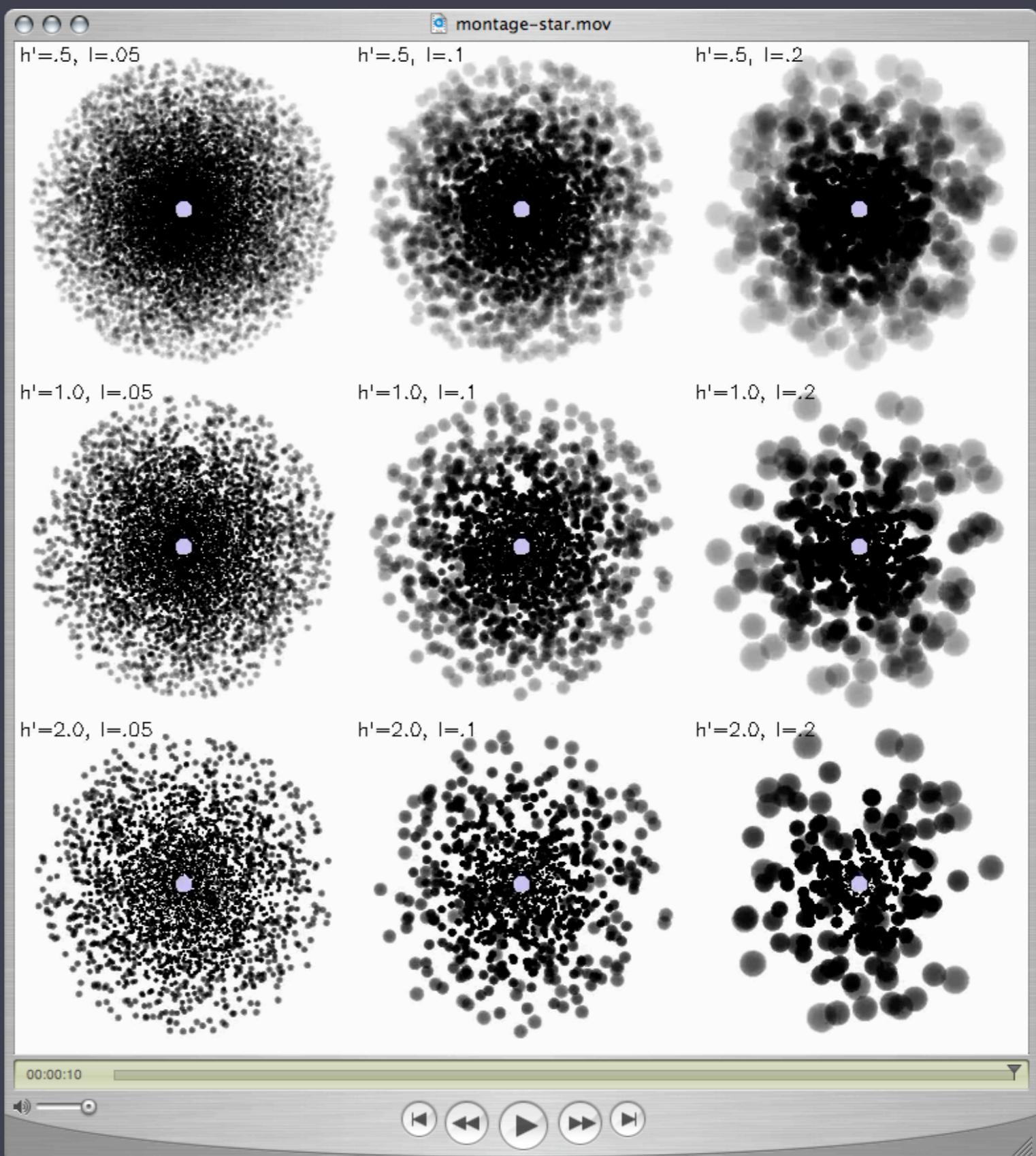
$f_{\text{cl}} \approx 40$



# Porosity

optically thick  
clumps

enhances photon  
escape through  
evacuated channels



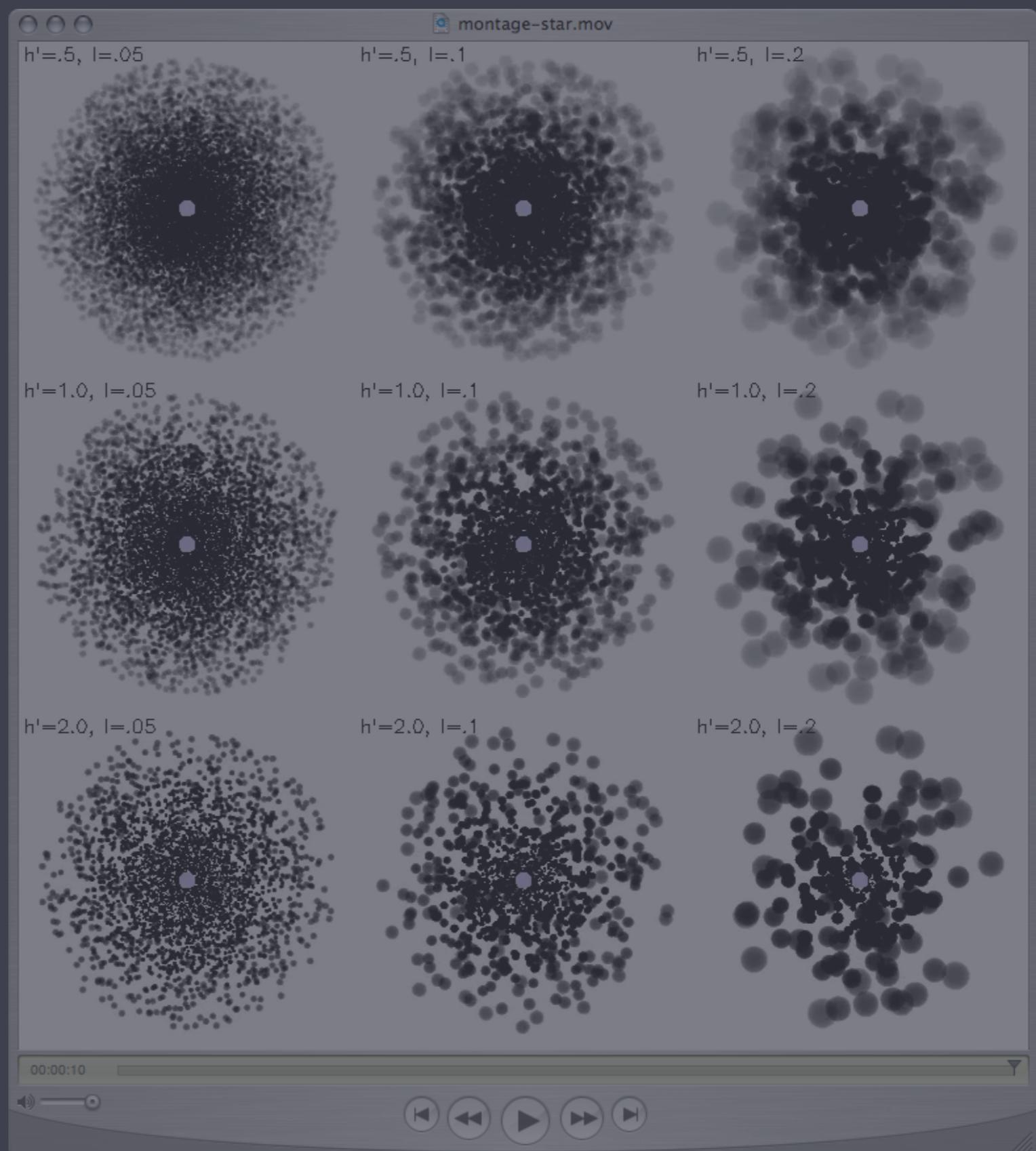
# Porosity

optically thick  
clumps

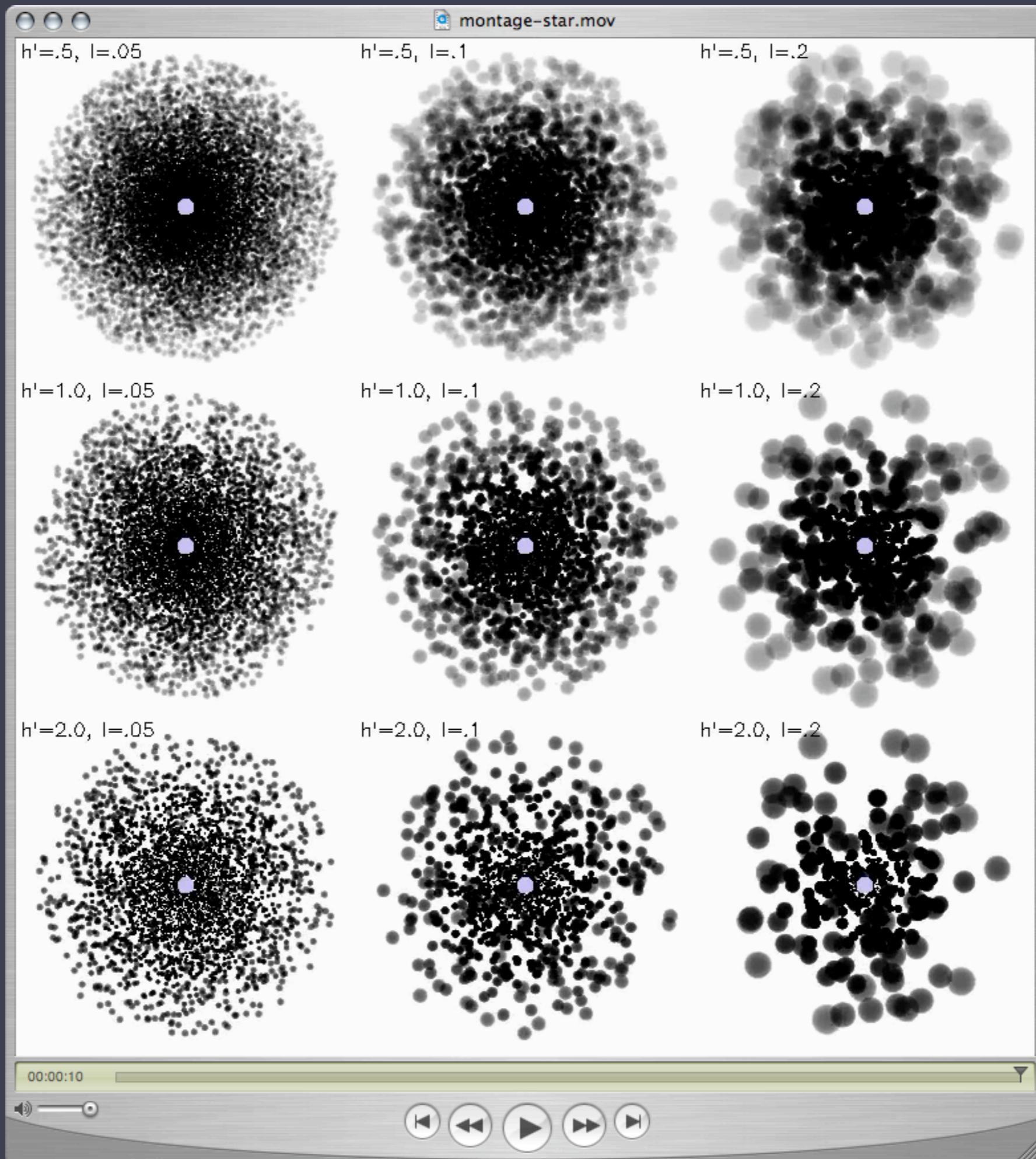
Thus, porosity only  
exists if there's

clumping

But, you *can* have  
clumping without  
having porosity

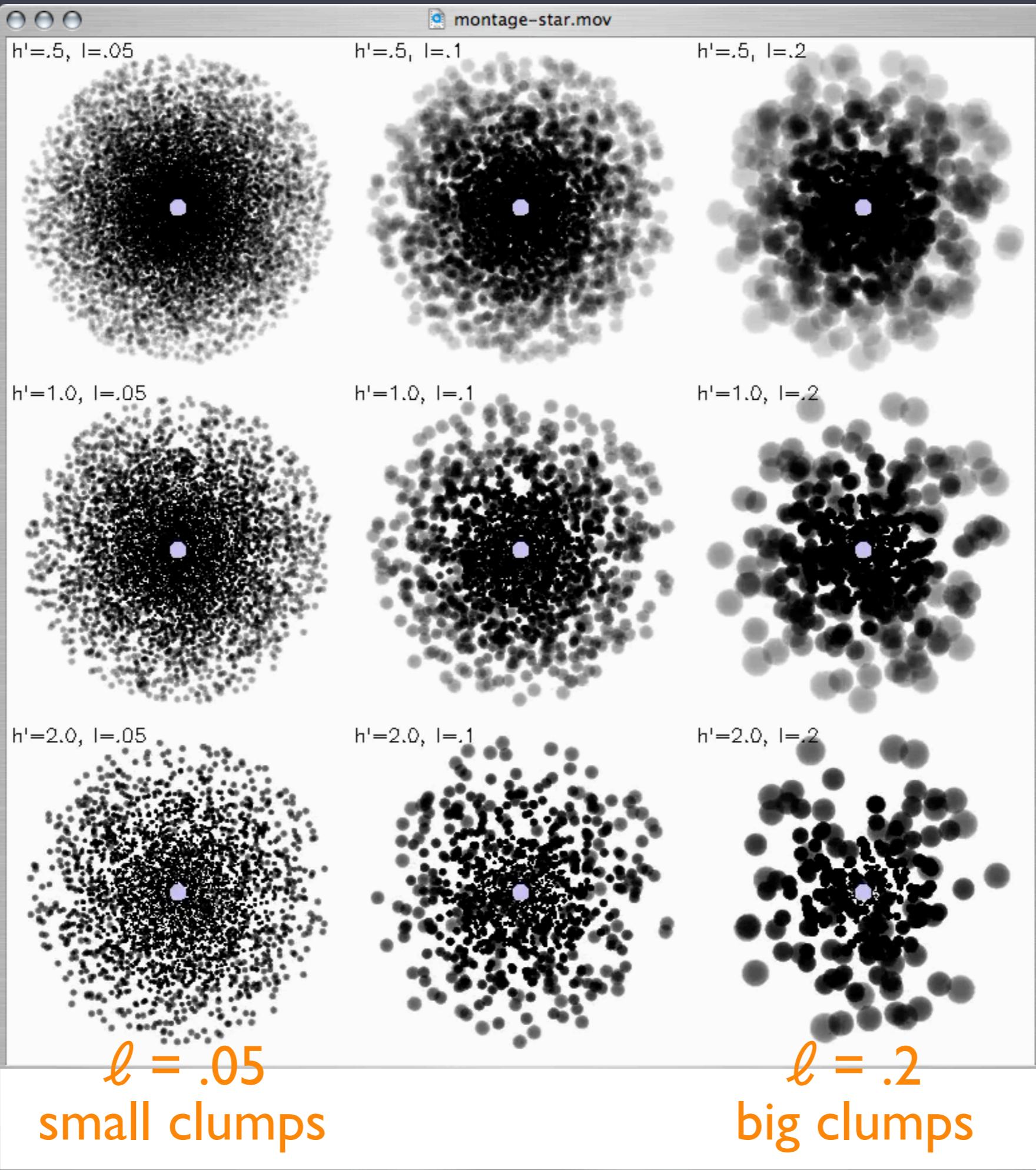


less  
porous



more  
porous

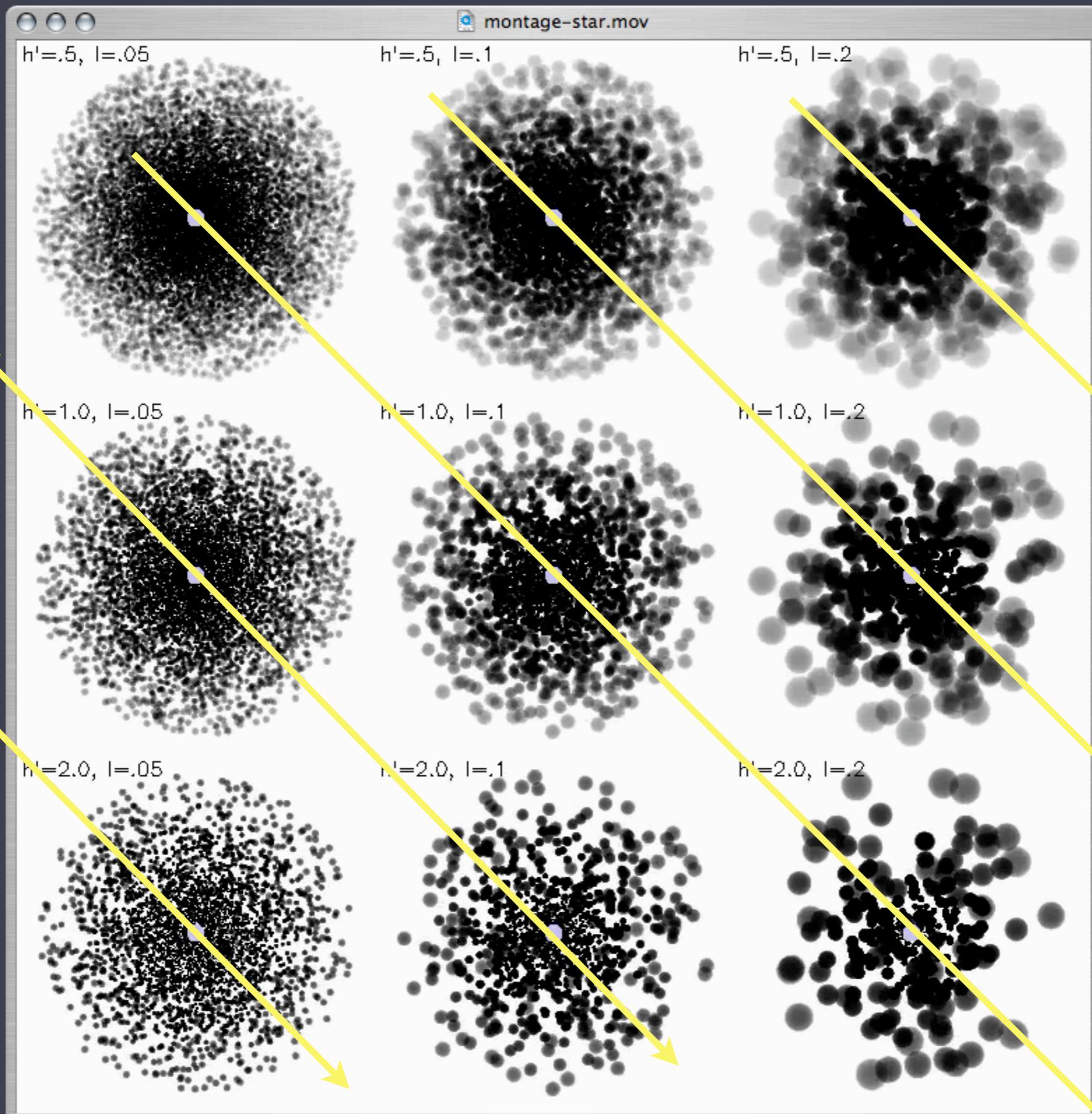
less  
porous



less  
porous  
 $f_{\text{cl}} \sim 20$

$f_{\text{cl}} \sim 40$

more  
porous



small clumps

big clumps

$f_{\text{cl}} \sim 2.5$

$f_{\text{cl}} \sim 5$

$f_{\text{cl}} \sim 10$

# Porosity length

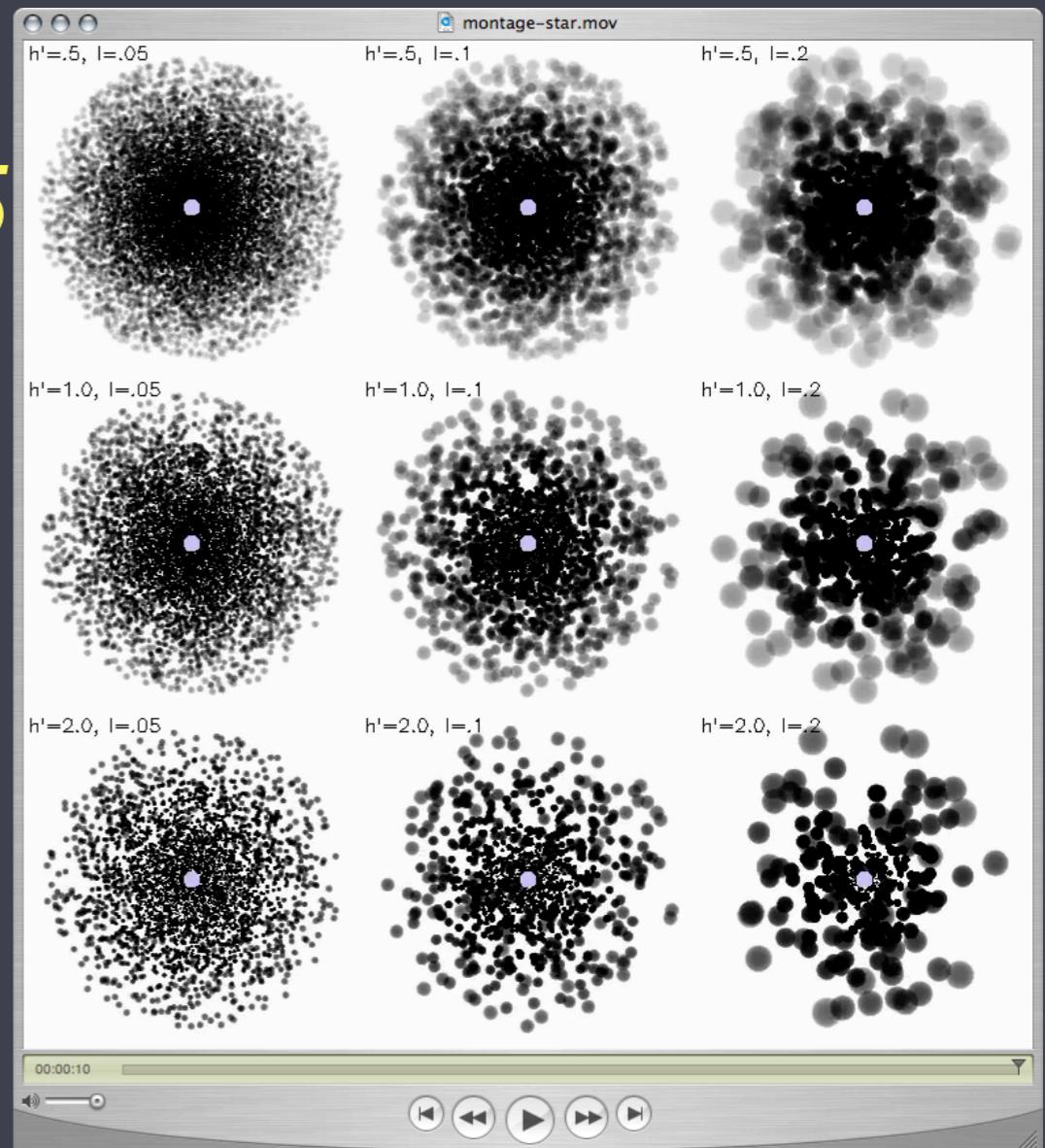
The degree of porosity is characterized by the  
**porosity length,  $h$**

less porous  
 $h=0.5$

$$h \equiv (n_{\text{cl}} A_{\text{cl}})^{-1} (\text{ = mfp})$$
$$= L^3 / \ell^2 = \ell / f_{\text{vol}} = \ell * f_{\text{cl}} \quad h=1$$

$$f_{\text{vol}} \equiv \ell^3 / L^3 \text{ or } f_{\text{cl}} = L^3 / \ell^3$$

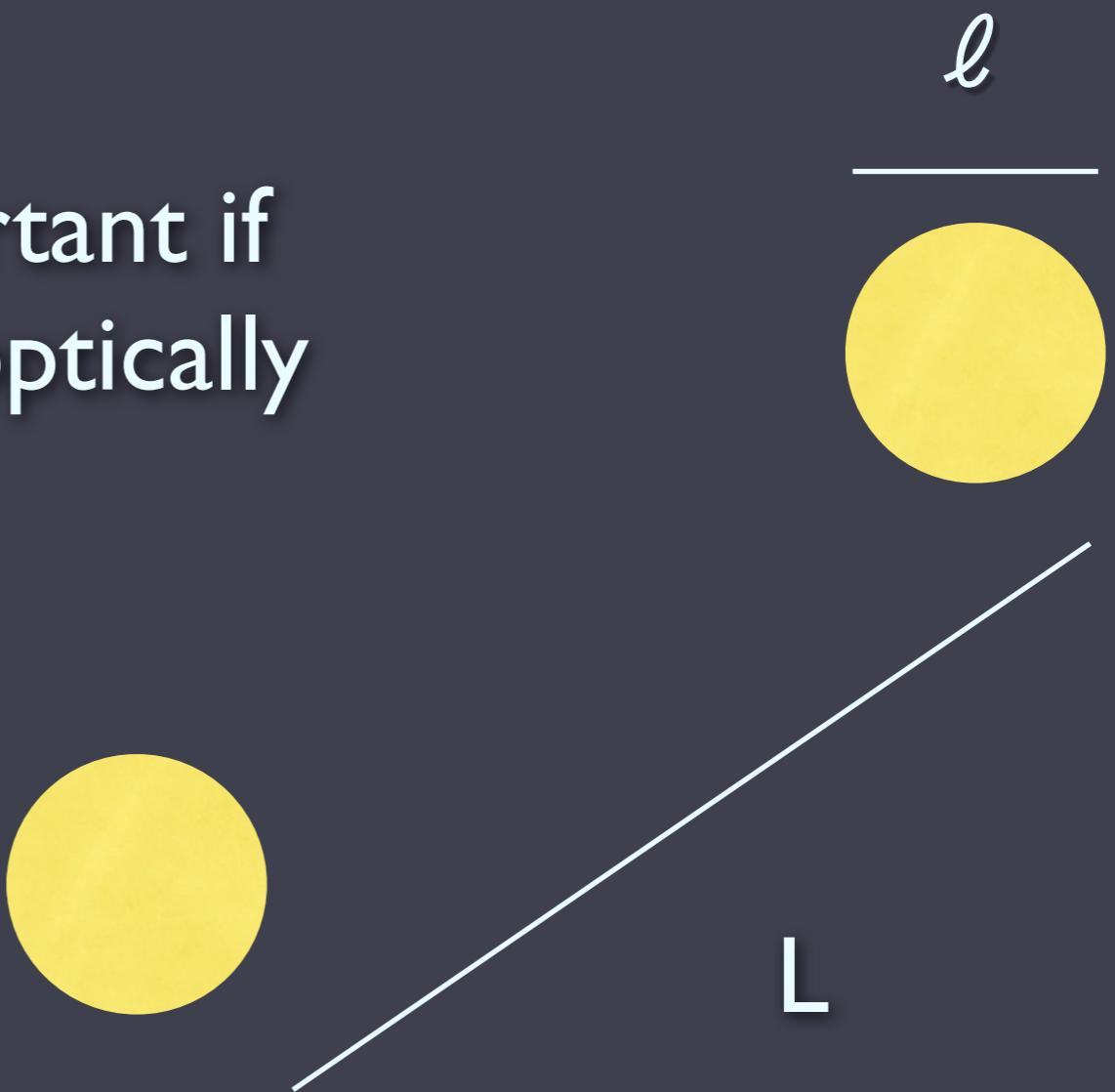
$h=2$   
more porous



# Summary of porosity considerations

*porosity length,  $h$*  = mean free path  
between clumps

porosity is only important if  
individual clumps are optically  
thick

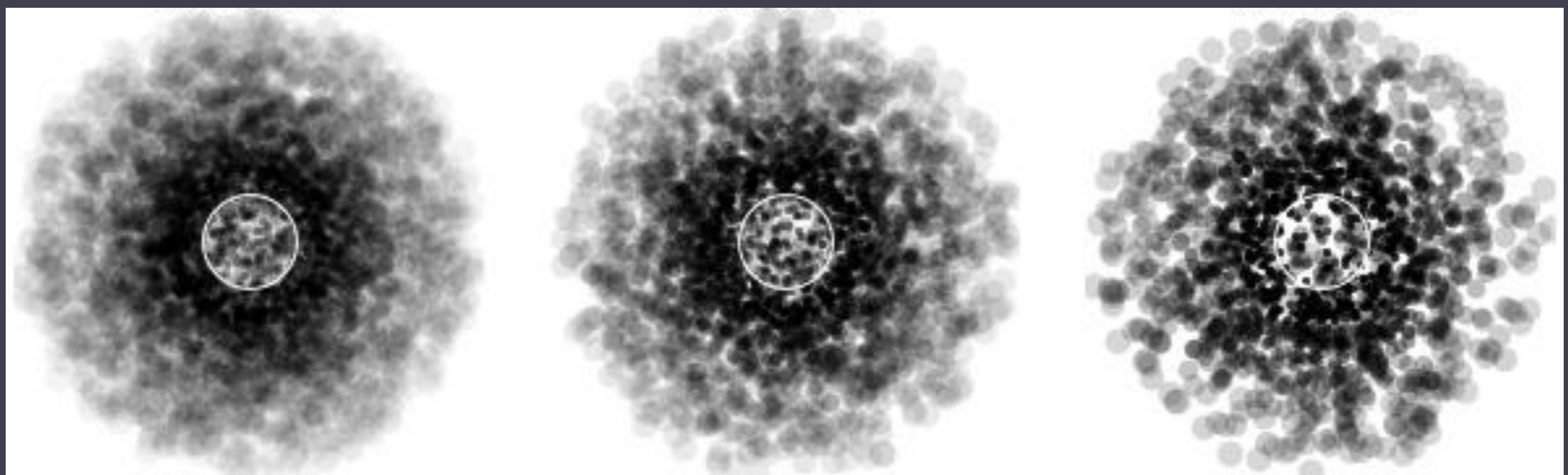


# Quantitative treatment of porosity

porosity reduces the effective opacity of the wind

$$K_{\text{eff}} \equiv \ell^2/m_{\text{cl}} \text{ vs. } K \equiv \sigma_{\text{atom}}/m_{\text{atom}}$$

$$\tau_{\text{cl}} = K \rho_{\text{cl}} \ell = K \langle \rho \rangle \ell f_{\text{cl}} = K \langle \rho \rangle h$$



# Quantitative treatment of porosity

porosity reduces the effective opacity of the wind

$$K_{\text{eff}} \equiv \ell^2/m_{\text{cl}} \quad \text{vs.} \quad K \equiv \sigma_{\text{atom}}/m_{\text{atom}}$$

$$\tau_{\text{cl}} = K \rho_{\text{cl}} \ell = K \langle \rho \rangle \ell f_{\text{cl}} = K \langle \rho \rangle h$$

in radiation transport, simply replace  $K$  with  $K_{\text{eff}}$  where

$$K_{\text{eff}} = K / (1 + \tau_{\text{cl}})$$

porosity length,  $h$ ,  
is the only new  
parameter

# Testing models of clumping and porosity with data

...or, measuring  $f_{\text{cl}}$  and  $h$

# Testing models of clumping and porosity with data

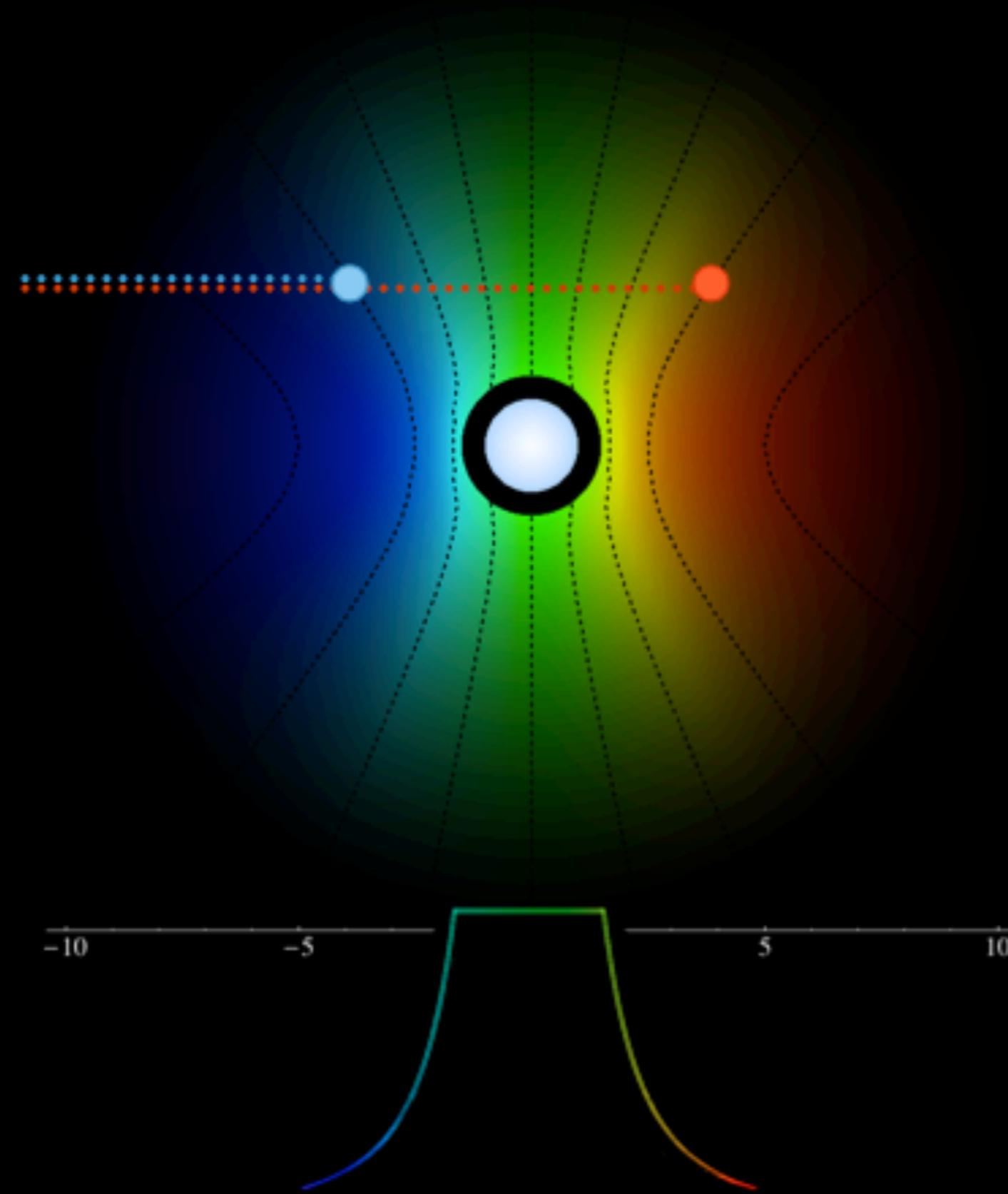
...or, measuring  $f_{\text{cl}}$  and  $h$

first, consider emission line profiles,  
ignoring clumping and porosity for now

# Line Asymmetry

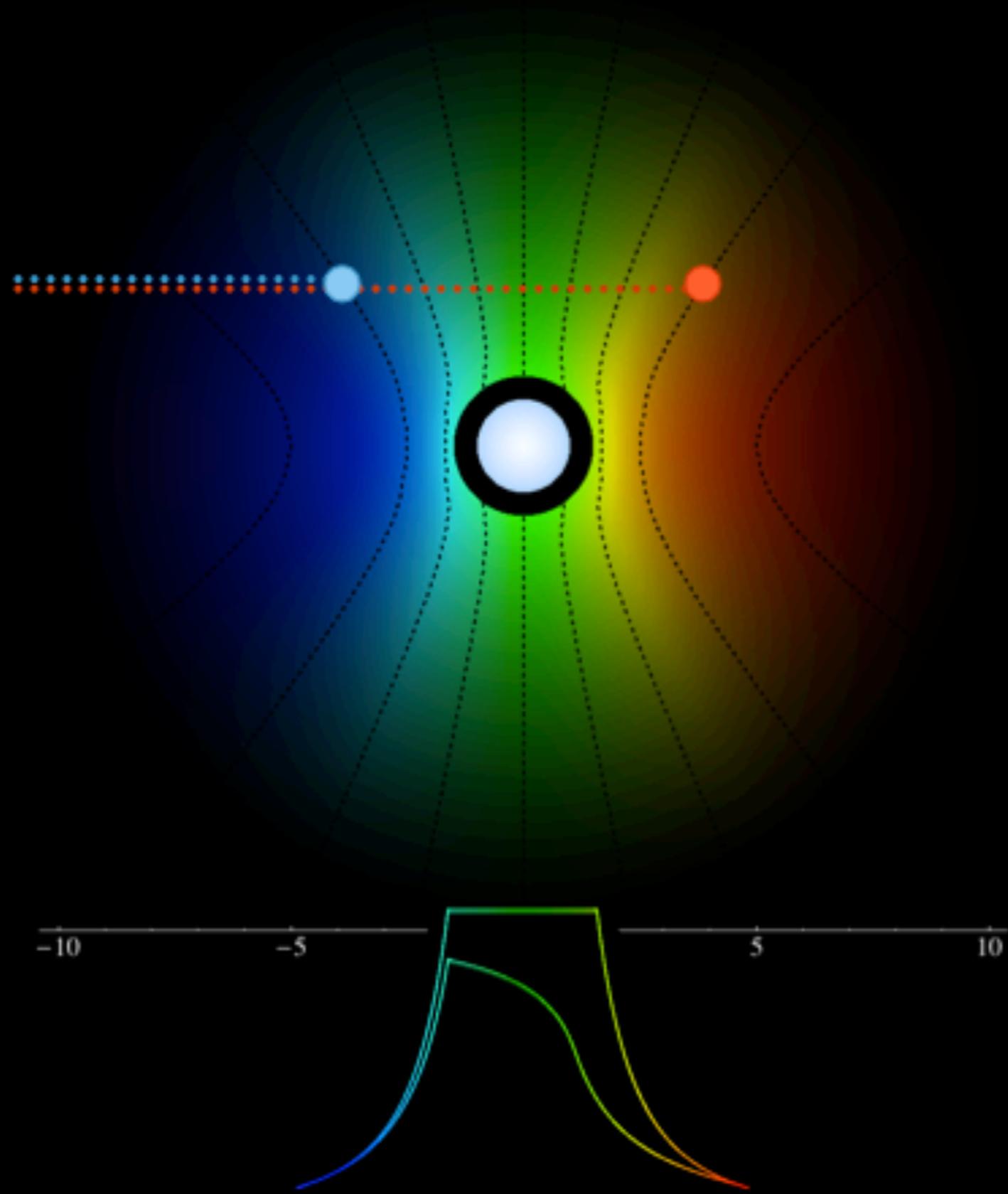
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A



# Line Asymmetry

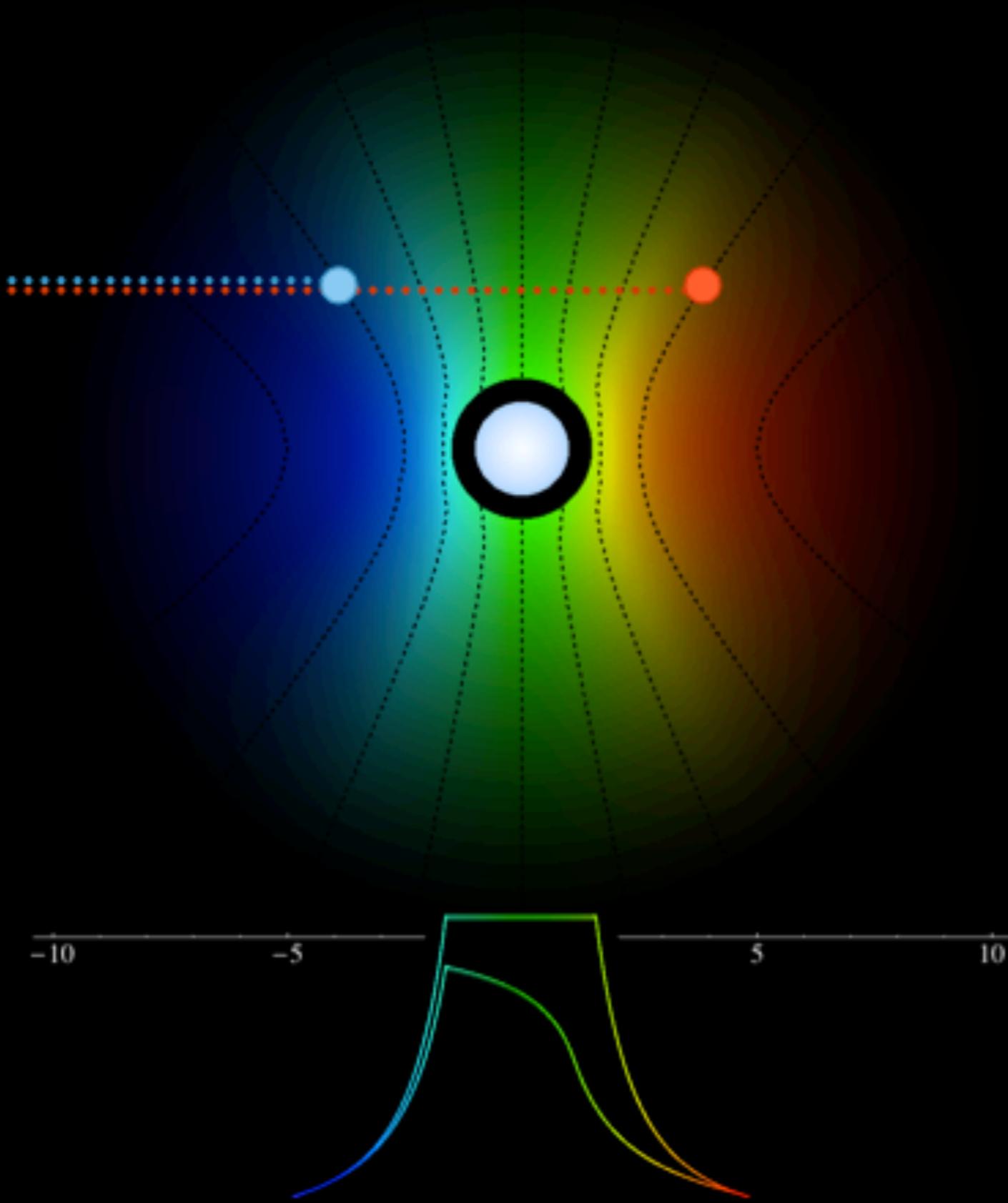
A



# Line Asymmetry

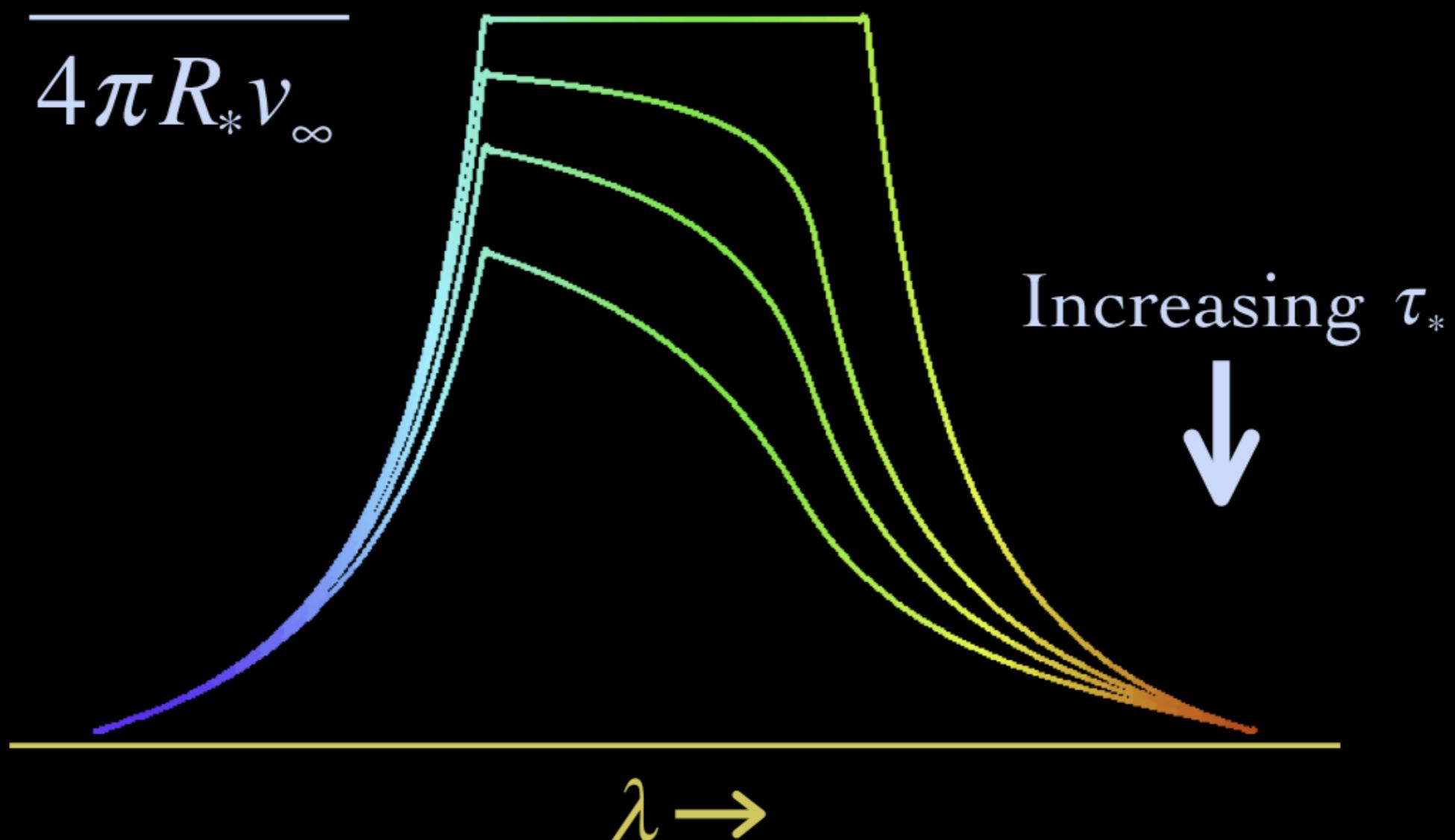
$$\tau = \tau_* \int_z^\infty \frac{R_* dz'}{r'^2 (1 - \frac{R_*}{r'})^\beta}$$

A



# Wind Profile Model

$$\tau_* = \frac{\kappa \dot{M}}{4\pi R_* v_\infty}$$



# Quantifying the wind optical depth

opacity of the cold wind component (due to bound-free transitions in C, N, O, Ne, Fe)

wind mass-loss rate

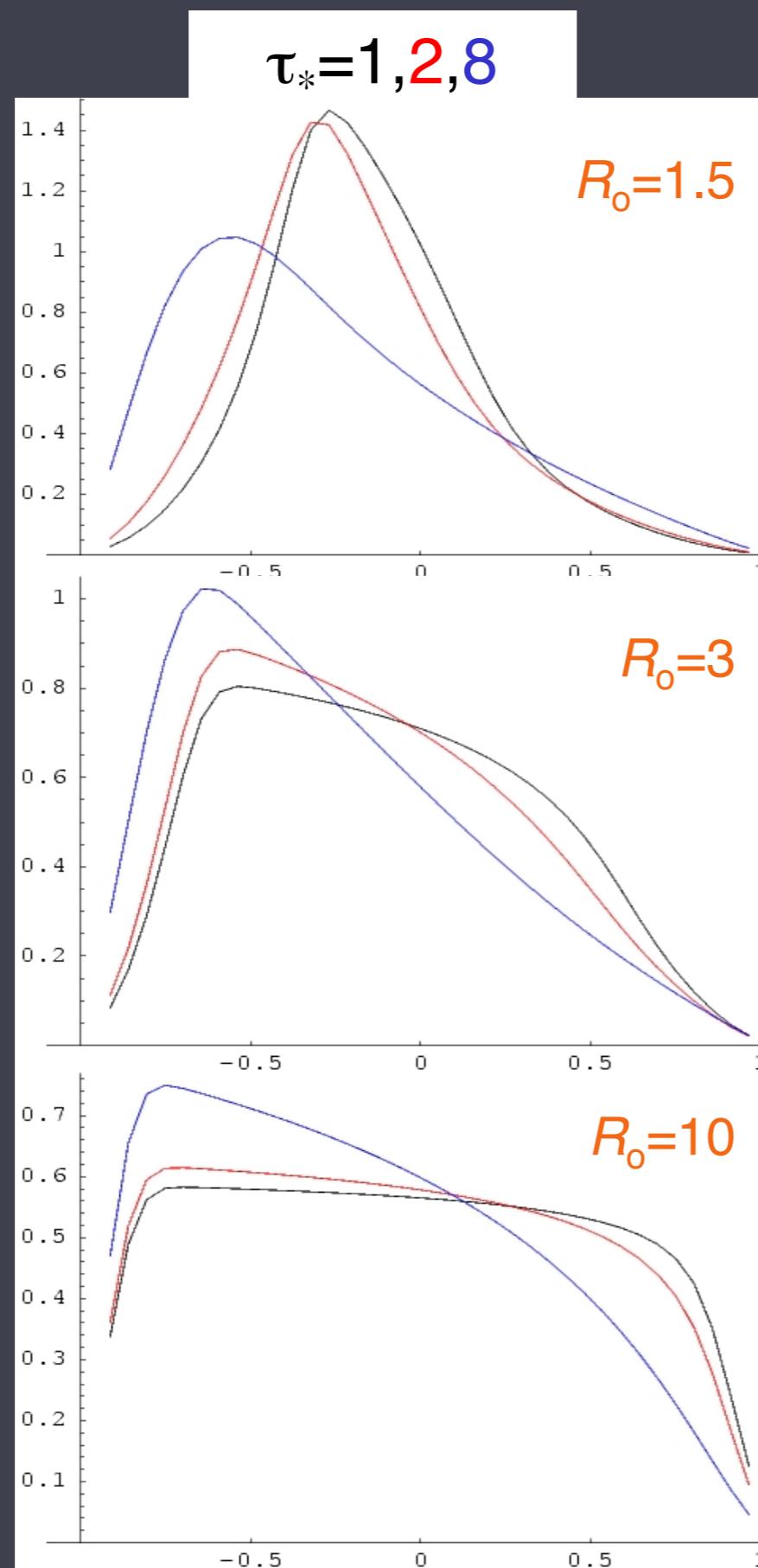
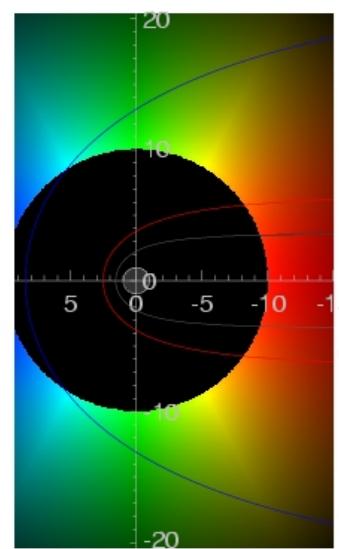
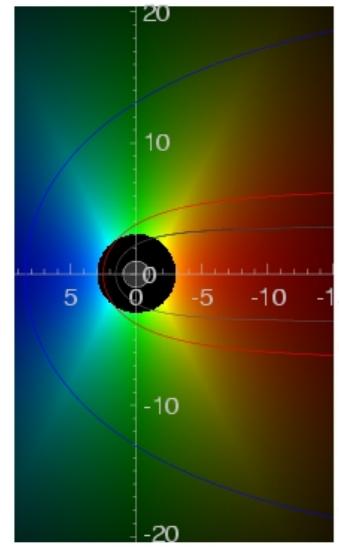
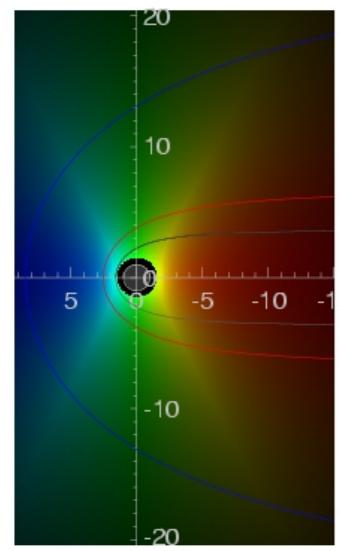
$$\dot{M} = 4\pi r^2 v \rho$$

$$\tau_* \equiv \frac{\kappa M}{4\pi R_* v_\infty}$$

stellar radius

wind terminal velocity

# Line profile shapes



key parameters:  $R_o$  &  $\tau_*$

$$j \sim \rho^2 \text{ for } r/R_* > R_o, \\ = 0 \text{ otherwise}$$

$$\tau = \tau_* \int_z^\infty \frac{R_* dz'}{r'^2 (1 - R_*/r')^\beta}$$

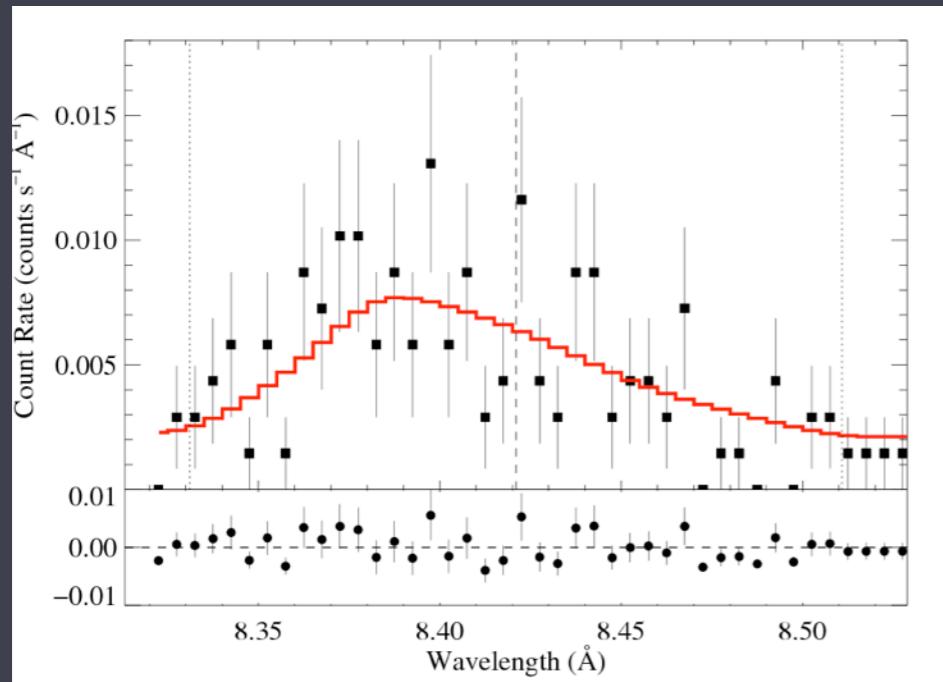
$$\tau_* \equiv \frac{\kappa M}{4\pi R_* v_\infty}$$

# Measurements of $\tau_*$ from line profiles

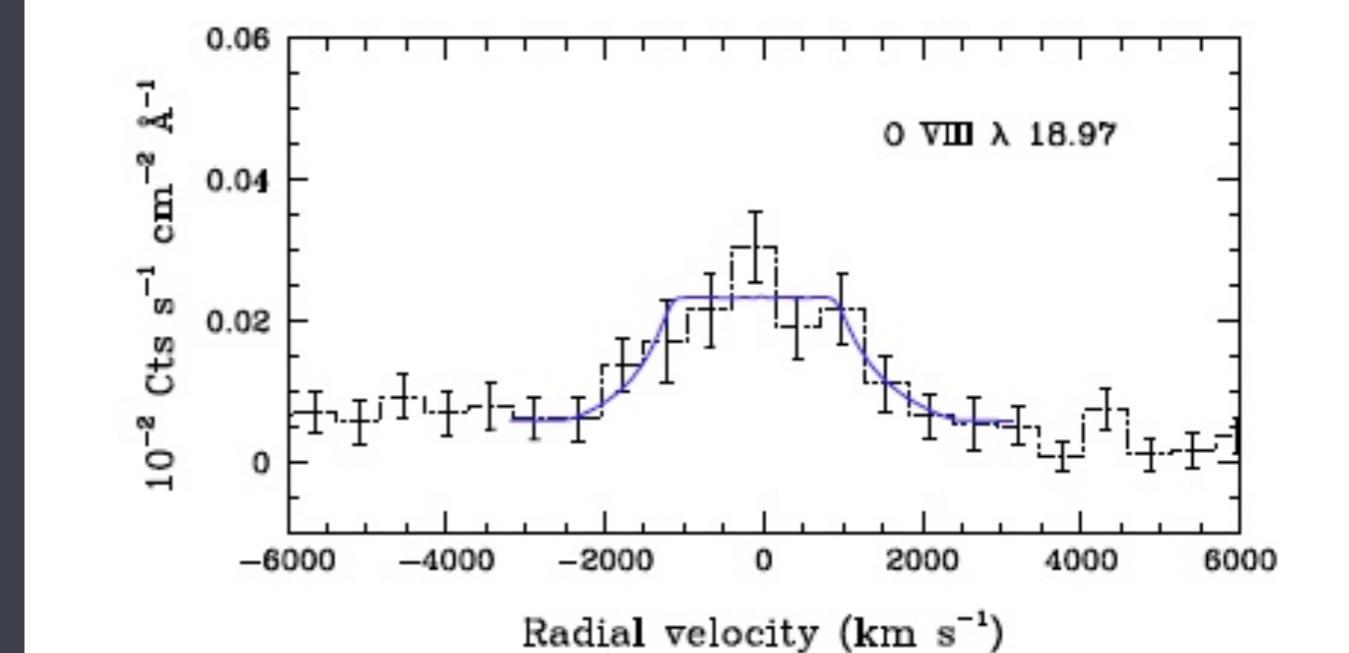
$\zeta$  Ori (Cohen et al. 2006)

$\zeta$  Pup (Cohen et al. 2010)

HD 93129A (Cohen et al. 2011)

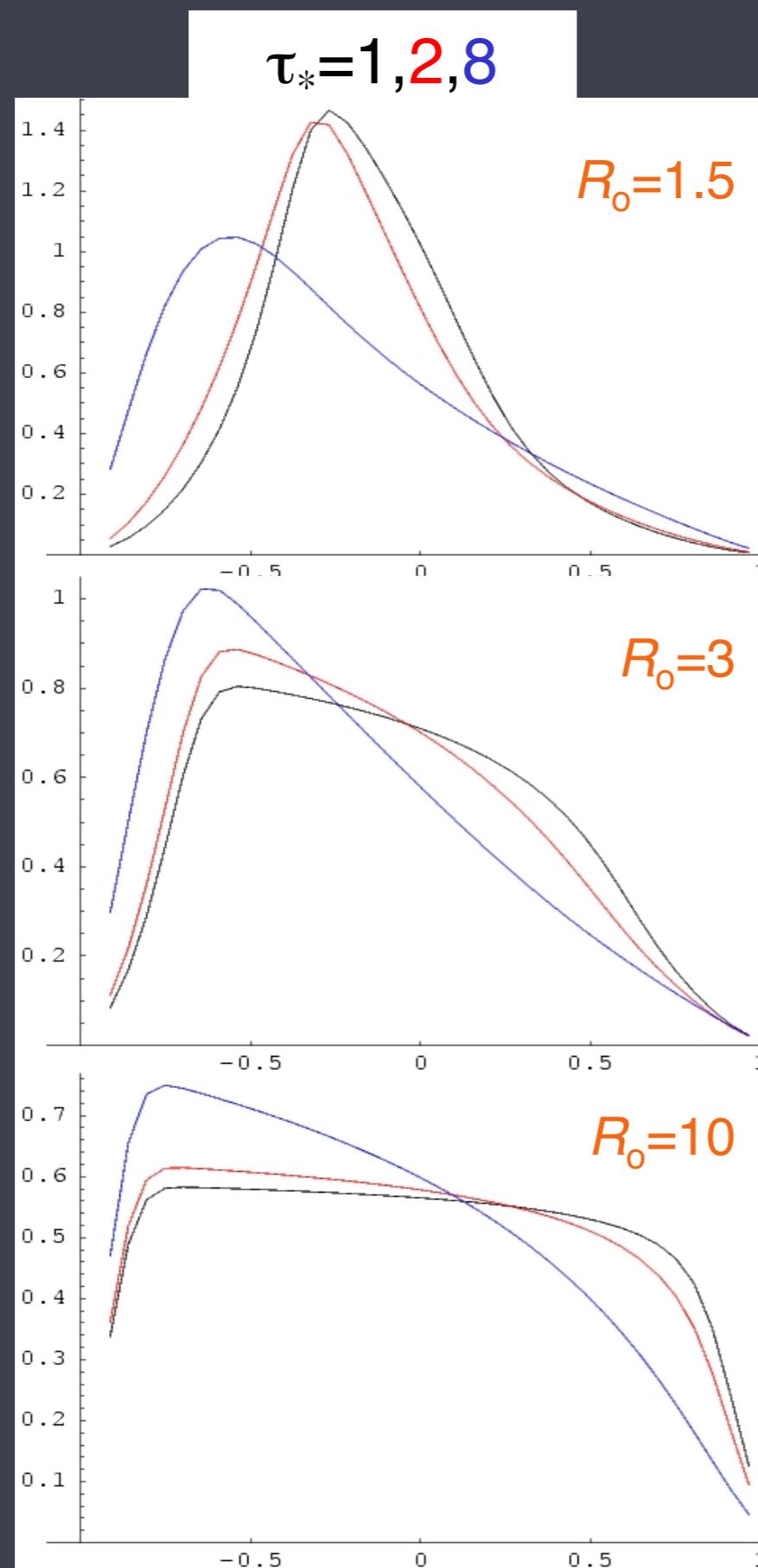
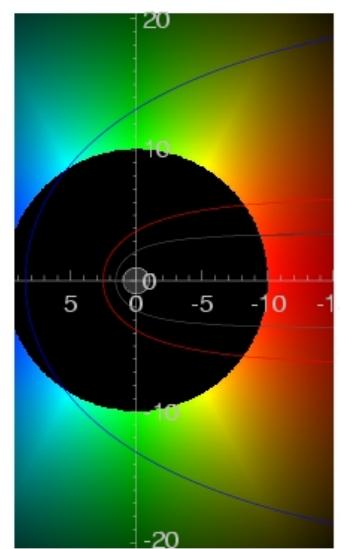
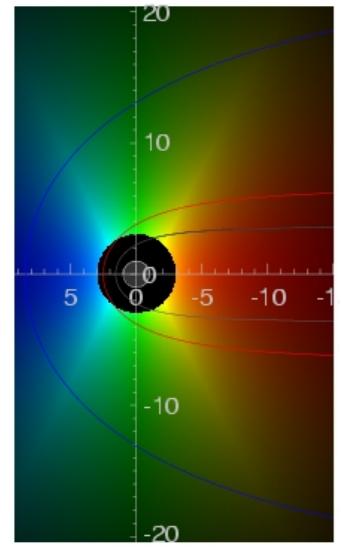
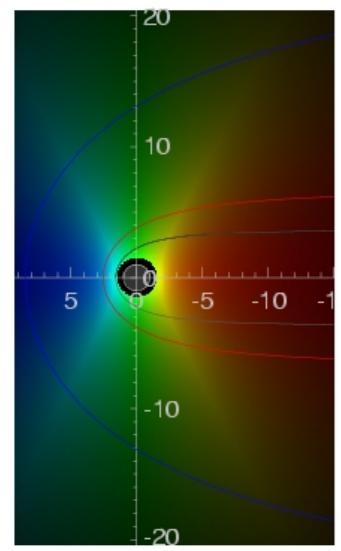


HD 155806 (Naze et al. 2010)



**Fig. 2.** The best-fit exospheric line-profile model (with the X-rays emitted above  $R_0 = 1.85 R_*$  and a wind opacity of  $\tau_{\lambda,*} = 0.0$ ) overplotted on the RGS data of the O VIII Ly $\alpha$  line (binned to get 1000 bins for the entire wavelength range).

# Line profile shapes



key parameters:  $R_o$  &  $\tau_*$

$$j \sim \rho^2 \text{ for } r/R_* > R_o, \\ = 0 \text{ otherwise}$$

$$\tau = \tau_* \int_z^\infty \frac{R_* dz'}{r'^2 (1 - R_*/r')^\beta}$$

$$\tau_* \equiv \frac{\kappa M}{4\pi R_* v_\infty}$$

# Line profile shapes: with porosity

key parameters:  $R_o$  &  $\tau_\star$

$$j \sim \rho^2 \text{ for } r/R_* > R_o, \\ = 0 \text{ otherwise}$$

simply replace  $\kappa$  with

$$\kappa_{\text{eff}} \propto \kappa/(1+h)$$

$$\tau = \tau_* \int_z^\infty \frac{R_* dz'}{r'^2 (1 - R_*/r')^\beta}$$

$$\tau_* \equiv \frac{\kappa M}{4\pi R_* v_\infty}$$

remember: clumping does not affect X-ray  
line shapes; only porosity does

# Line profiles with porosity

$h = 0 R_\star$

$h$  has to be big for porosity to have an effect

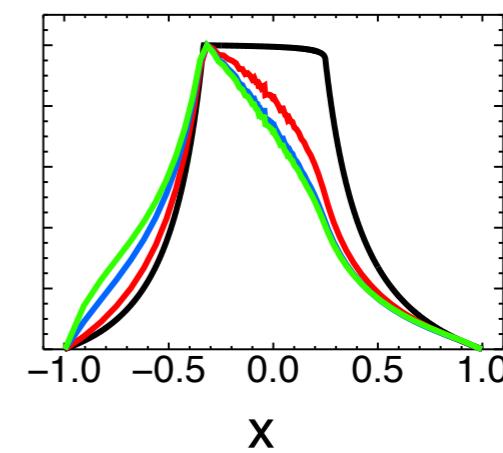
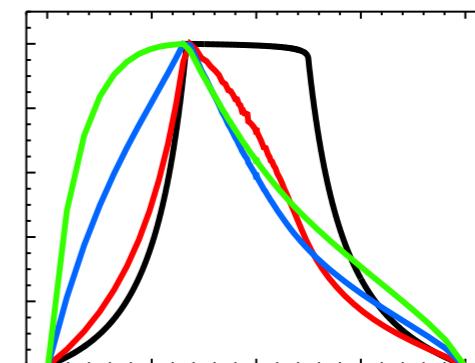
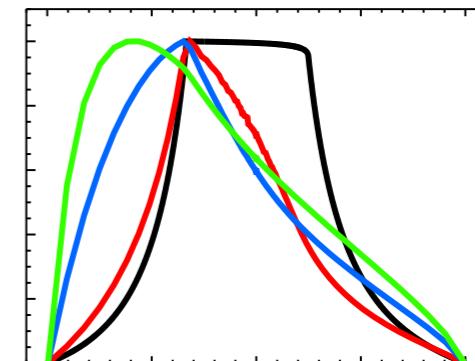
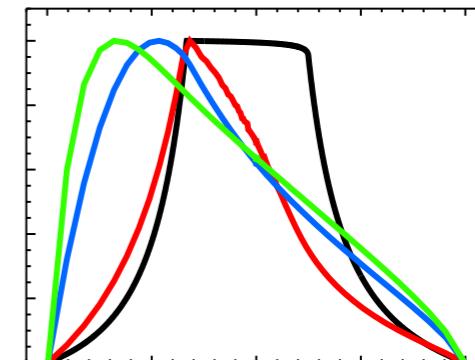
porosity makes lines more symmetric, mimicking lower optical depths

$h = 0.5 R_\star$

$h = 1 R_\star$

$h = 5 R_\star$

$$\chi_{\text{eff}}/\langle \chi \rangle = 1/(1+\tau)$$



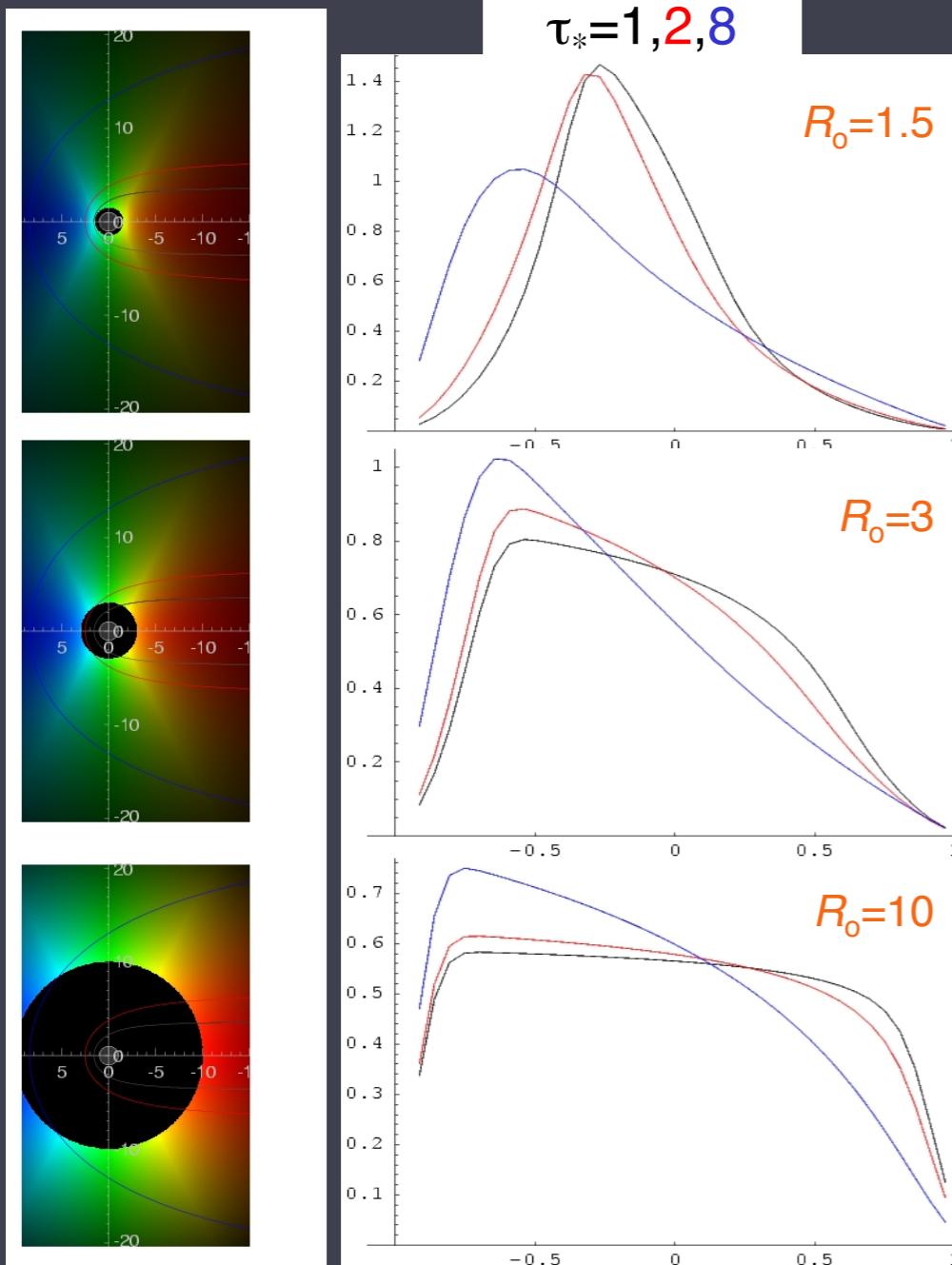
# Testing models of clumping and porosity with data

...or, measuring  $f_{\text{cl}}$  and  $h$

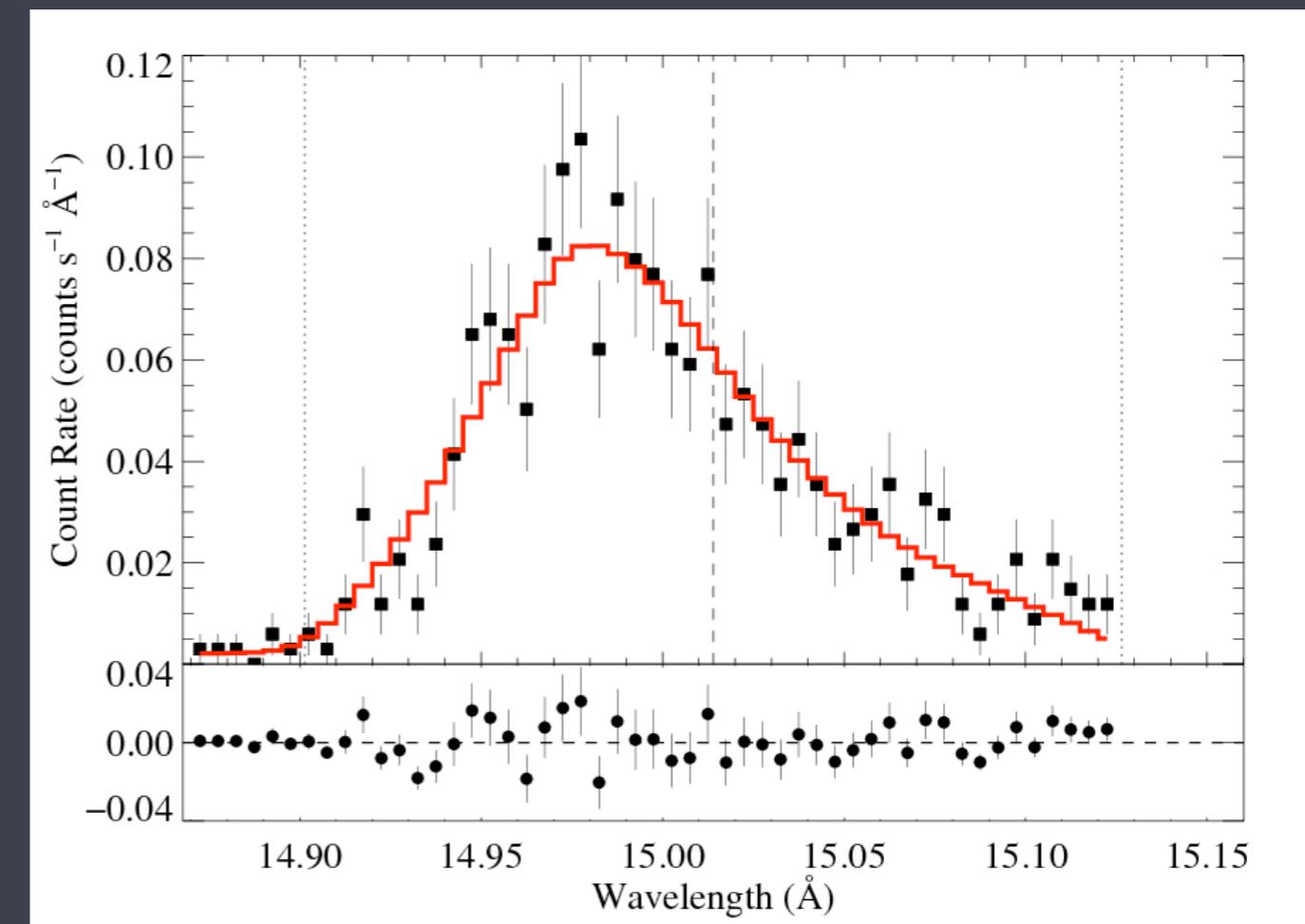
Measuring  $\tau_*$  along with  $h$  gives the mass-loss rate, but the two parameters are degenerate

H $\alpha$ , IR & radio free-free, measures  $\dot{M}f_{\text{cl}}^{0.5}$ .

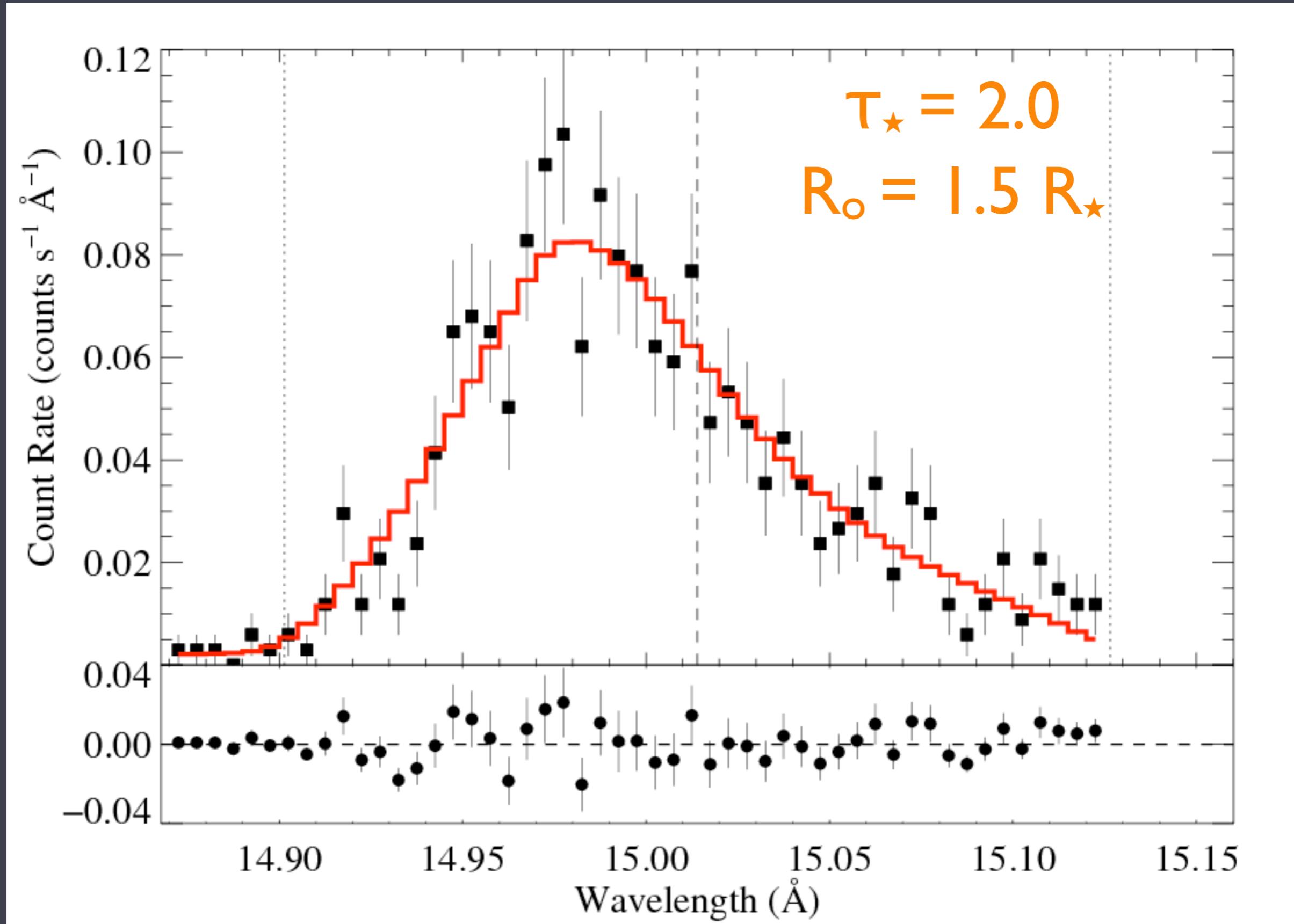
# Testing models of clumping and porosity with data



$\zeta$  Pup: Chandra MEG



# $\zeta$ Pup: Chandra MEG



What about with porosity?

Use a model of a radially varying porosity length

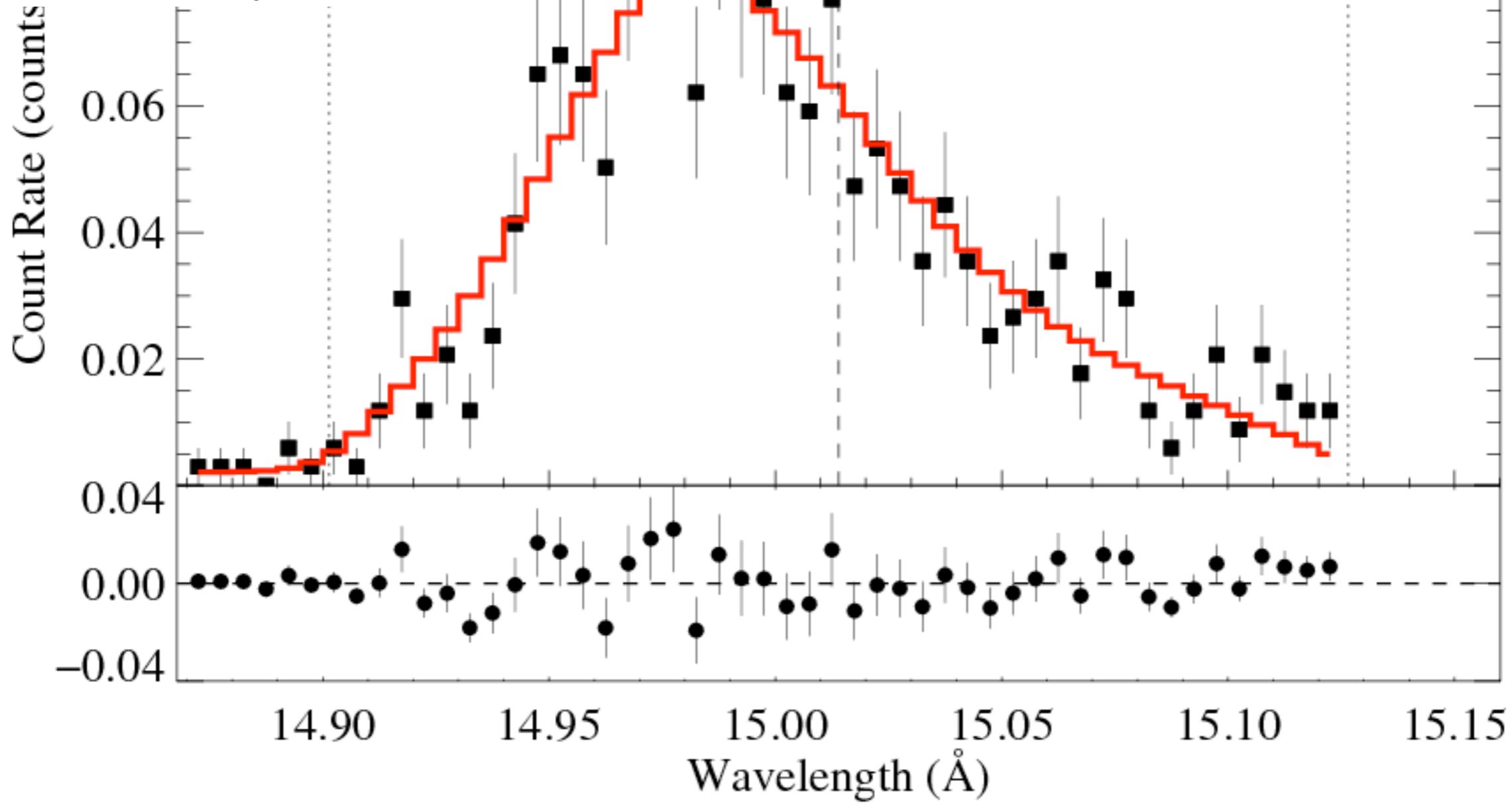
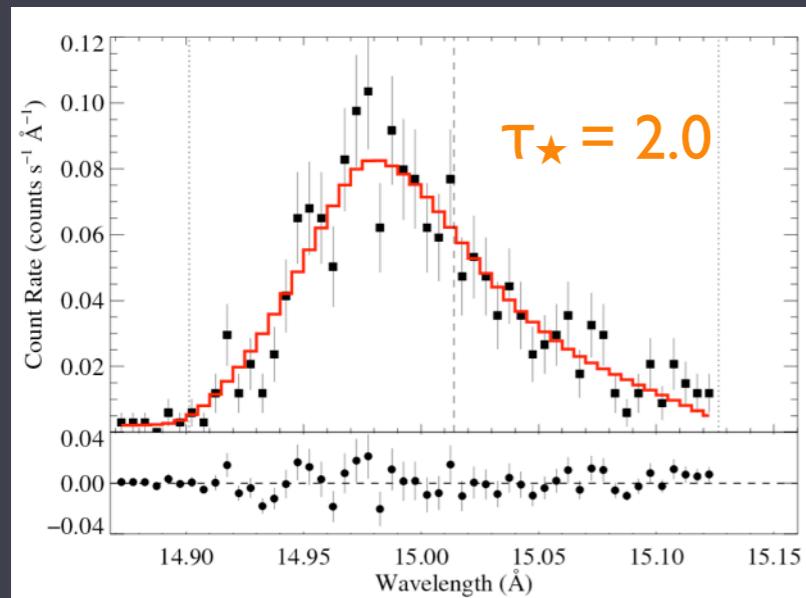
$$h(r) = h_\infty(1 - R_\star/r)^\beta$$

note the resemblance:

$$v(r) = v_\infty(1 - R_\star/r)^\beta$$

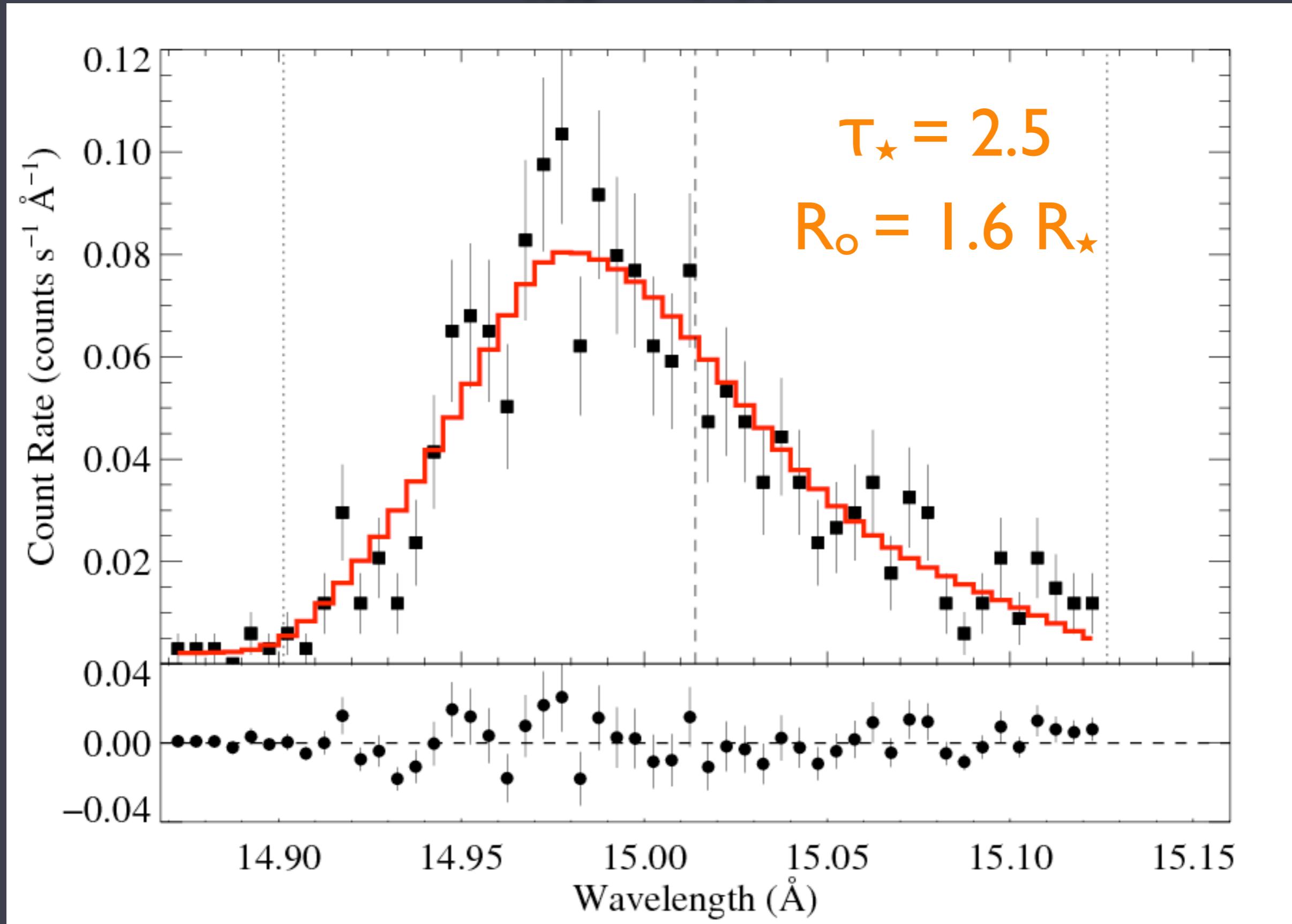
# $\zeta$ Pup: Chandra MEG

$h_\infty = 0.5 R_\star$

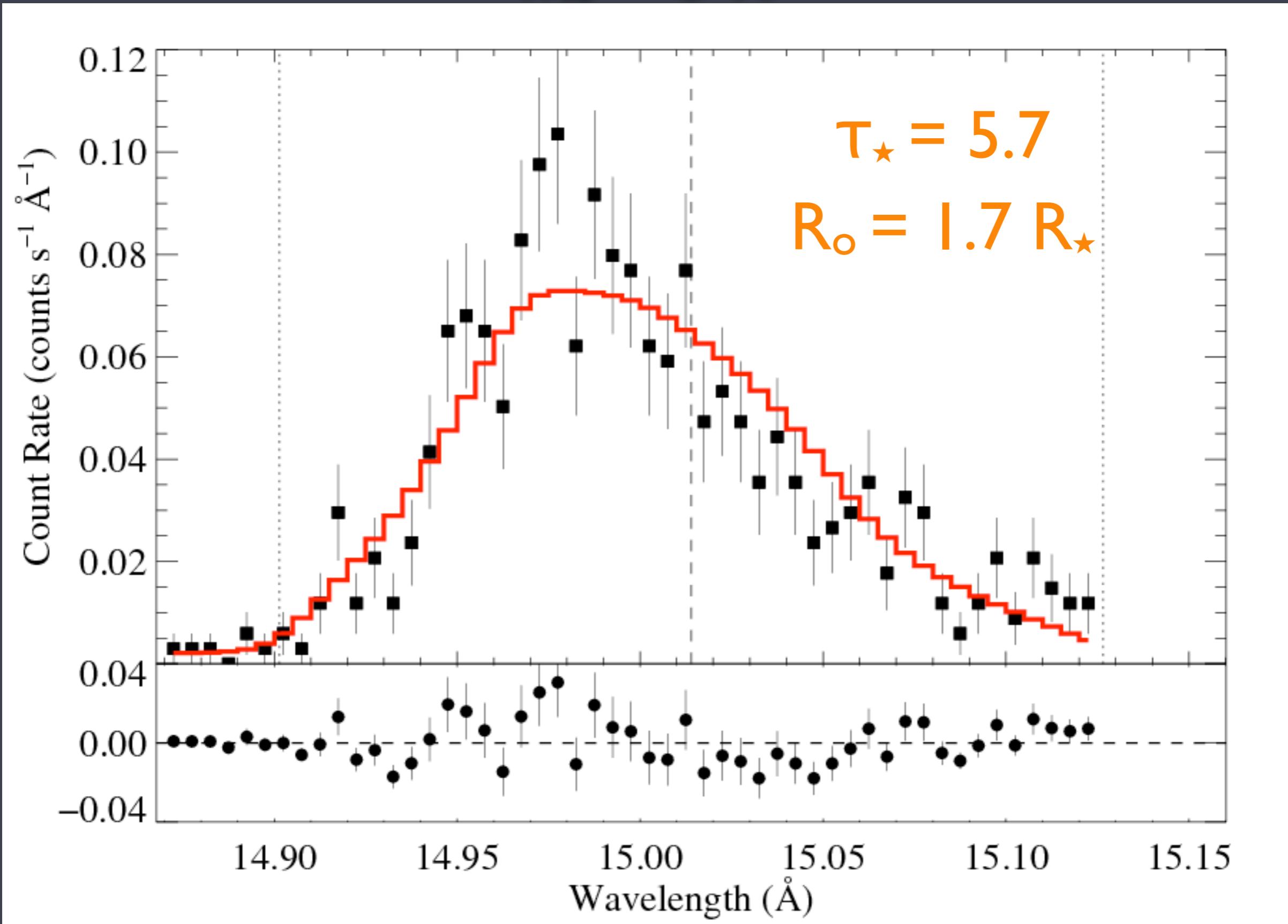


# $\zeta$ Pup: Chandra MEG

$$h_\infty = |R_\star|$$

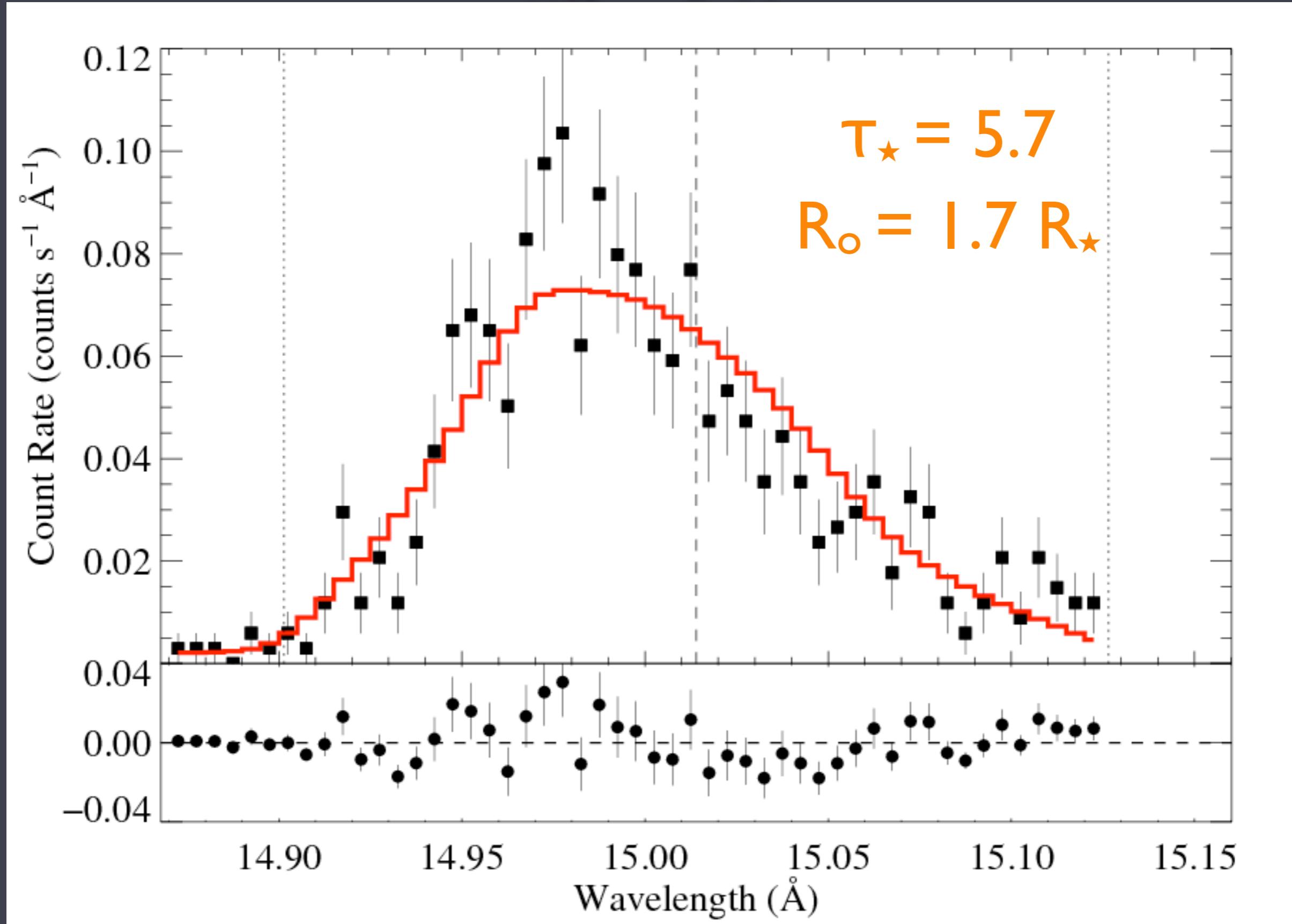


# $\zeta$ Pup: Chandra MEG

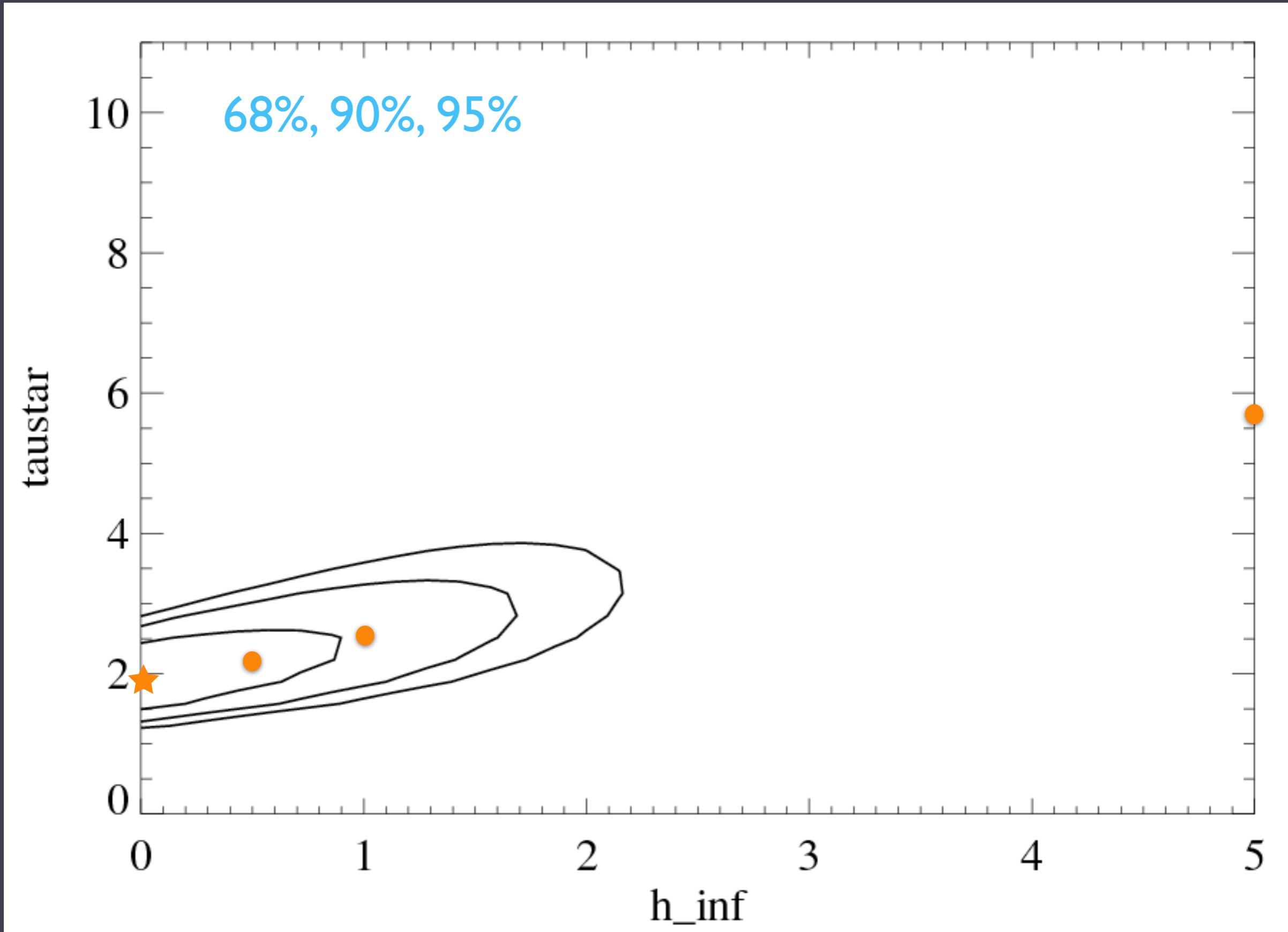
 $h_\infty = 5 R_\star$ 

poor fit ( $P > 99.9\%$ ) and large  $\tau_\star$

$h_\infty = 5 R_\star$

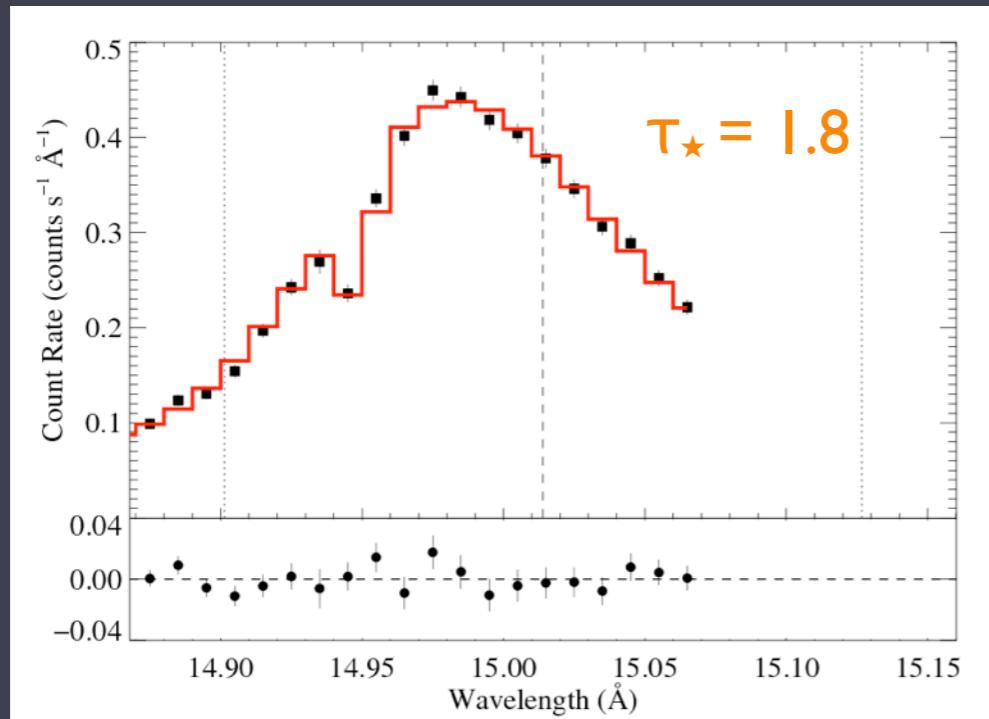


# Confidence limits on $h_\infty$ and $\tau_*$

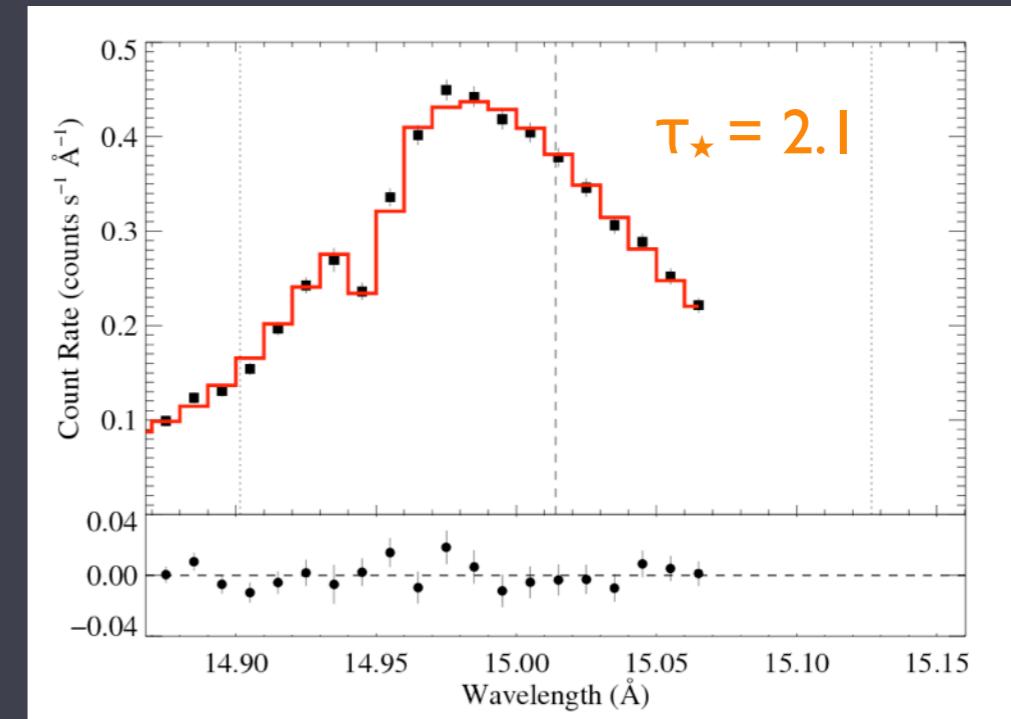


# XMM RGS spectrum

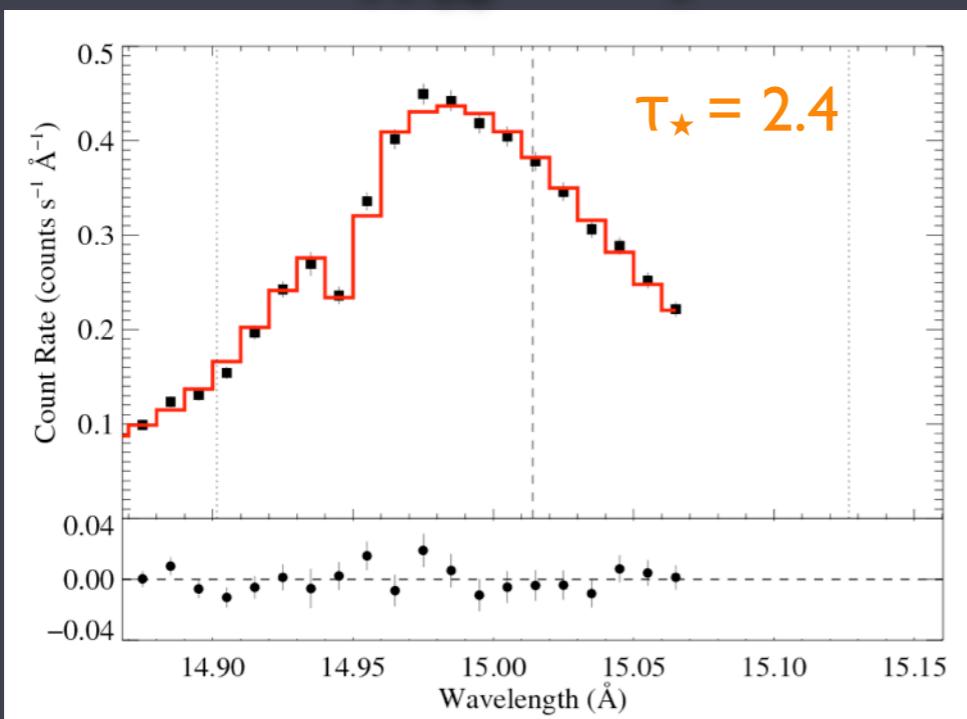
$h_\infty = 0$



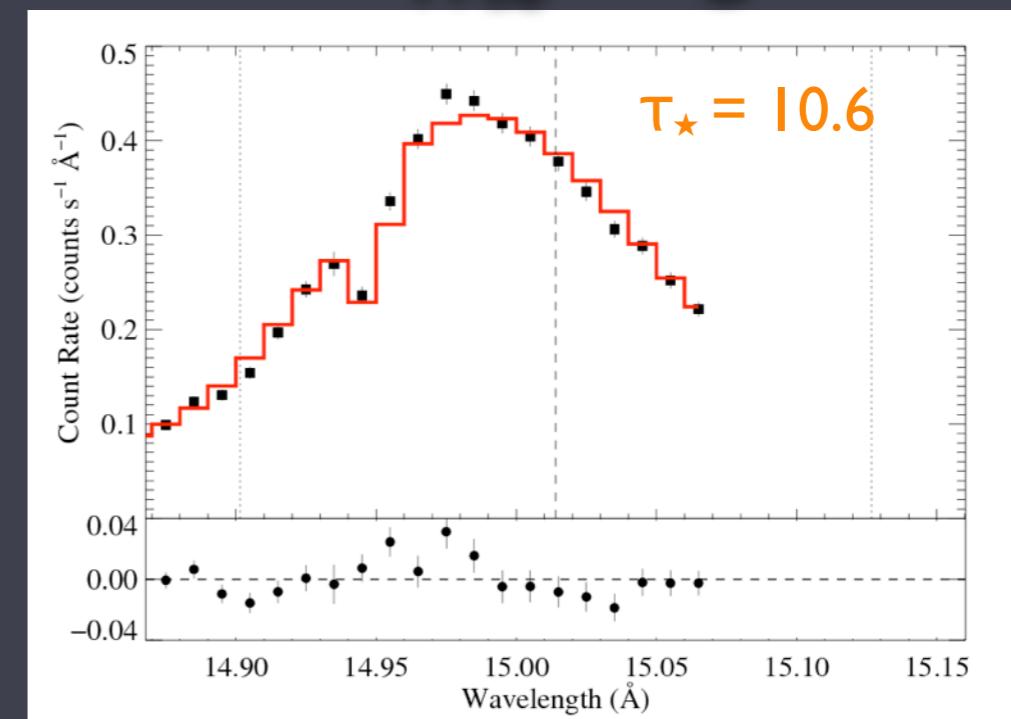
$h_\infty = 0.5$



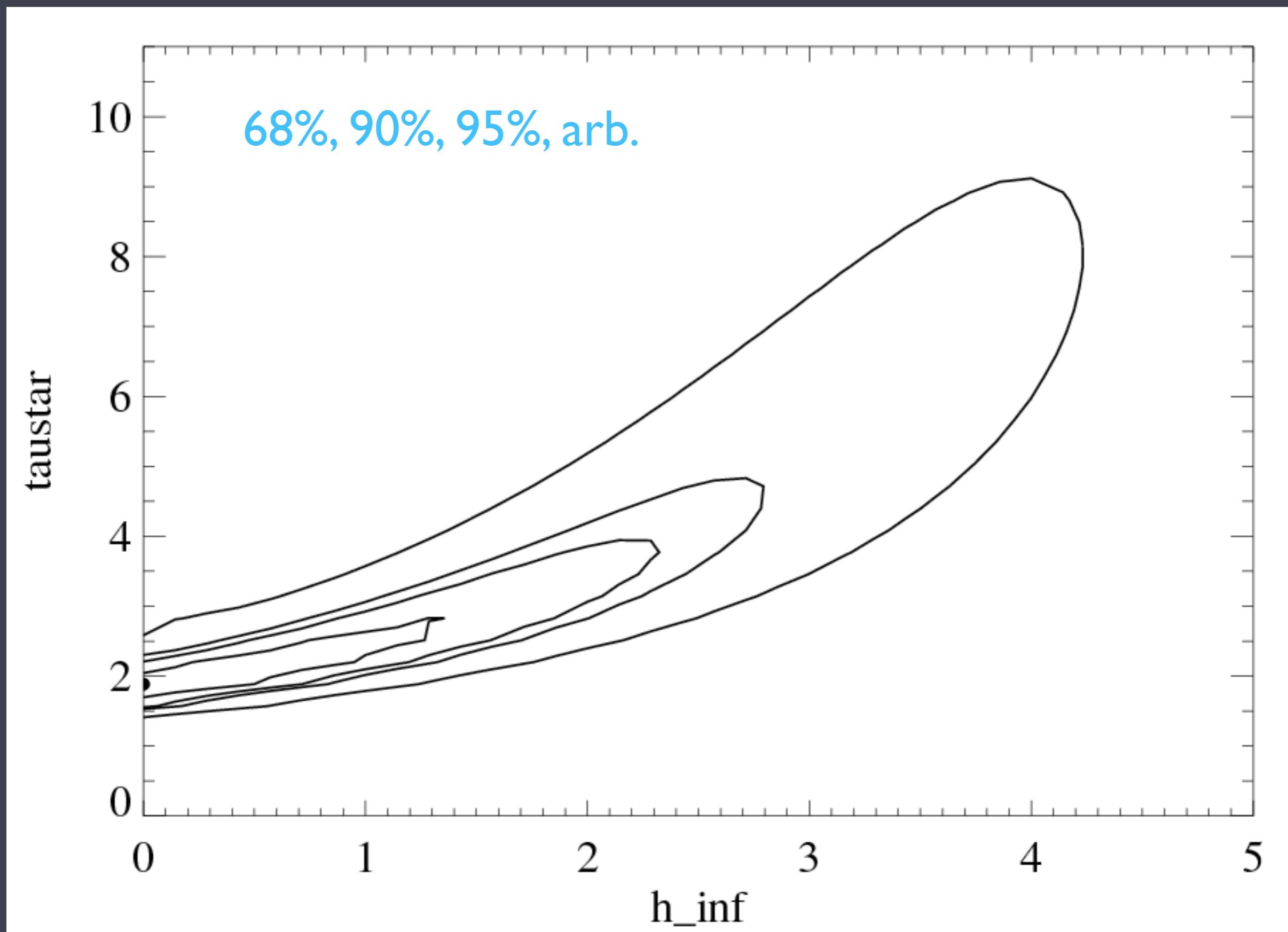
$h_\infty = 1$



$h_\infty = 5$



# RGS Confidence limits on $h_\infty$ and $\tau_\star$

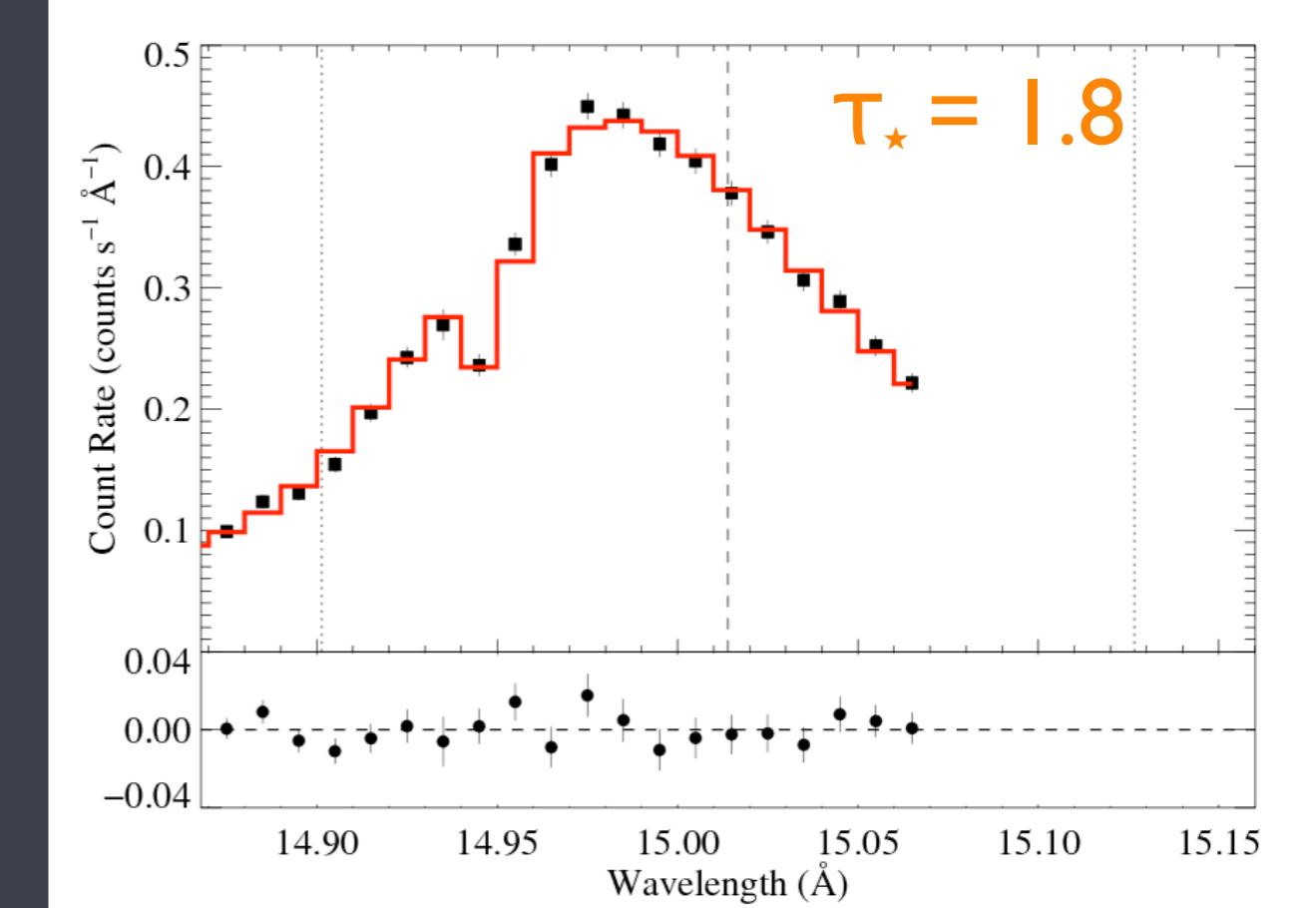
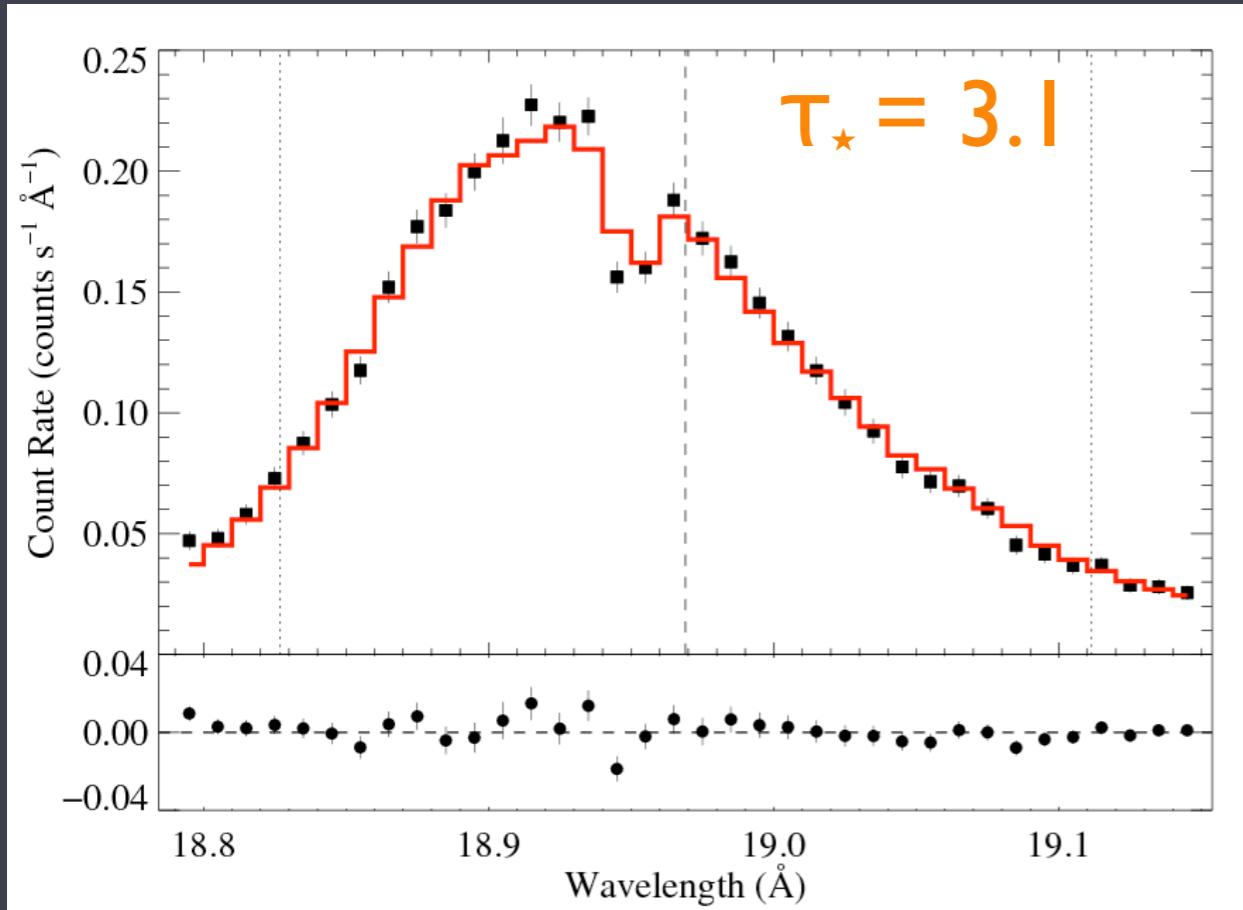


# What about other spectral lines?

O VIII Ly $\alpha$  18.969 Å

$$h_\infty = 0 \quad h_\infty = 0$$

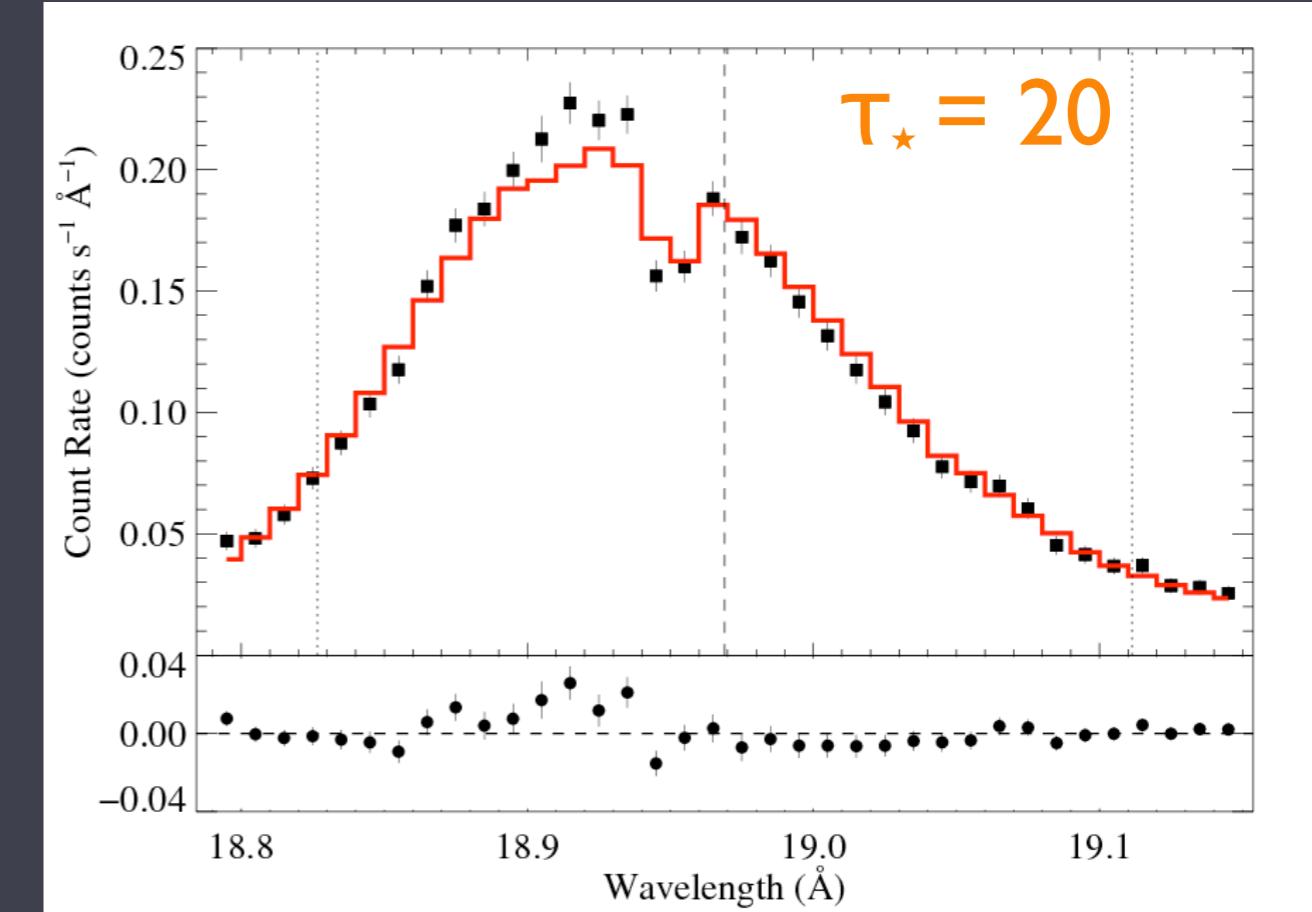
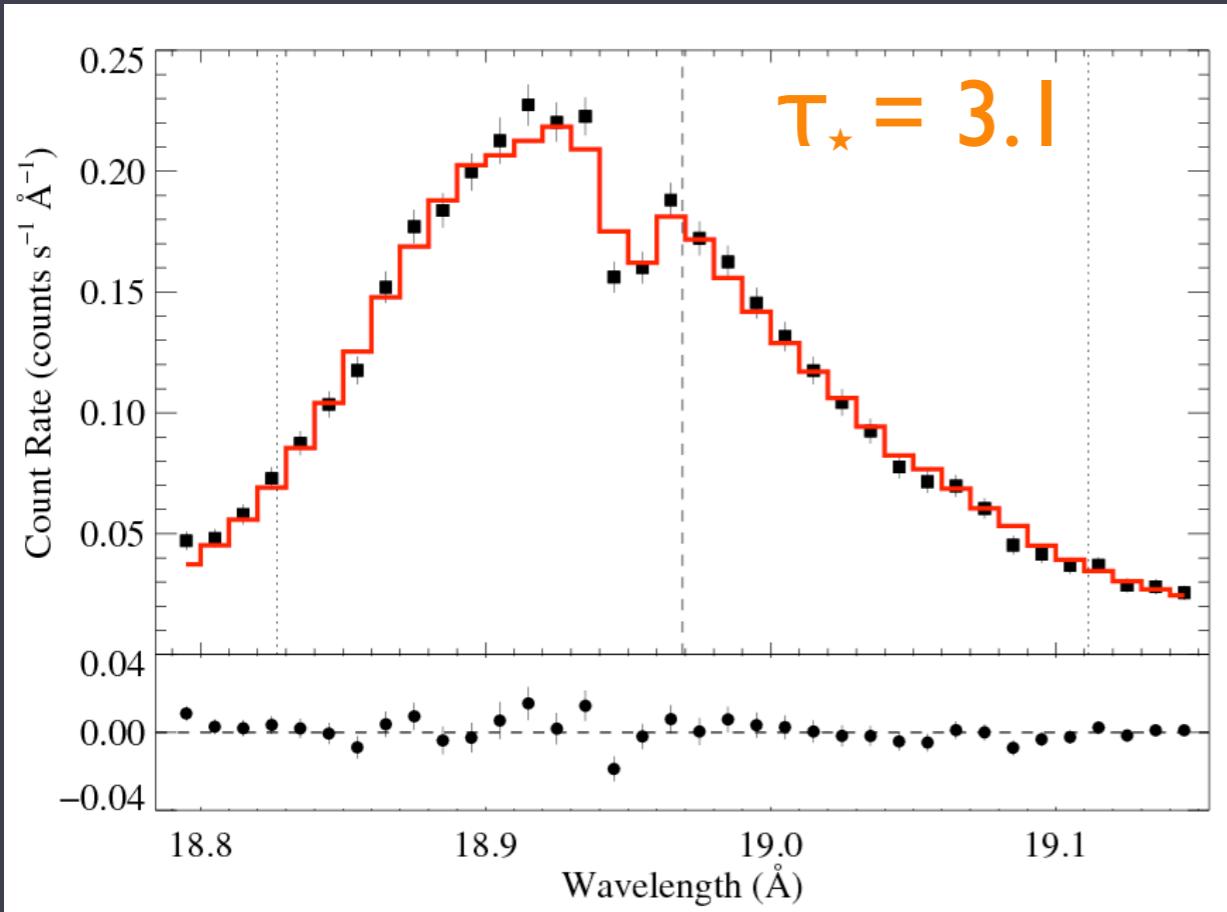
Fe XVII 15.014 Å



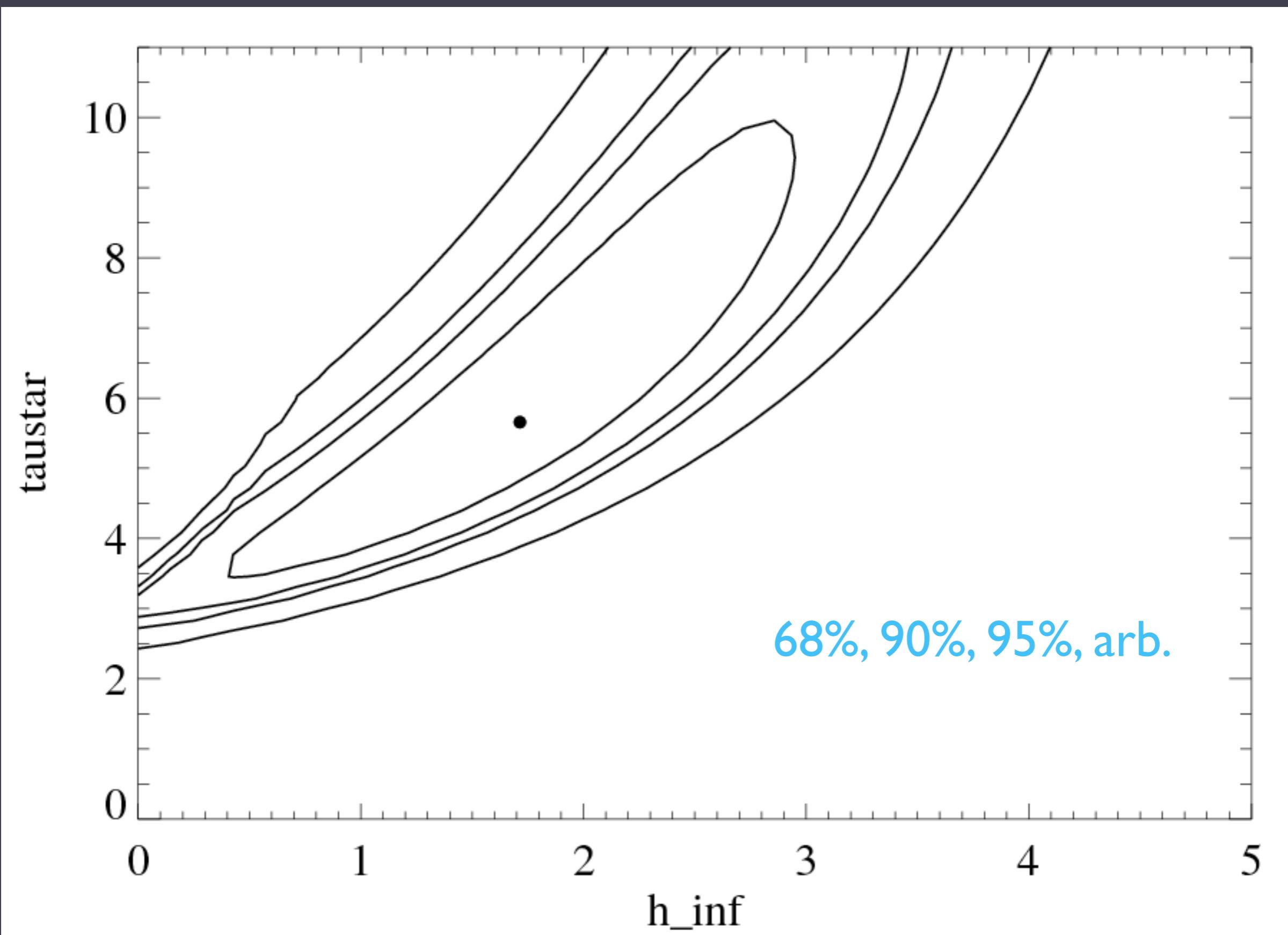
# What about other spectral lines?

O VIII Ly $\alpha$  18.969 Å

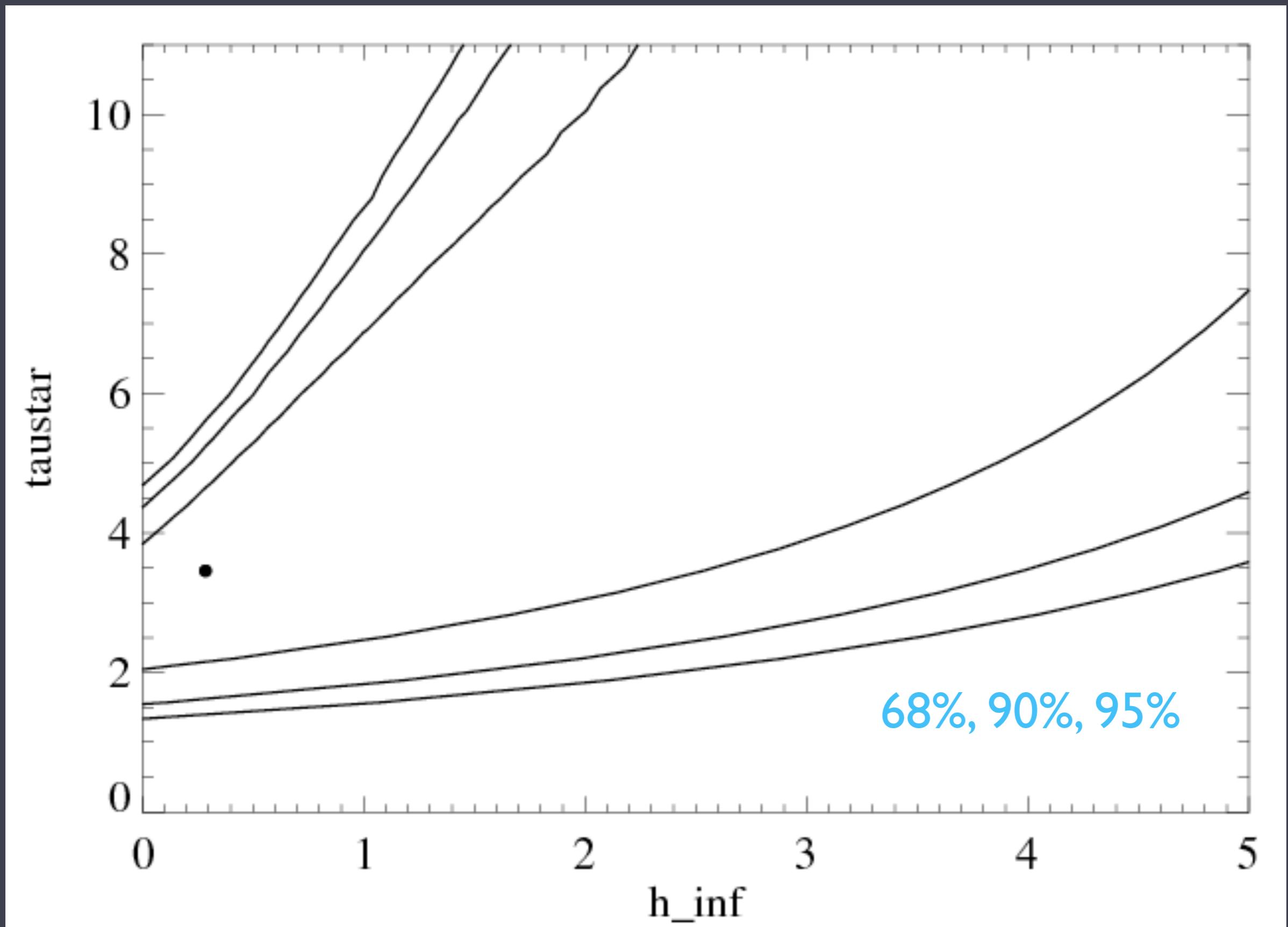
$$h_\infty = 0 \quad h_\infty = 5$$



# RGS: Confidence limits on $h_\infty$ and $\tau_\star$



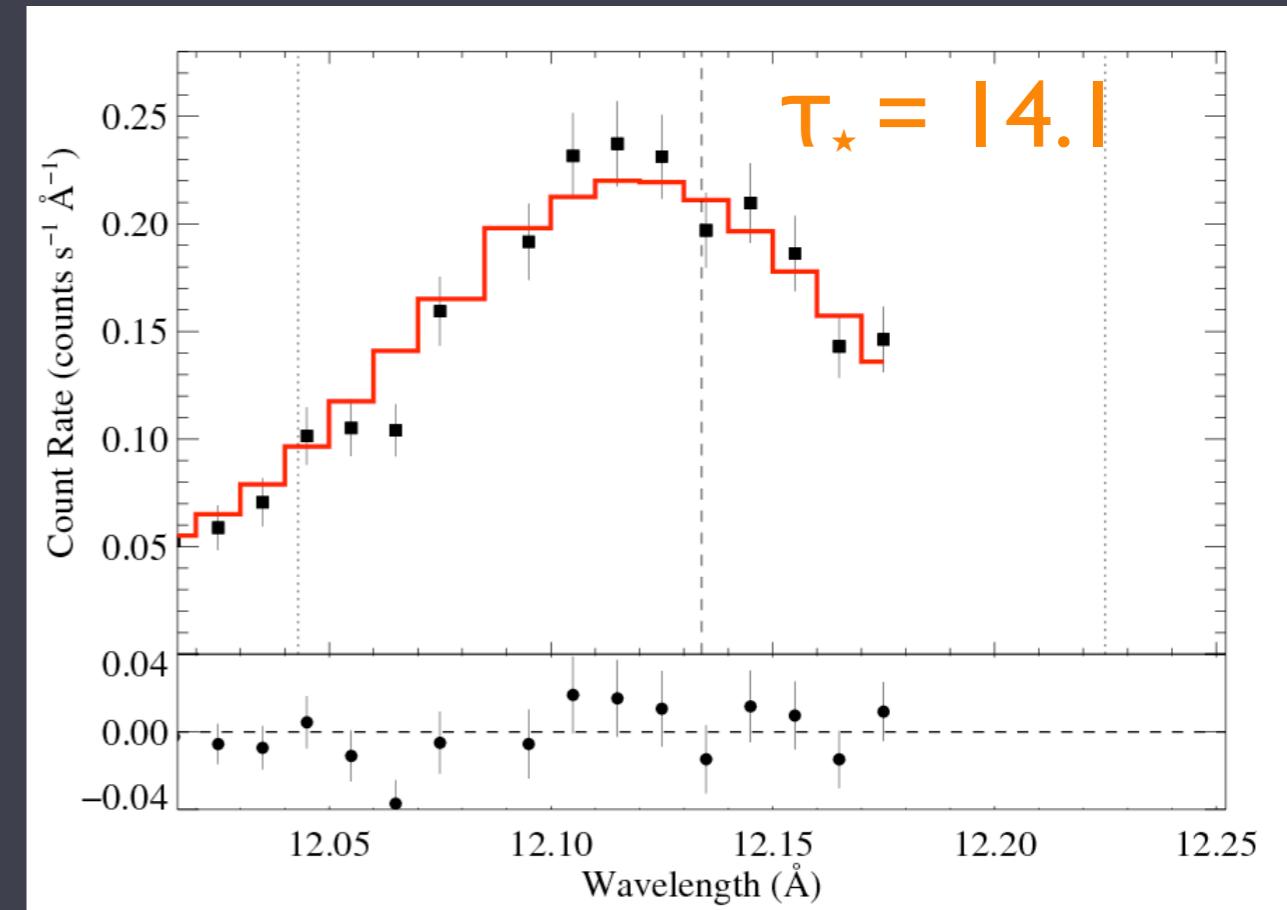
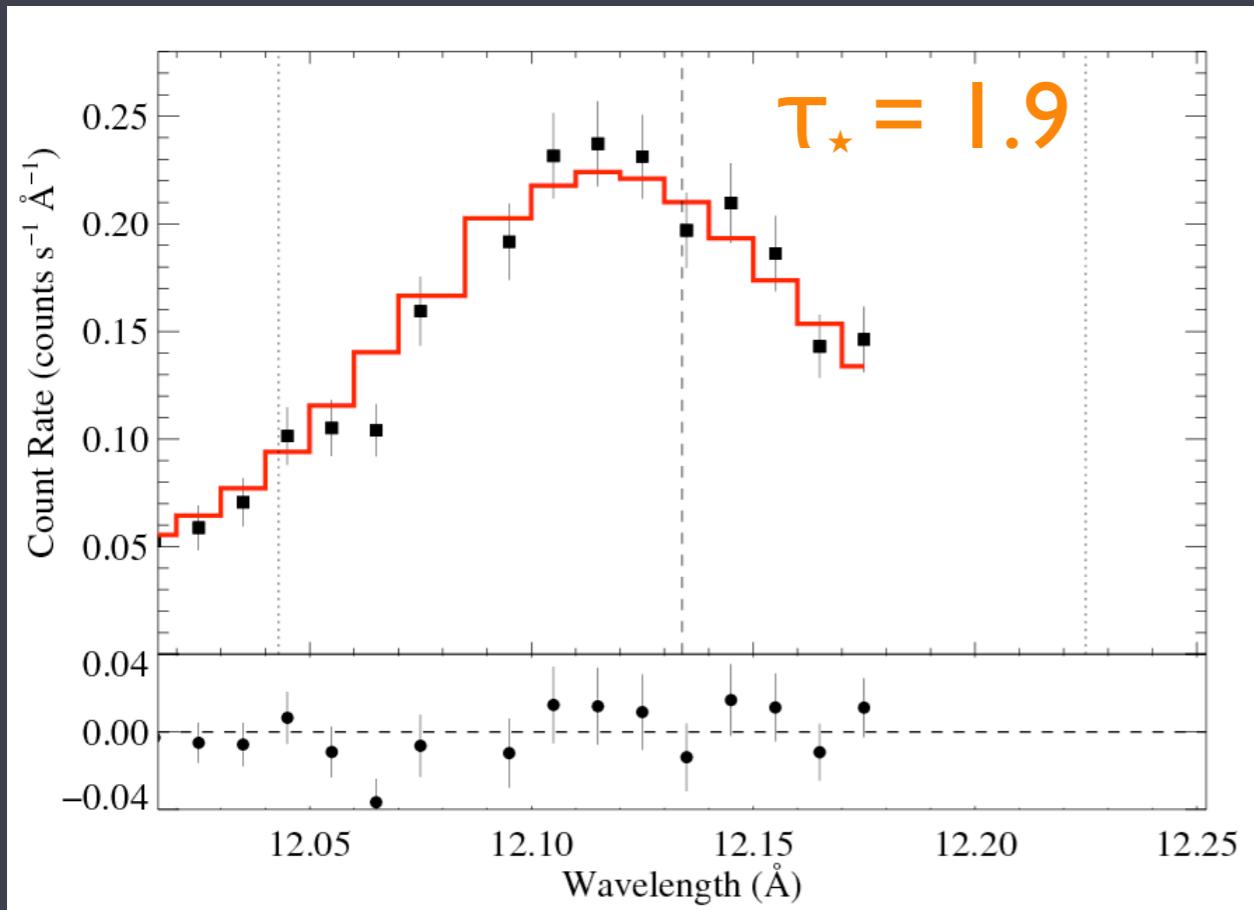
# Chandra: Confidence limits on $h_\infty$ and $\tau_*$



# What about other spectral lines?

Ne X Ly $\alpha$  12.134 Å : XMM RGS

$$h_\infty = 0 \quad h_\infty = 5$$



lower S/N, high porosity fit is only moderately disfavored

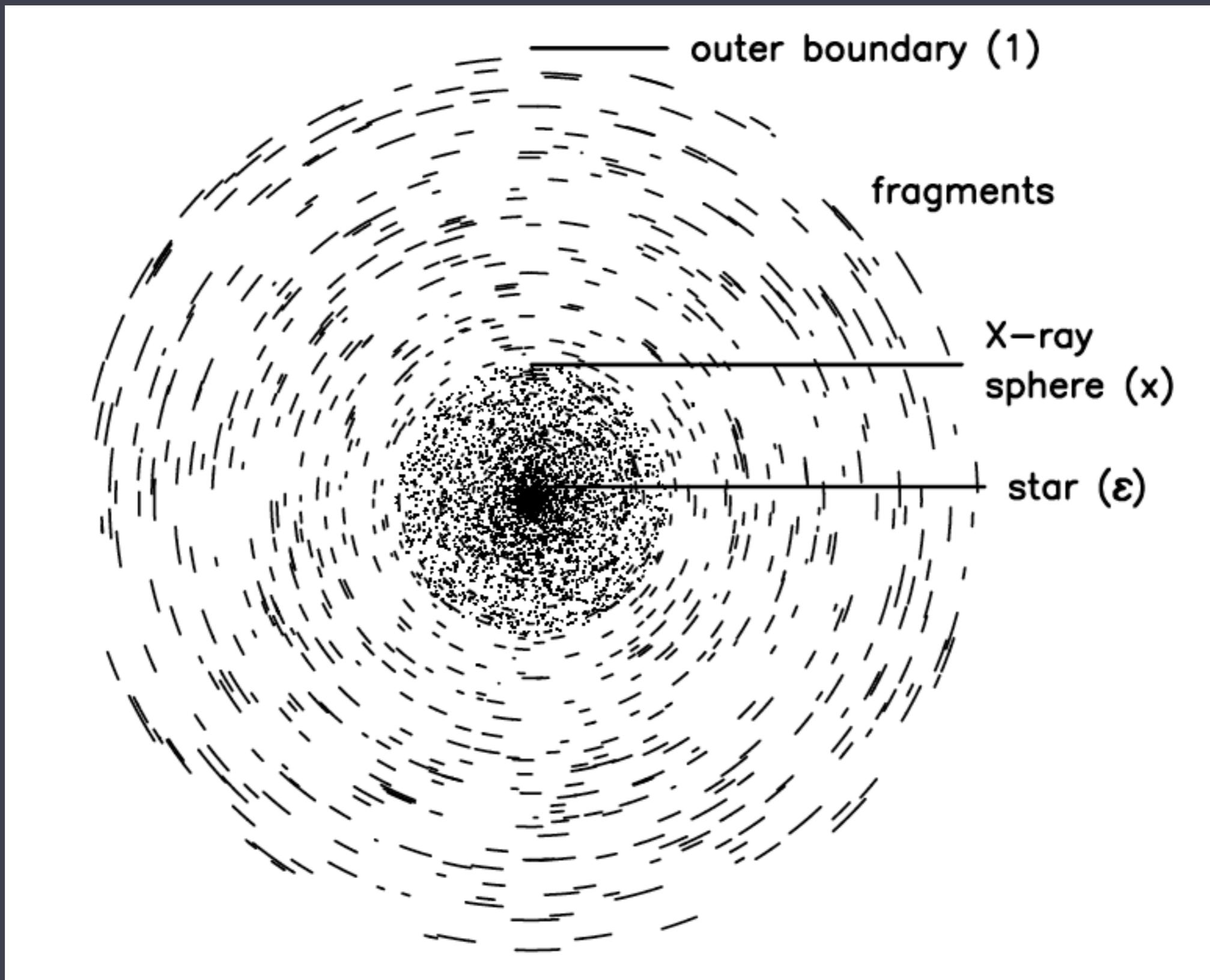
# Conclusion I

High porosity can be rejected

## Conclusion 2

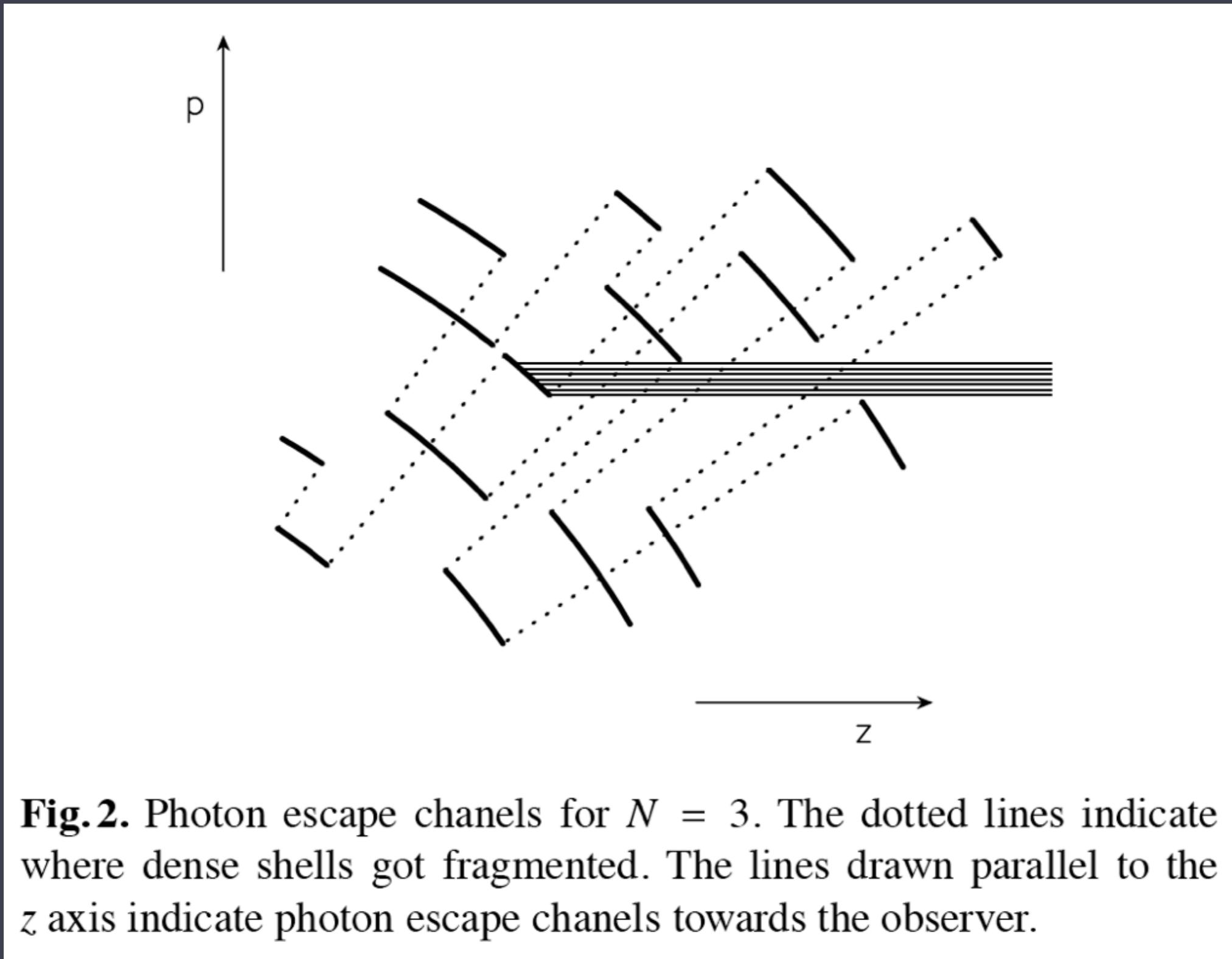
Moderate porosity ( $h_\infty \leq l$ ) increases  $T_*$   
by only 20% to 30%

# What about non-spherical clumps?

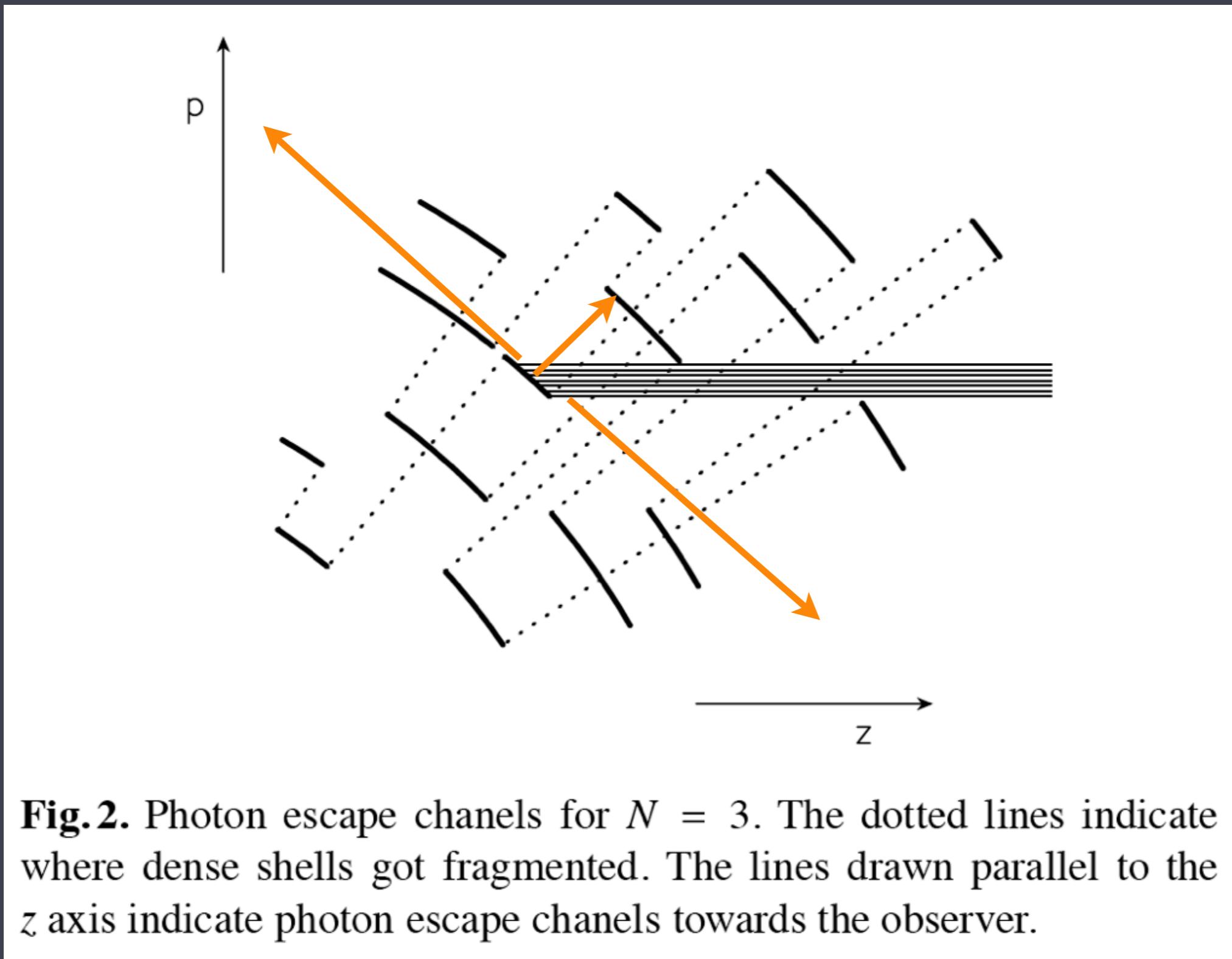


Feldmeier, Oskinova, & Hamann 2003

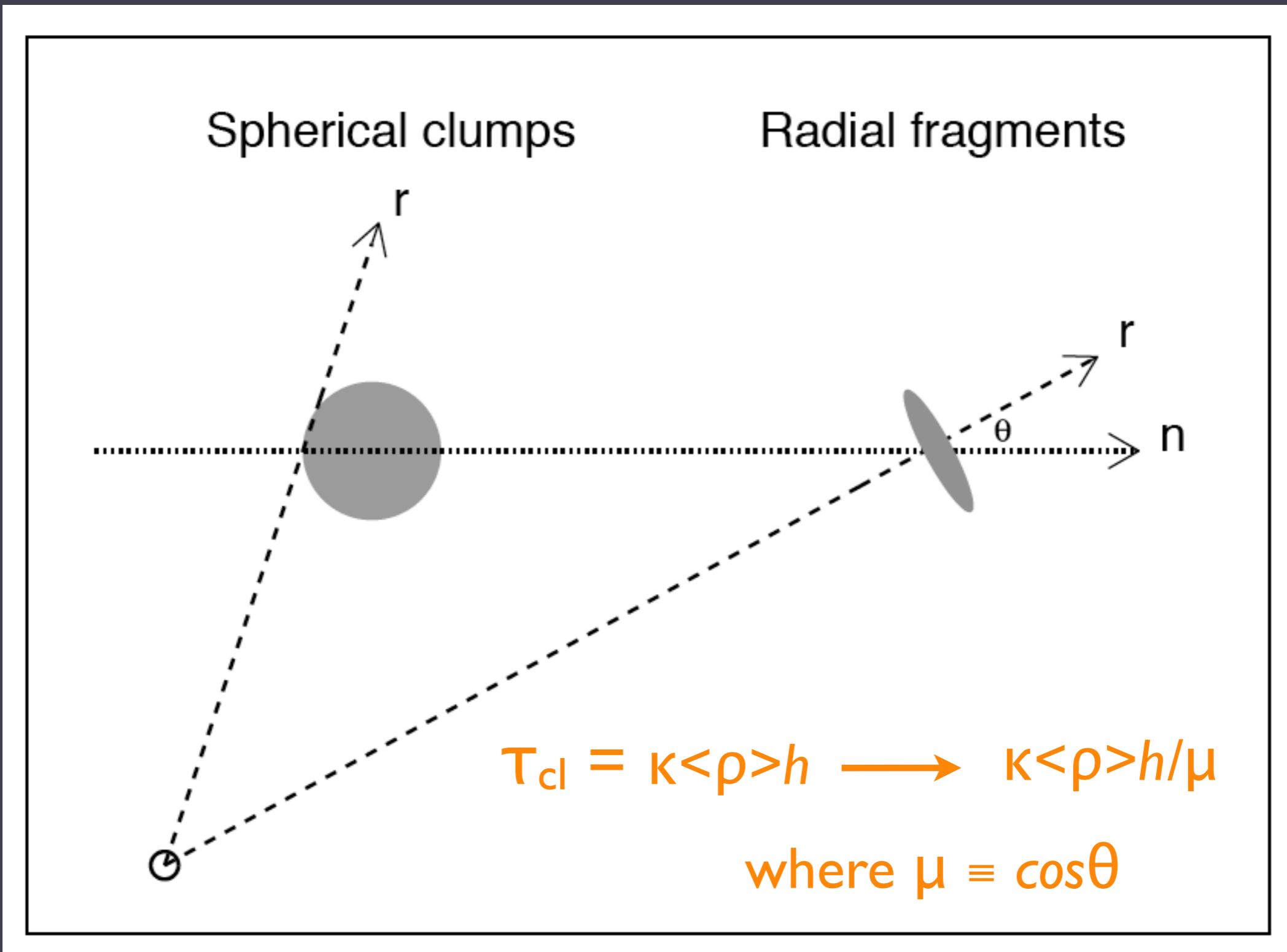
# Flattened clumps (pancakes - shell fragments)



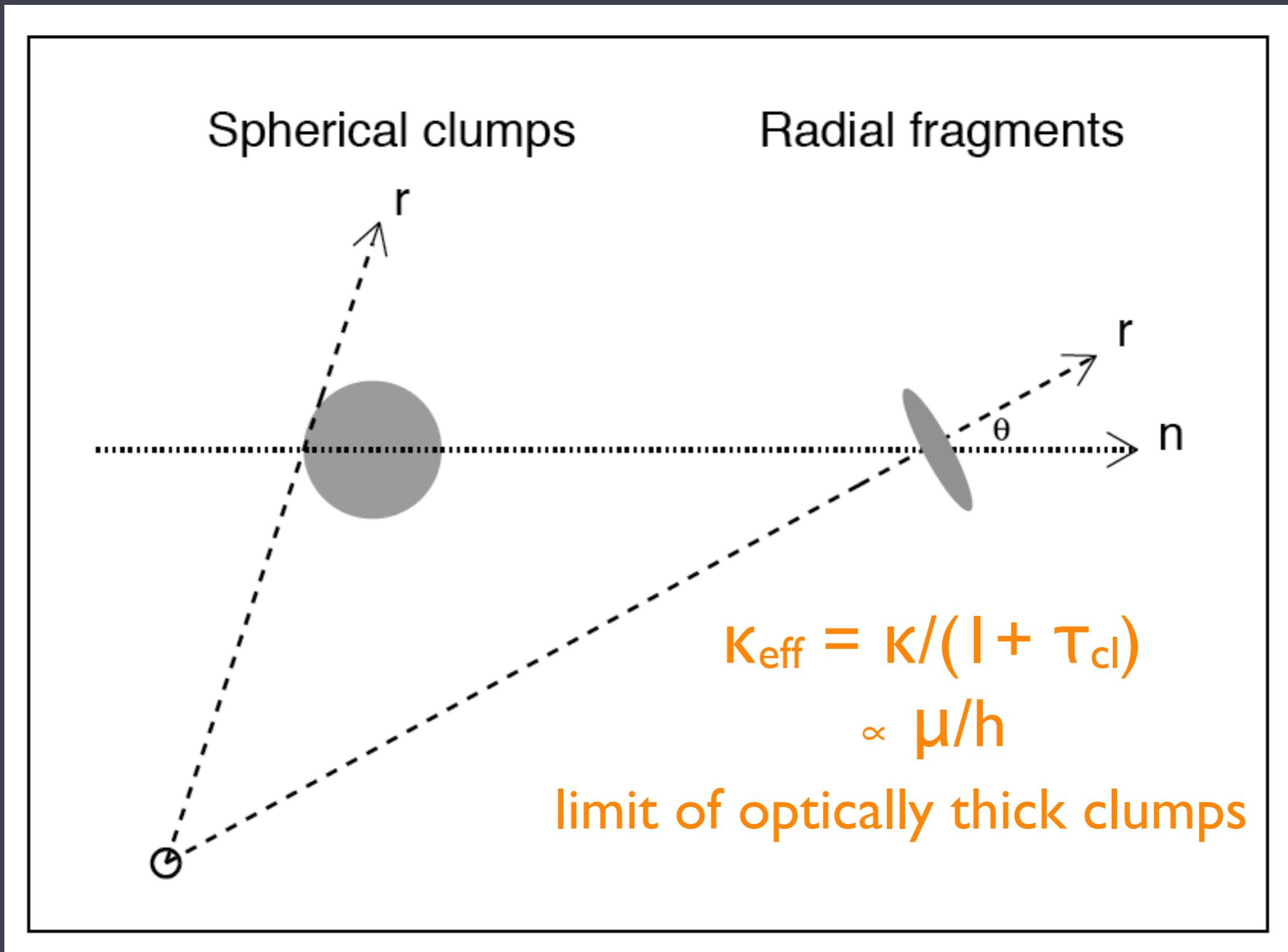
# Flattened clumps: lateral escape is enhanced



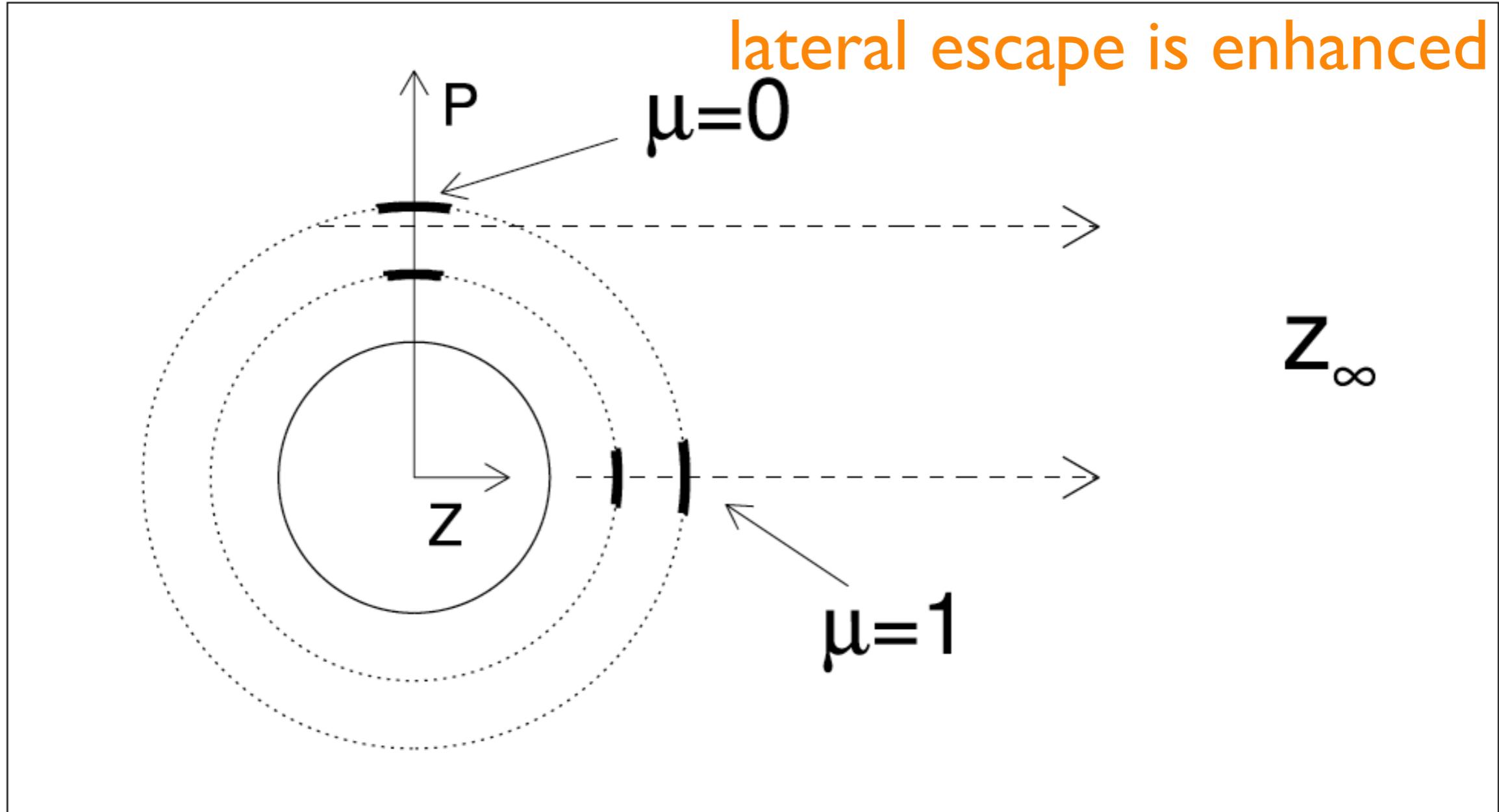
# Radial fragments = *anisotropic porosity*



# Radial fragments = *anisotropic porosity*



# The Venetian blind effect



**Figure 4.** Illustration of the ‘venetian blind’ effect seen in porosity models using an anisotropic effective opacity. The dashed arrowed lines represent two different  $p$ -rays and the observer is assumed to be located at  $z_\infty$ .

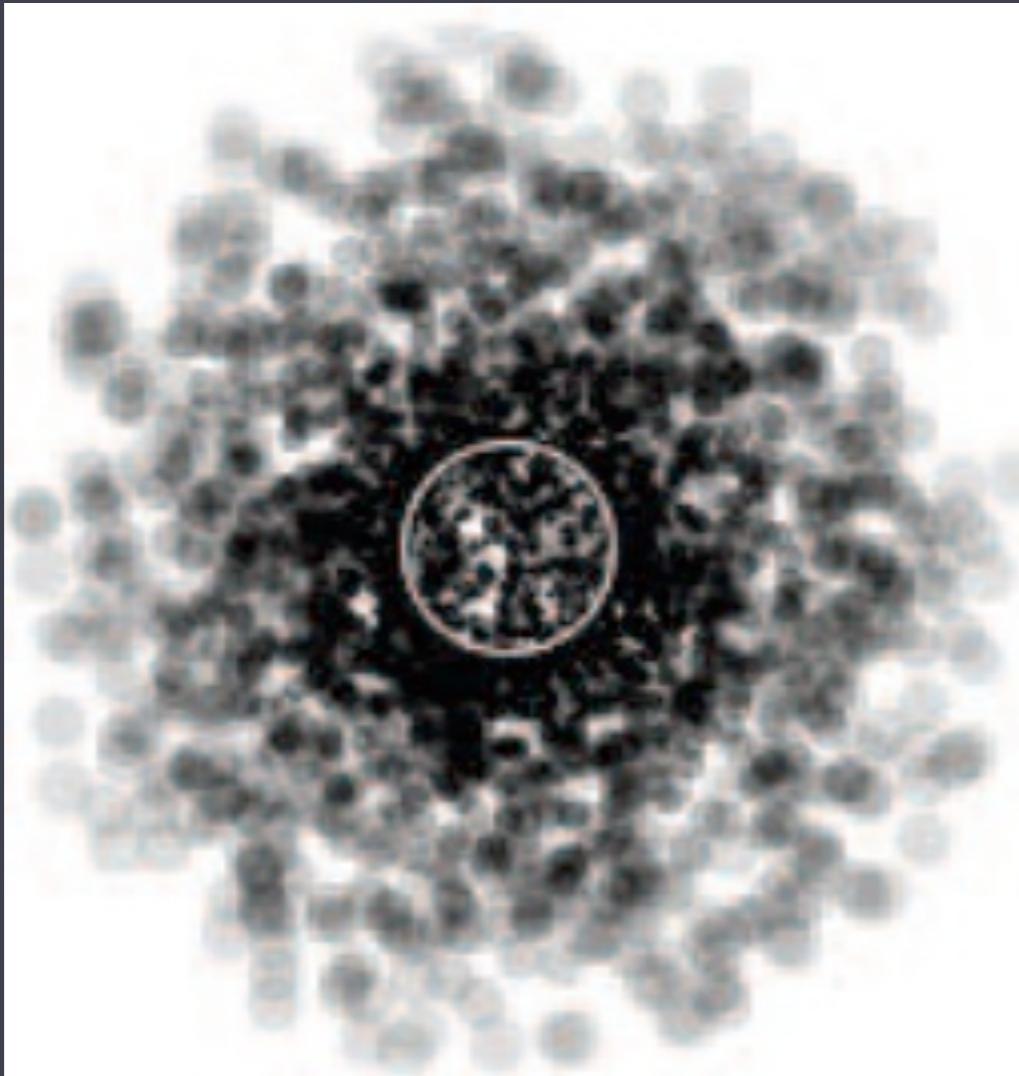
# Visualizations of porous wind models

all clumps have  $\ell = 0.1r$

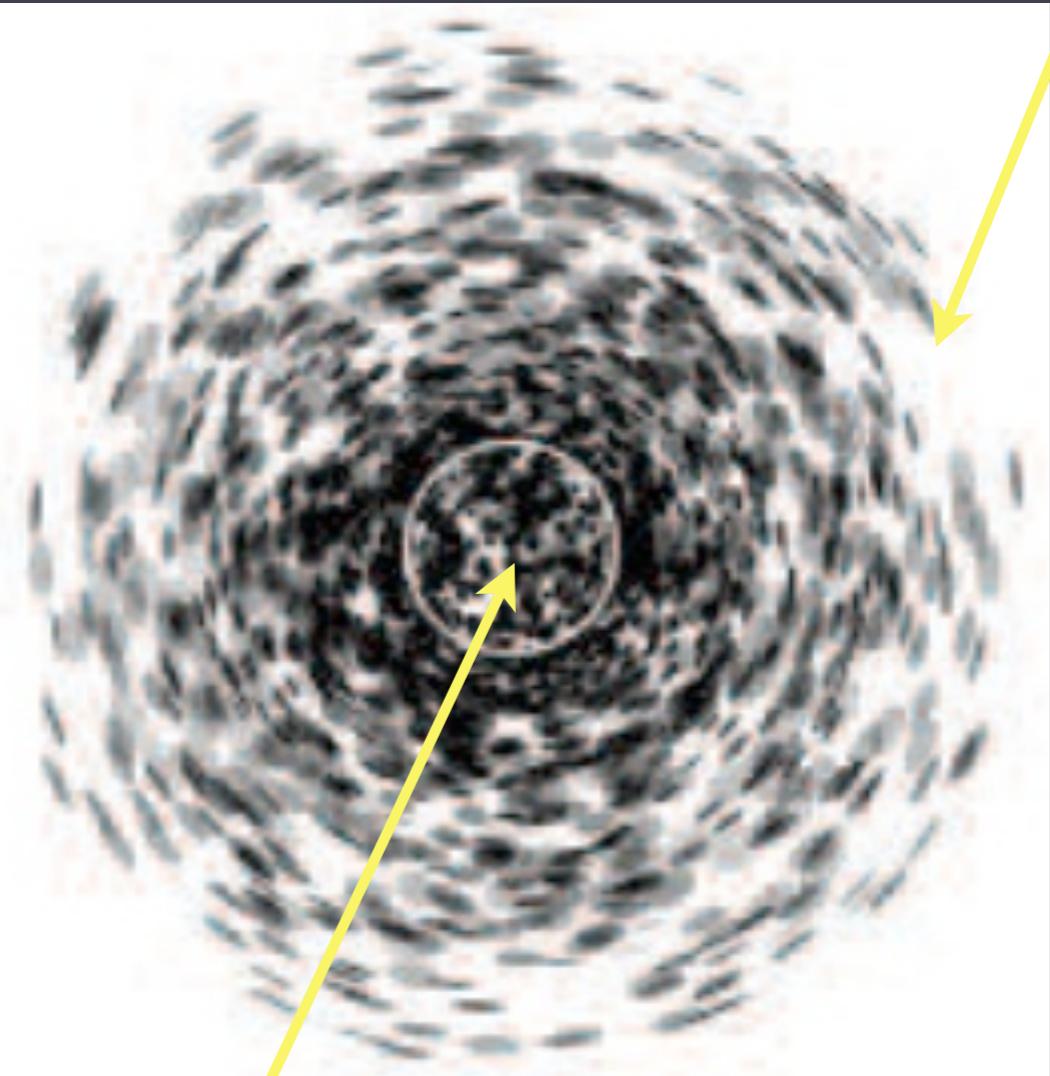
$h_\infty = 4$

open Venetian  
blinds

isotropic porosity



anisotropic porosity



closed Venetian blinds

# Visualizations of porous wind models

all clumps have  $\ell = 0.1r$

isotropic porosity

$h_\infty = 0$

$h_\infty = 0.25$

$h_\infty = 0.5$

$h_\infty = 1$

$h_\infty = 2$

$h_\infty = 4$

$h_\infty = 8$

{0, 0, 1}

{0.1, 0.25, 41881}

{0.1, 0.5, 20940}

{0.1, 1., 10470}

{0.1, 2., 5235}

{0.1, 4., 2617}

{0.1, 8., 1308}

{0, 0, 1}

{0.1, 0.25, 41881}

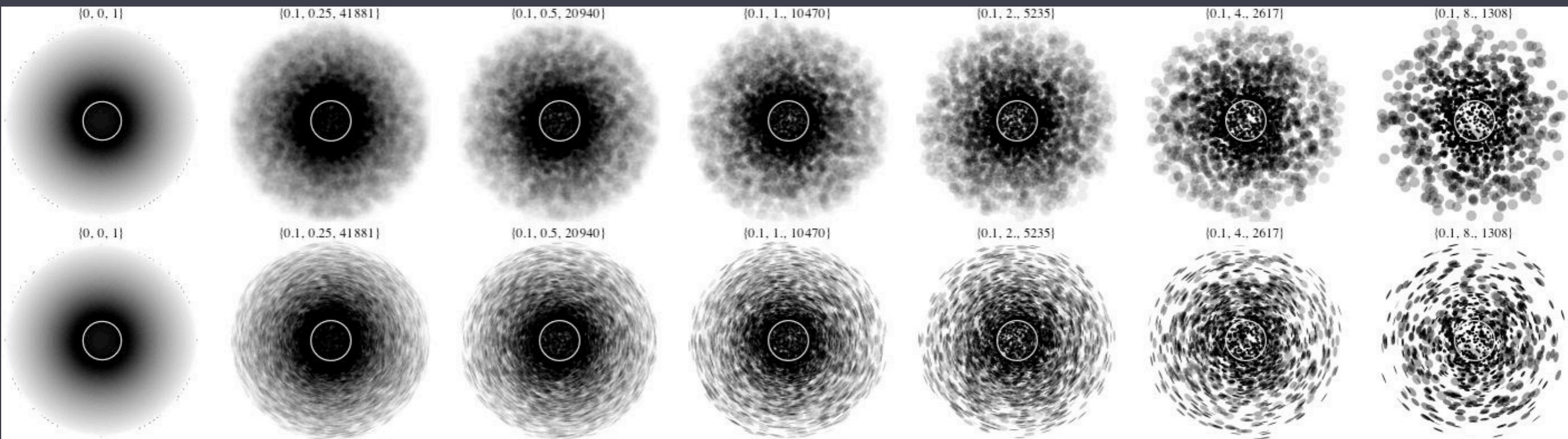
{0.1, 0.5, 20940}

{0.1, 1., 10470}

{0.1, 2., 5235}

{0.1, 4., 2617}

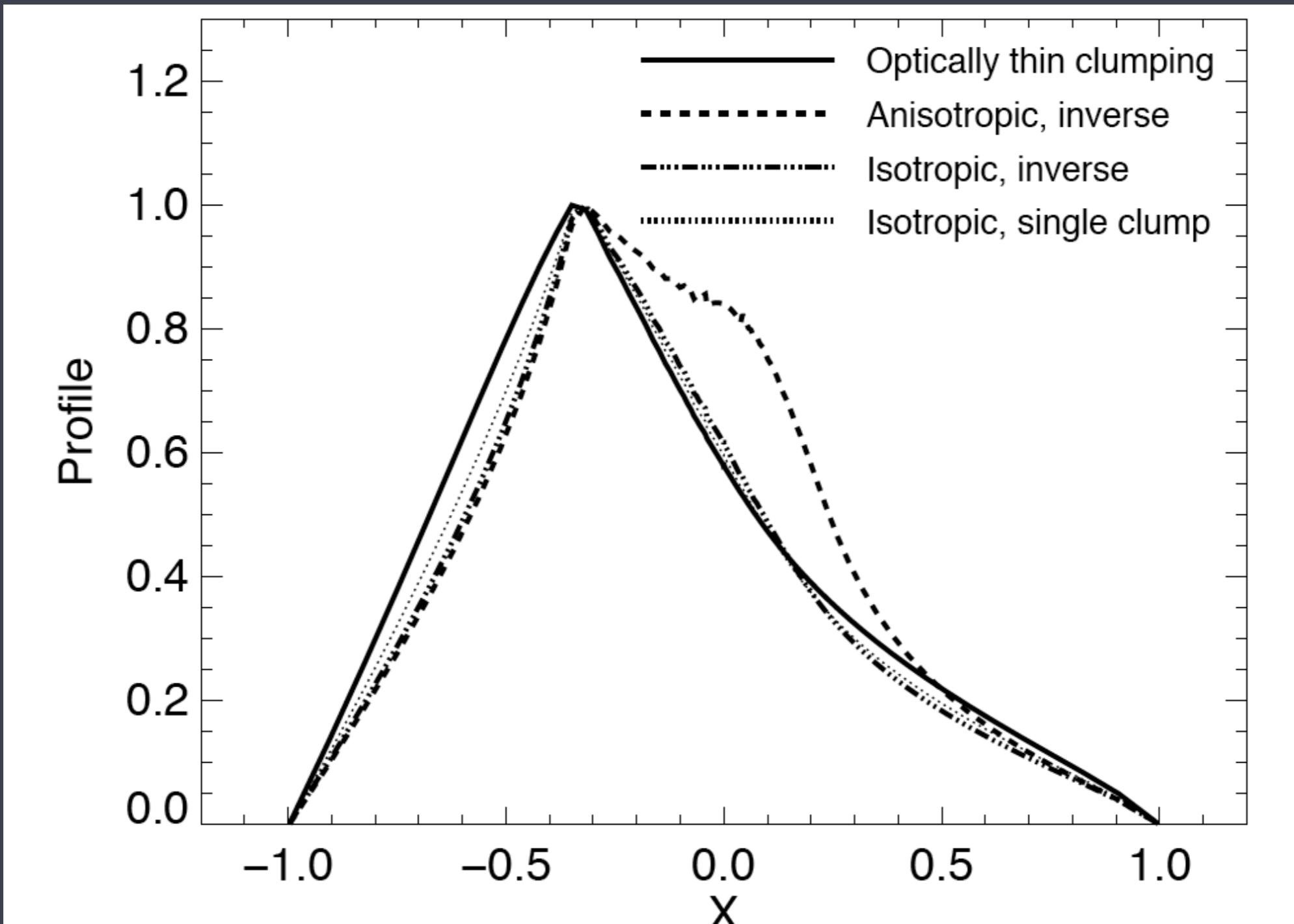
{0.1, 8., 1308}



anisotropic porosity

# Venetian blind bump

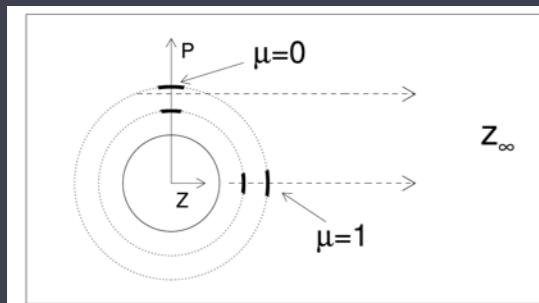
lateral escape is enhanced



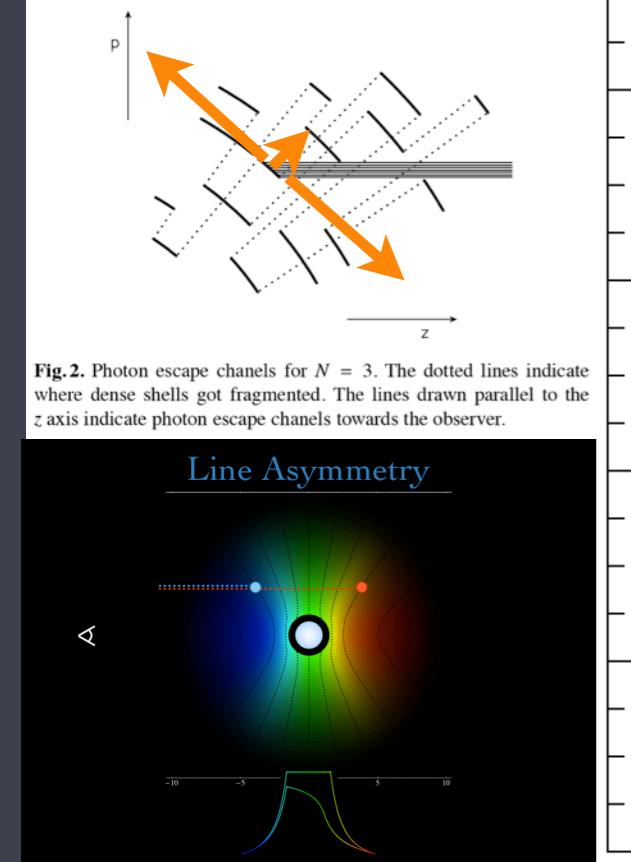
**Figure 5.** Line profiles for  $h_\infty/R_\star = 1.0$  and  $\tau_\star = 2.5$ , using different effective opacity laws, as labelled.

# Venetian blind bump

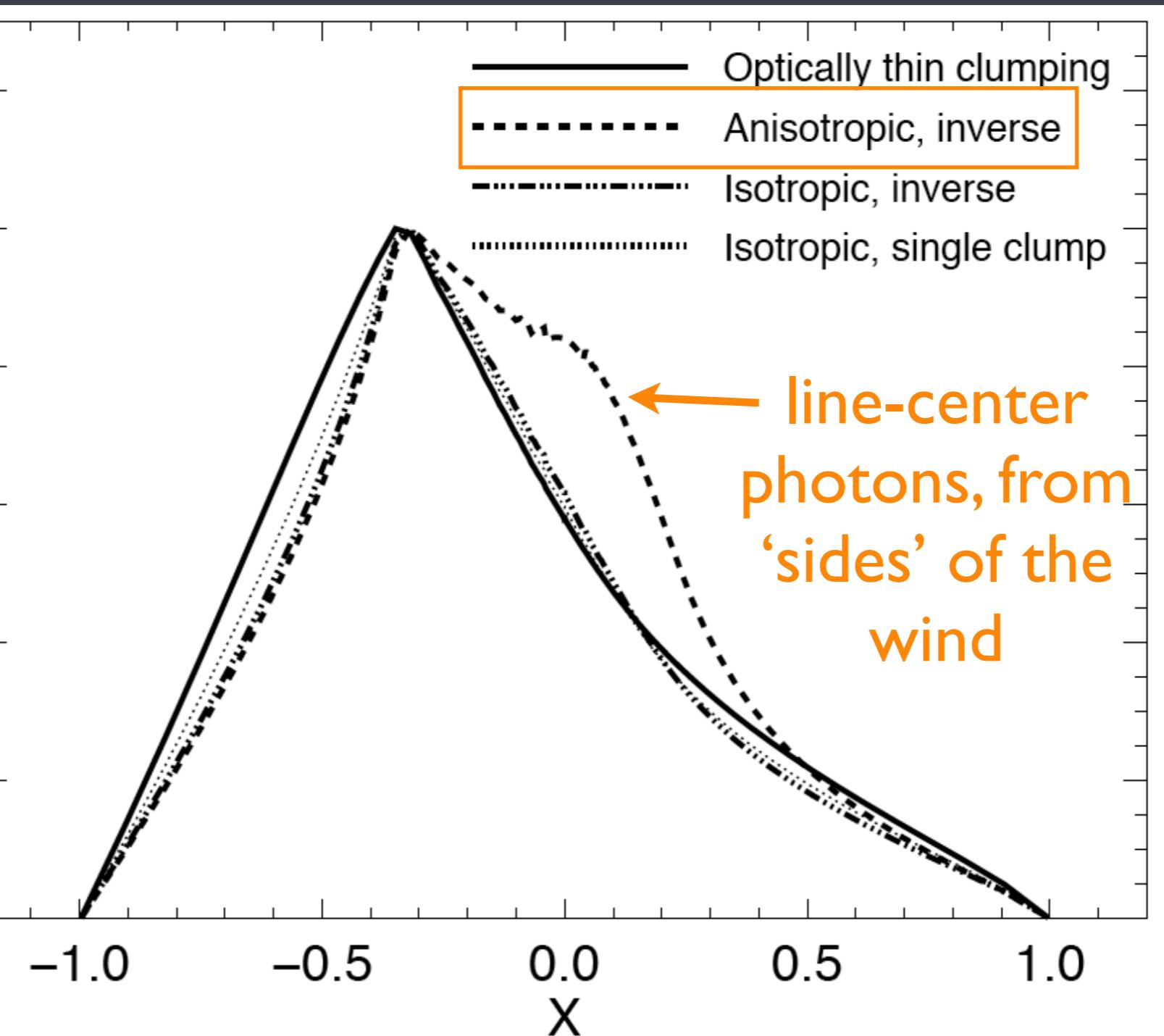
lateral escape is enhanced



**Figure 4.** Illustration of the ‘venetian blind’ effect seen in porosity models using an anisotropic effective opacity. The dashed arrowed lines represent two different  $p$ -rays and the observer is assumed to be located at  $z_\infty$ .



**Fig. 2.** Photon escape channels for  $N = 3$ . The dotted lines indicate where dense shells got fragmented. The lines drawn parallel to the  $z$  axis indicate photon escape channels towards the observer.

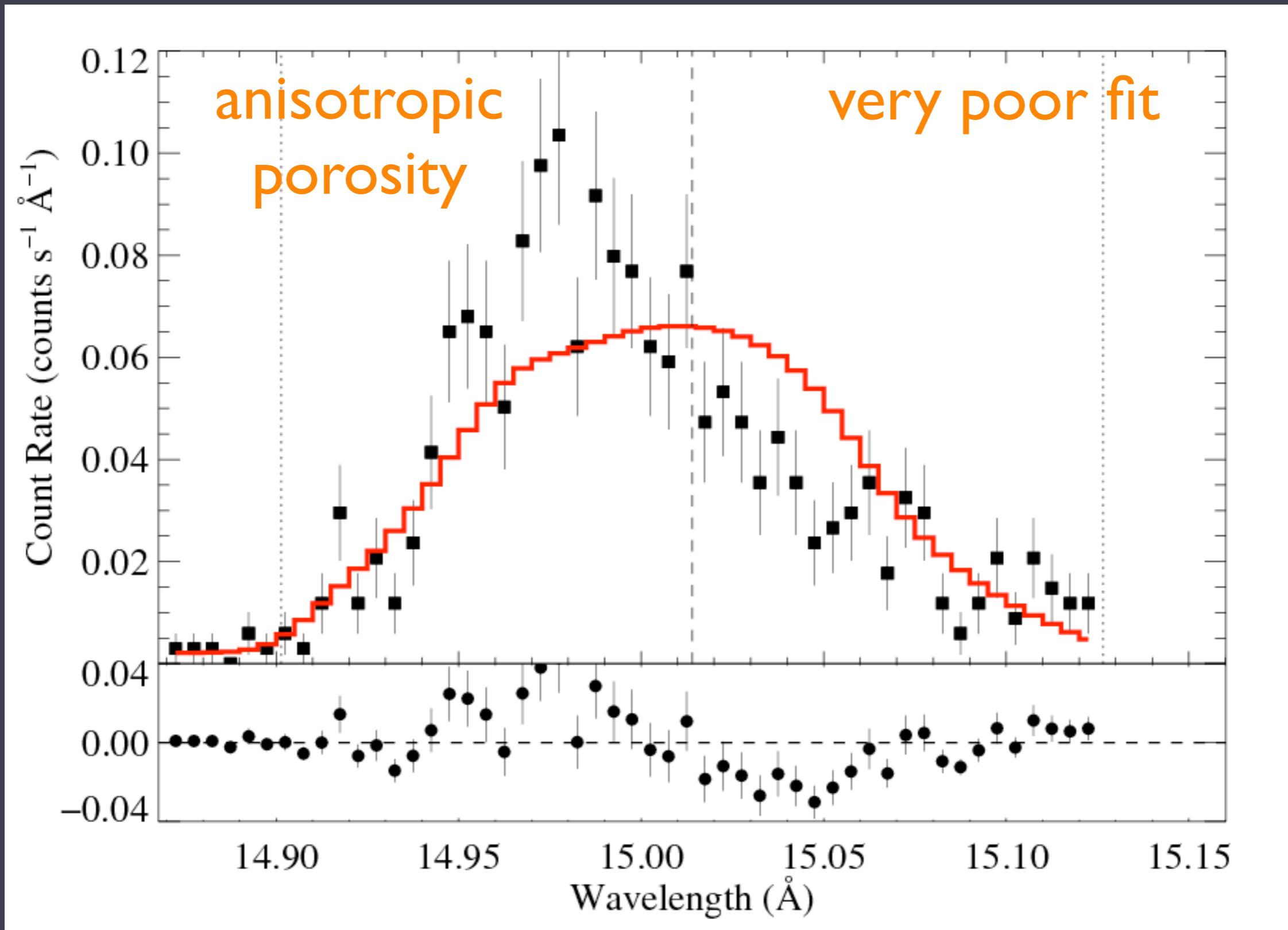


**Figure 5.** Line profiles for  $h_\infty/R_\star = 1.0$  and  $\tau_\star = 2.5$ , using different effective opacity laws, as labelled.

$\zeta$  Pup: Chandra

$h_\infty = 5$

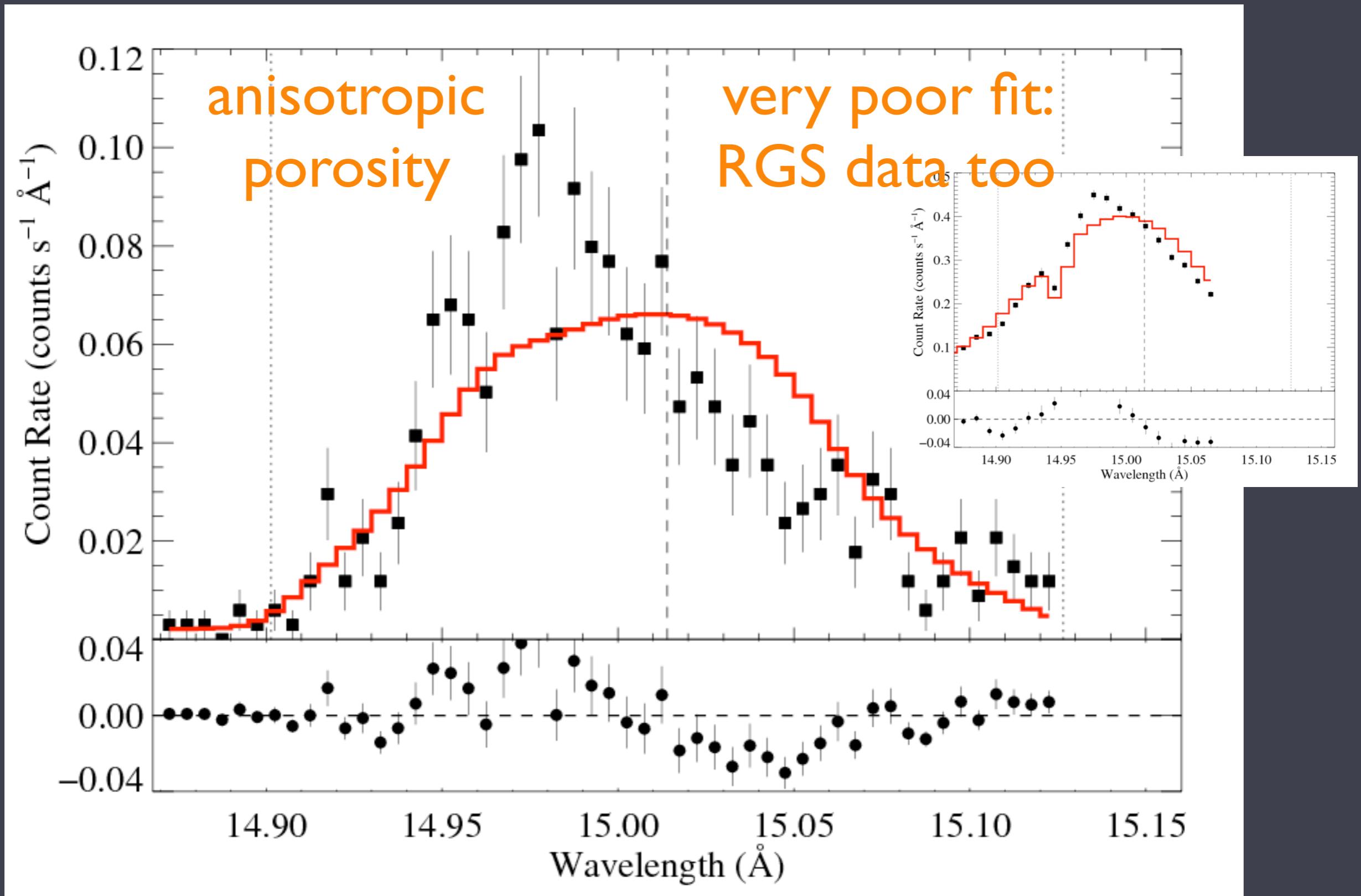
Fe XVII 15.014 Å



$\zeta$  Pup: Chandra

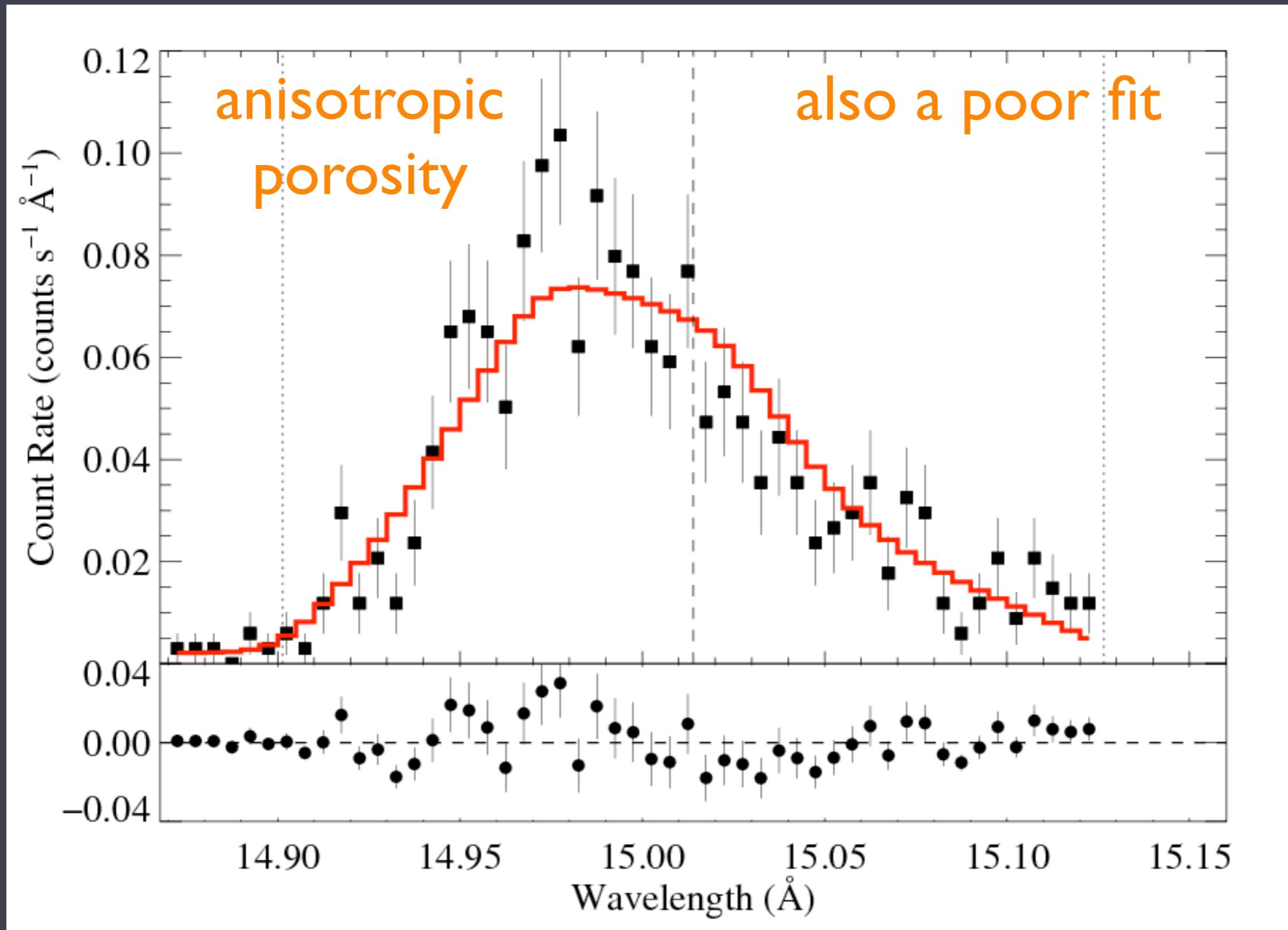
$h_\infty = 5$

Fe XVII 15.014 Å



$\zeta$  Pup: Chandra

$h_\infty = 0.5$  Fe XVII 15.014 Å



# Conclusion 3

Even modest *anisotropic* porosity can be rejected

# Global Conclusion

Porosity is *not* important in hot star winds

1. High porosity can be rejected
2. Moderate porosity ( $h_\infty \leq 1$ ) increases  $T_*$  by only 20% to 30%
3. Even modest *anisotropic* porosity can be rejected

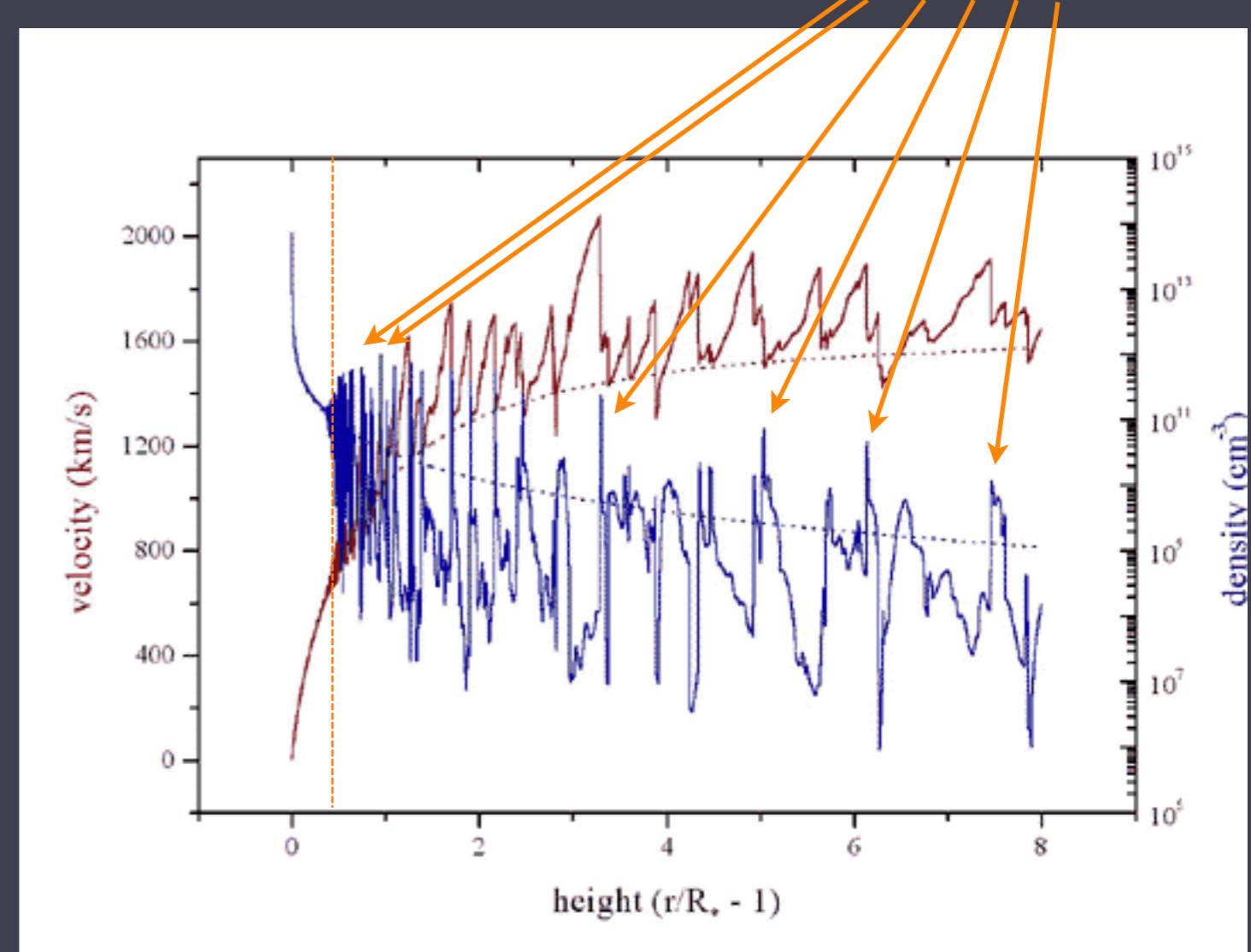
# Theory context: perhaps this is not surprising

## 1-D numerical simulations

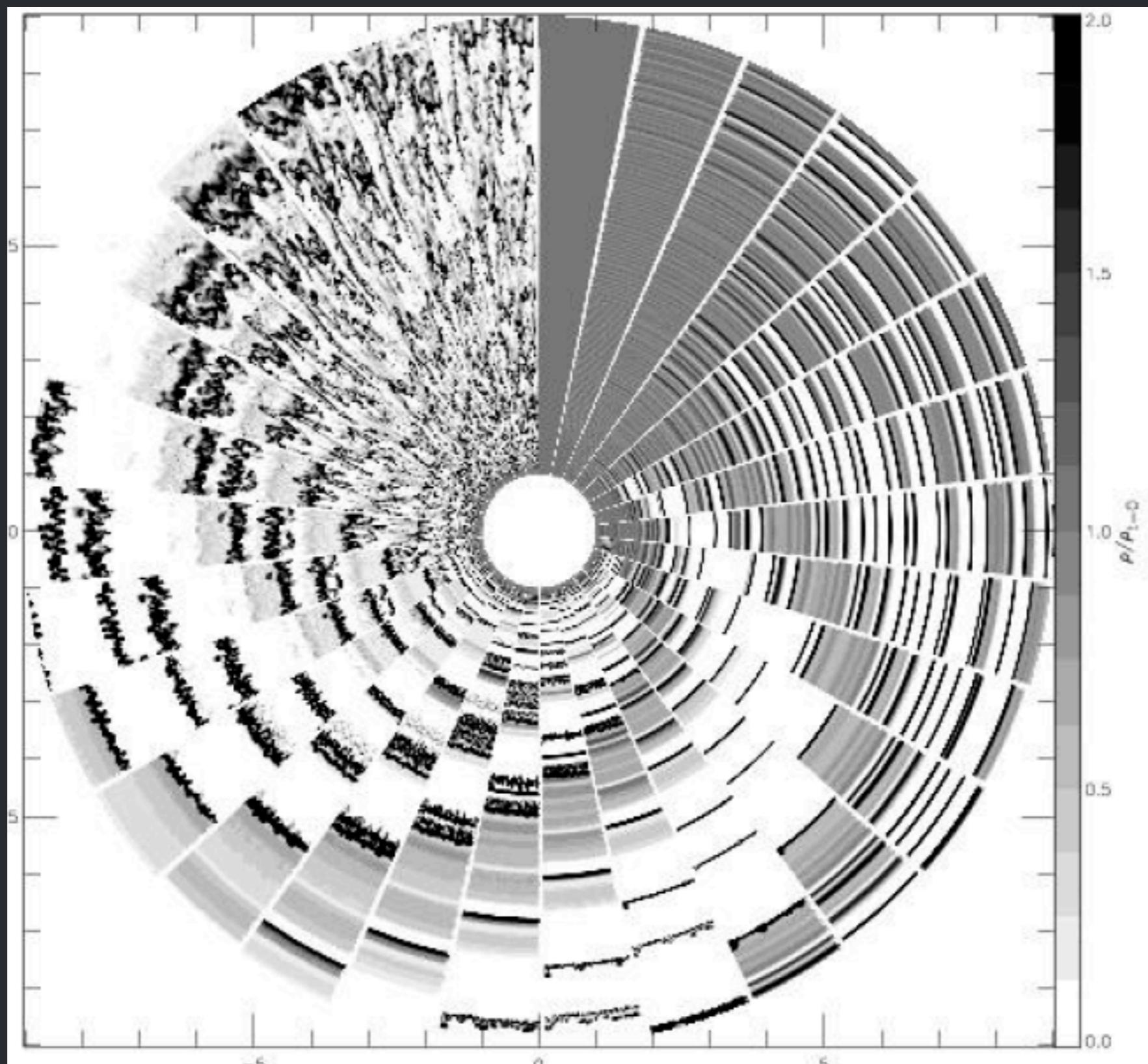
reasons why 1-D simulations  
overestimate porosity

**clumps**

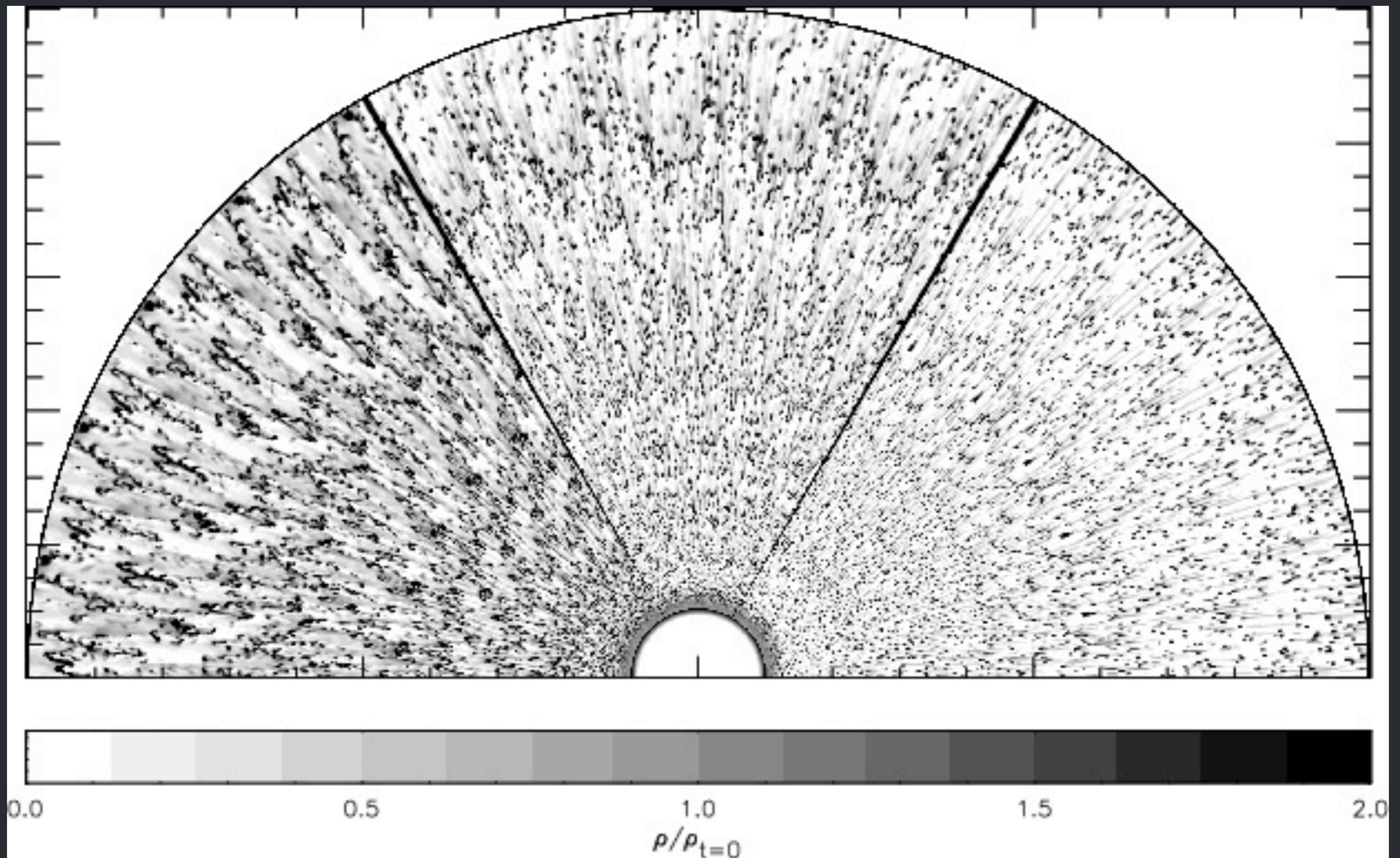
- geometry: all “clumps” are spherical shells
- inner wind has  $h \ll h_\infty$
- grid resolution



# More realistic 2-D simulations: R-T like break-up; structure on quite small scales



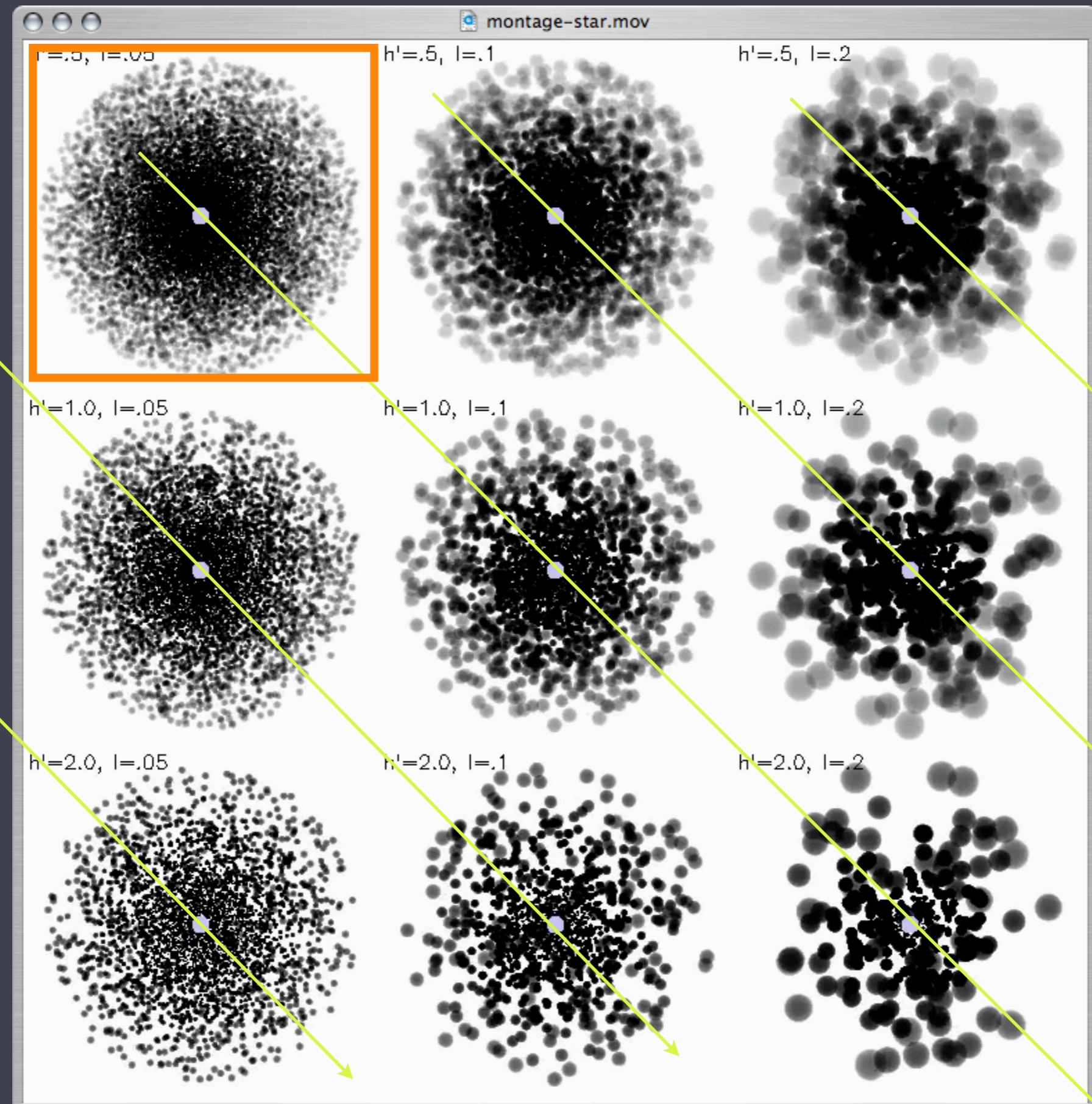
In some cases, structure approaches the grid scale: clumps are very small; not optically thick



less  
porous  
 $f_{\text{cl}} \sim 20$

$f_{\text{cl}} \sim 40$

more  
porous



small clumps

big clumps

$f_{\text{cl}} \sim 2.5$

$f_{\text{cl}} \sim 5$

$f_{\text{cl}} \sim 10$

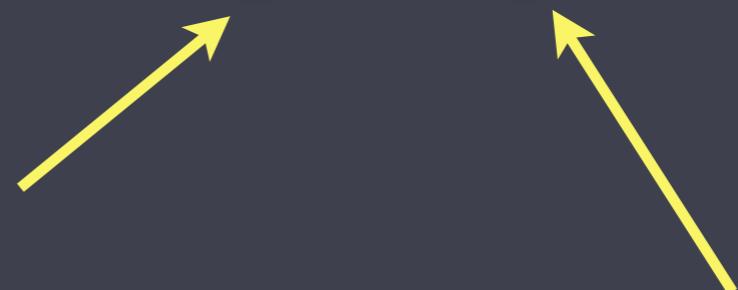
So, clumping *without* porosity.

What observational constraints?

# X-ray line profiles to measure the clumping factor and the mass-loss rate

basic definition:  $f_{\text{cl}} \equiv \langle \rho^2 \rangle / \langle \rho \rangle^2$

from density-squared  
diagnostic like H $\alpha$



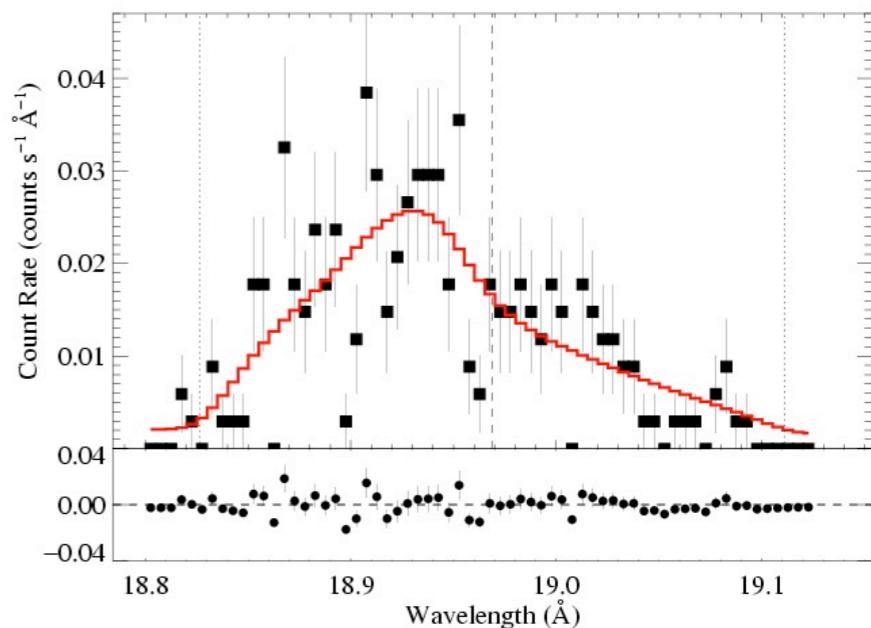
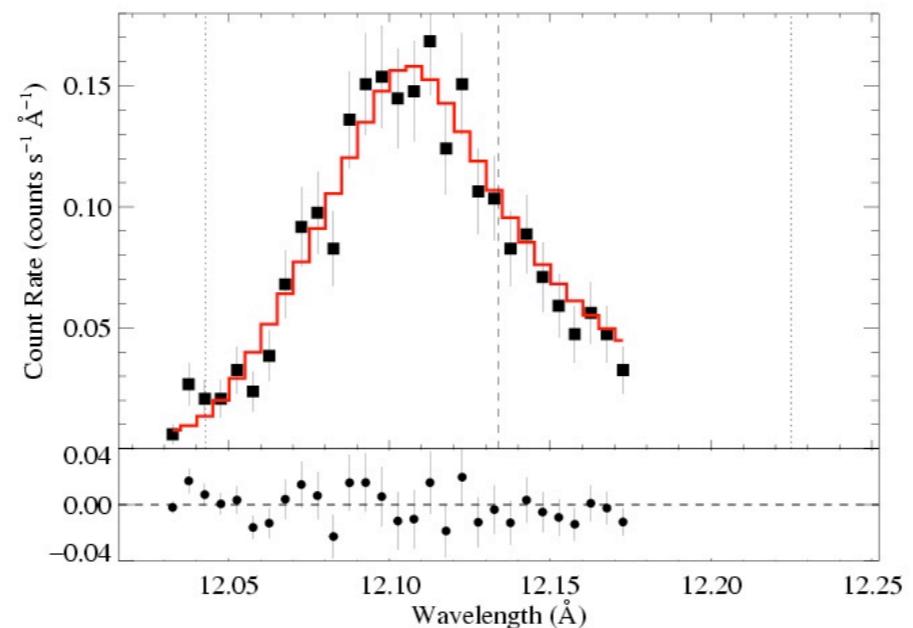
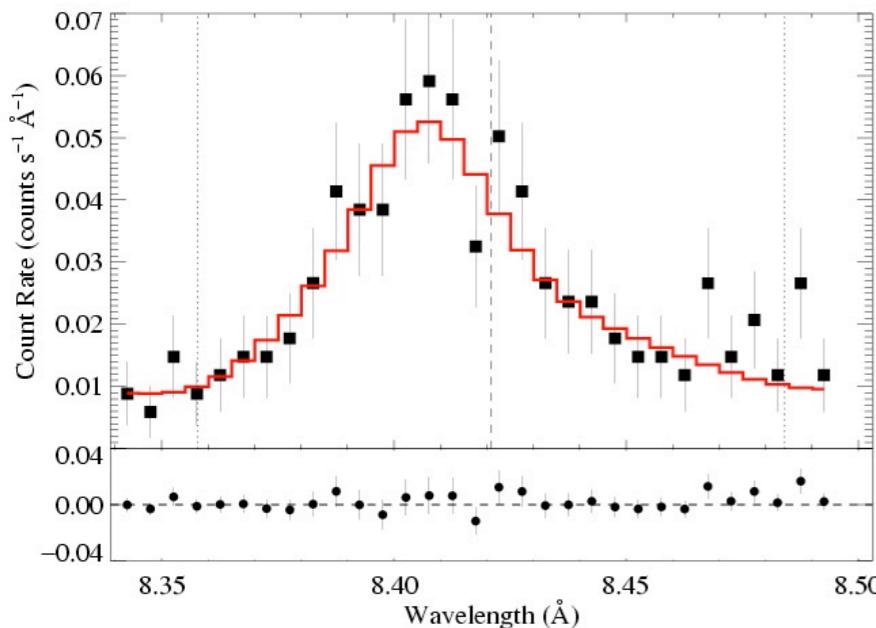
from (column) density  
diagnostic like T $\star$  from  
X-ray profiles

# $\zeta$ Pup *Chandra*: three emission lines

Mg Ly $\alpha$ : 8.42 Å

Ne Ly $\alpha$ : 12.13 Å

O Ly $\alpha$ : 18.97 Å



$\tau_* = 1$

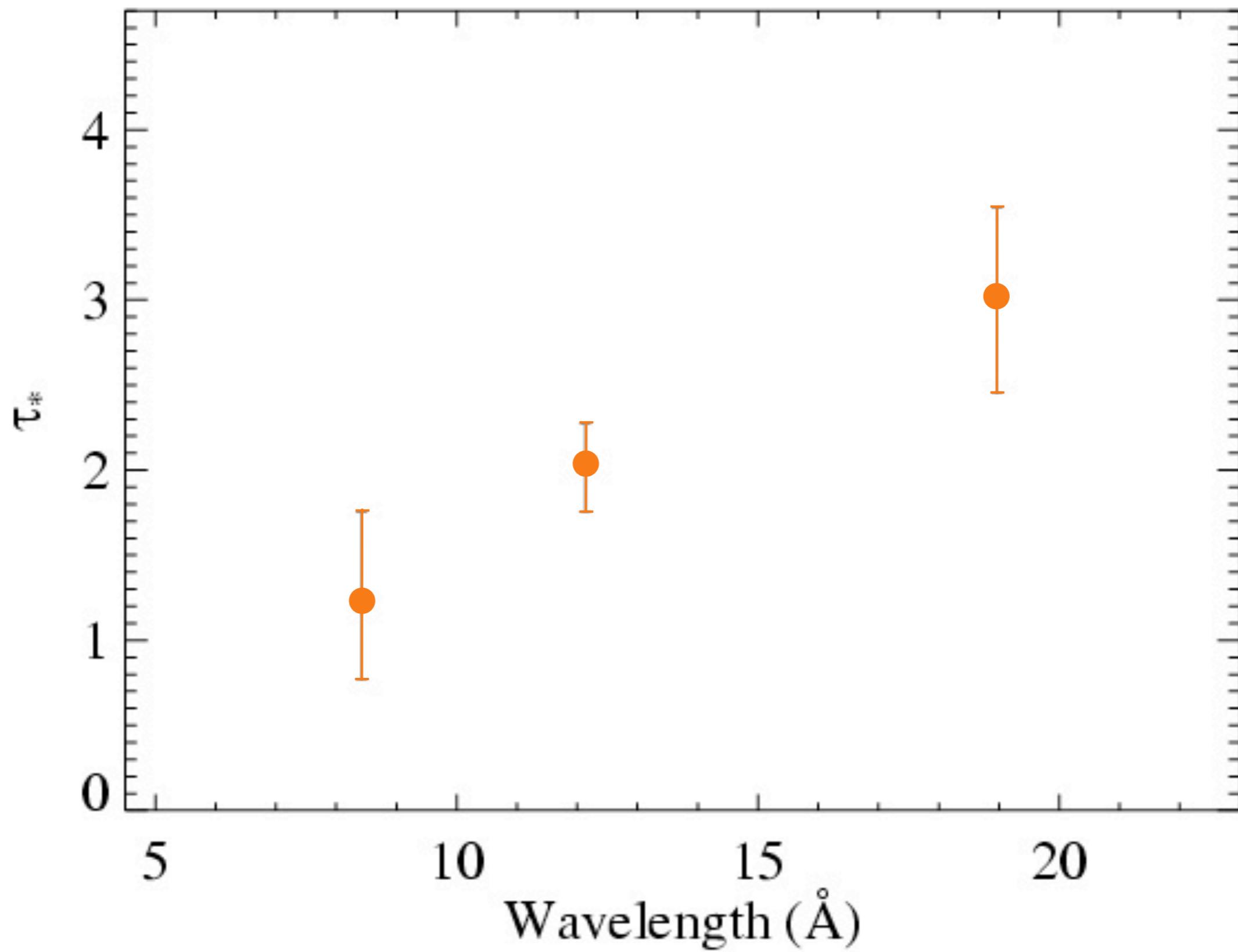
$\tau_* = 2$

$\tau_* = 3$

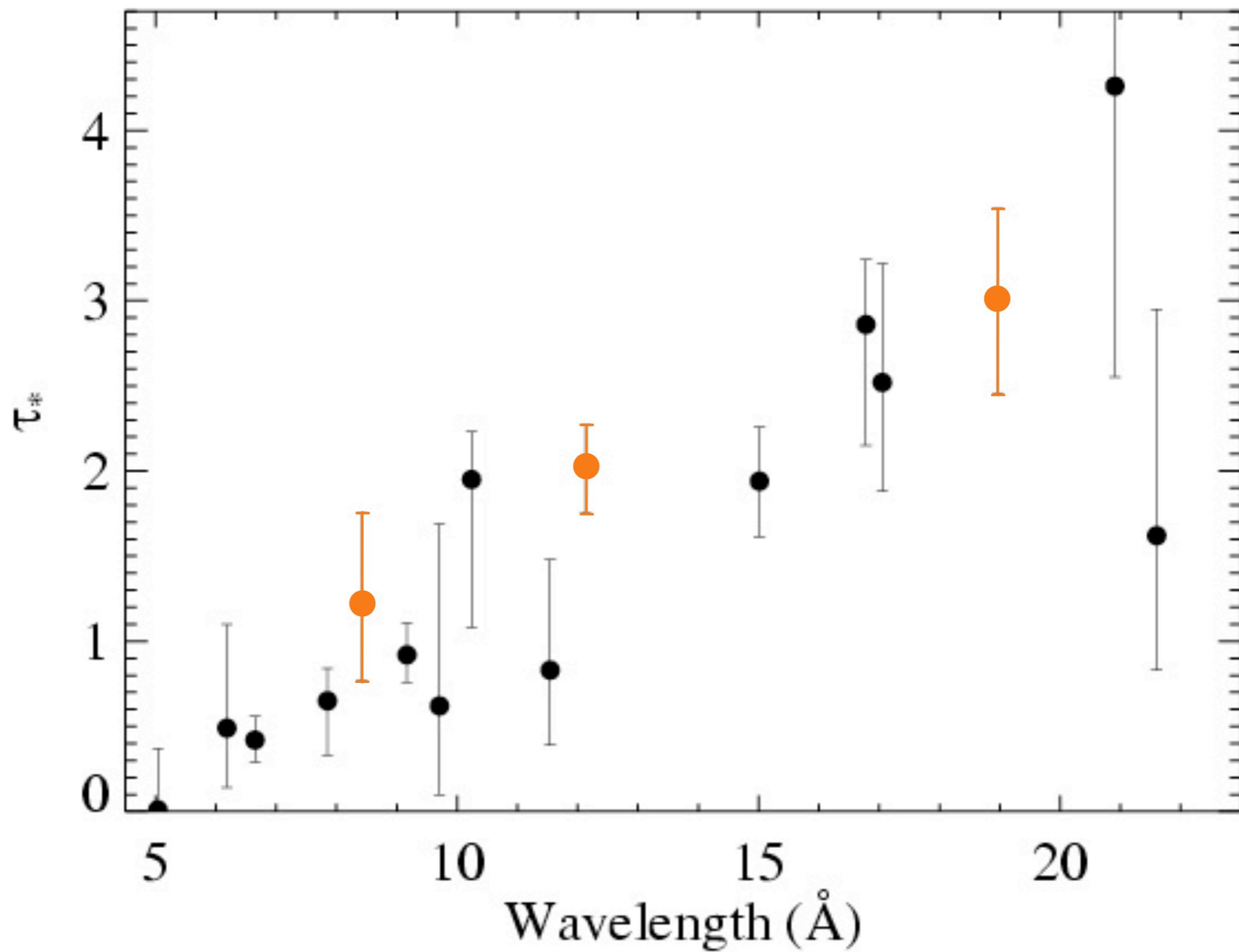
Recall:

$$\tau_* \equiv \frac{\kappa \dot{M}}{4\pi R_* v_\infty}$$

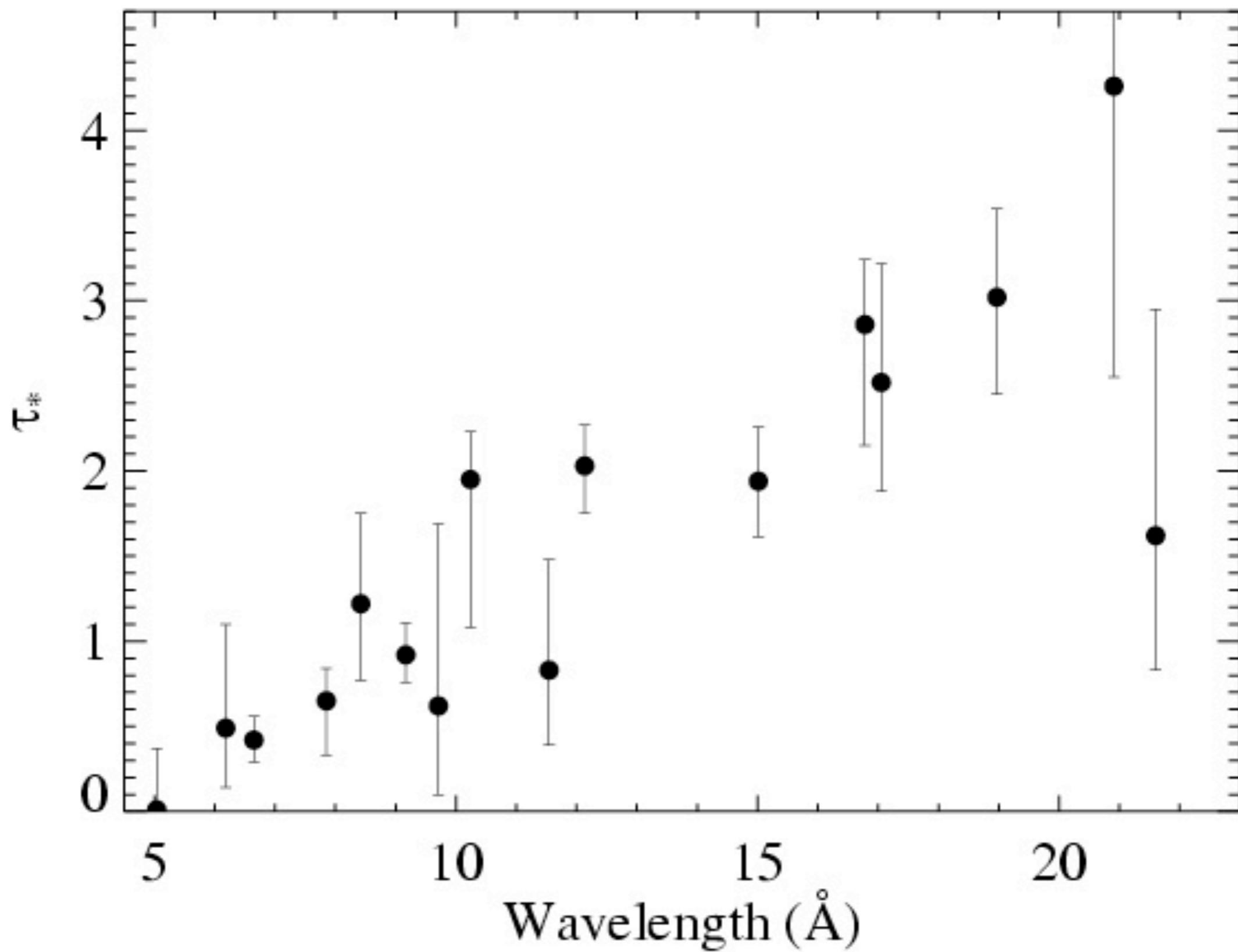
Results from the 3 line fits shown previously



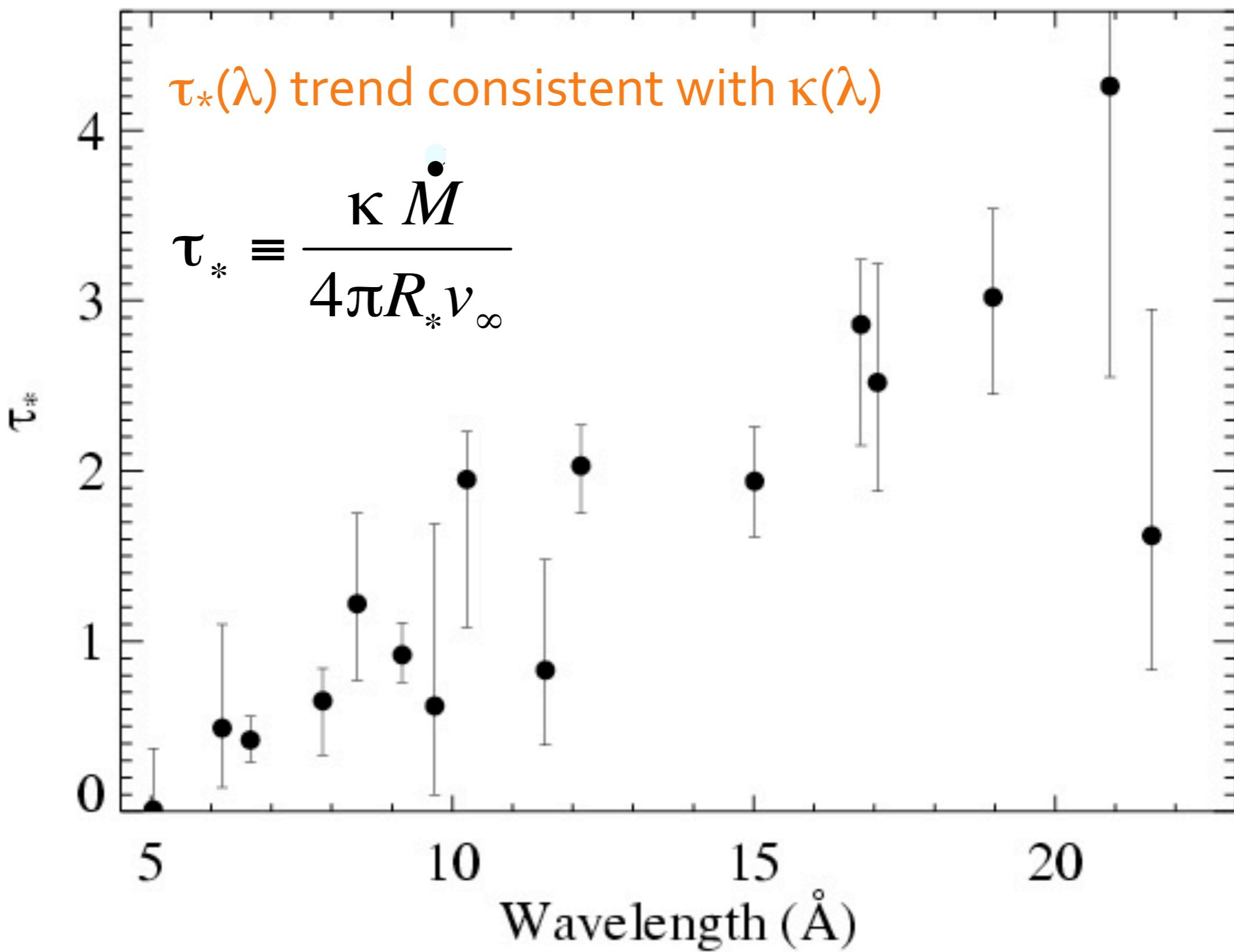
# Fits to 16 lines in the *Chandra* spectrum of $\zeta$ Pup



# Fits to 16 lines in the *Chandra* spectrum of $\zeta$ Pup

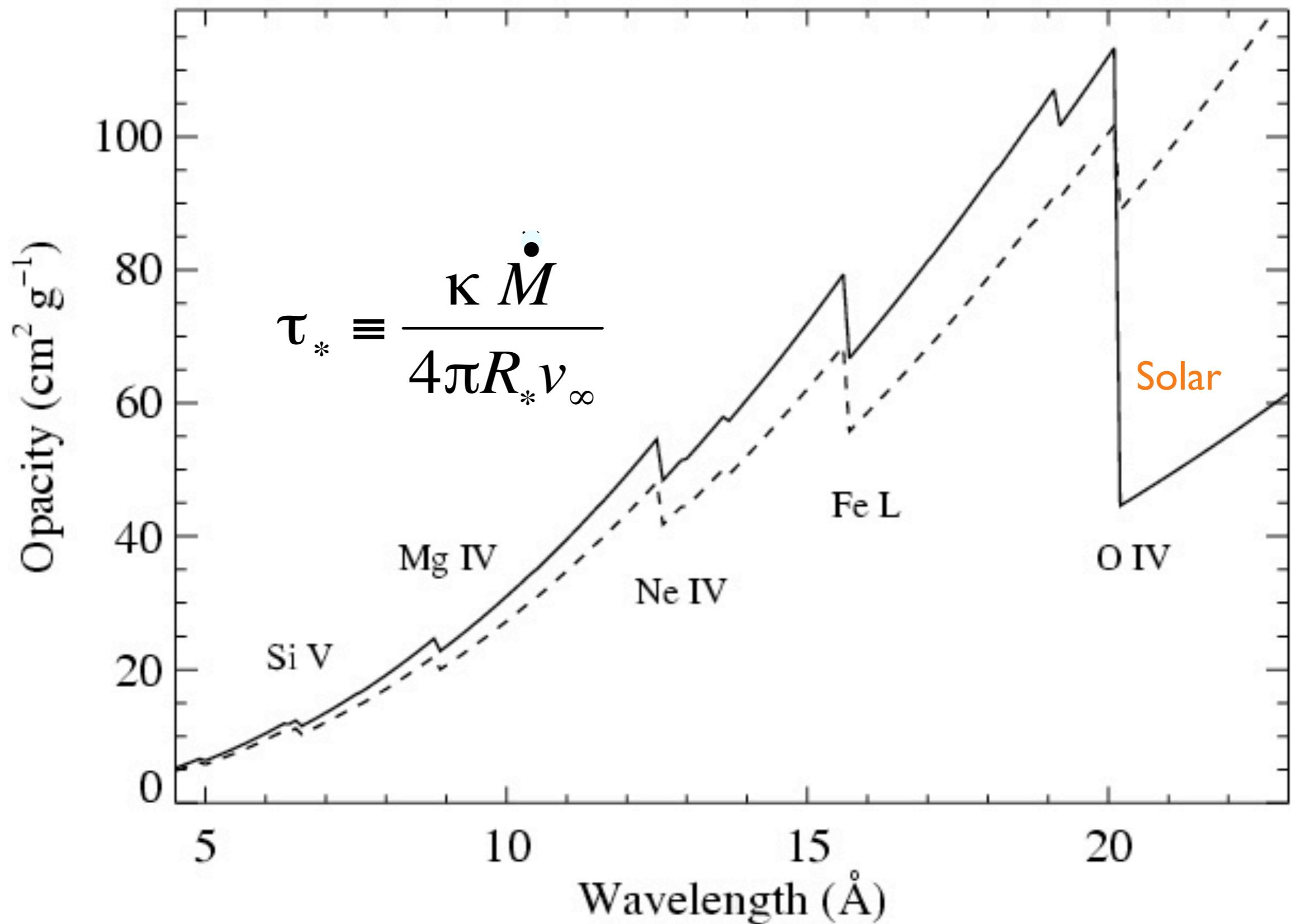


# Fits to 16 lines in the *Chandra* spectrum of $\zeta$ Pup



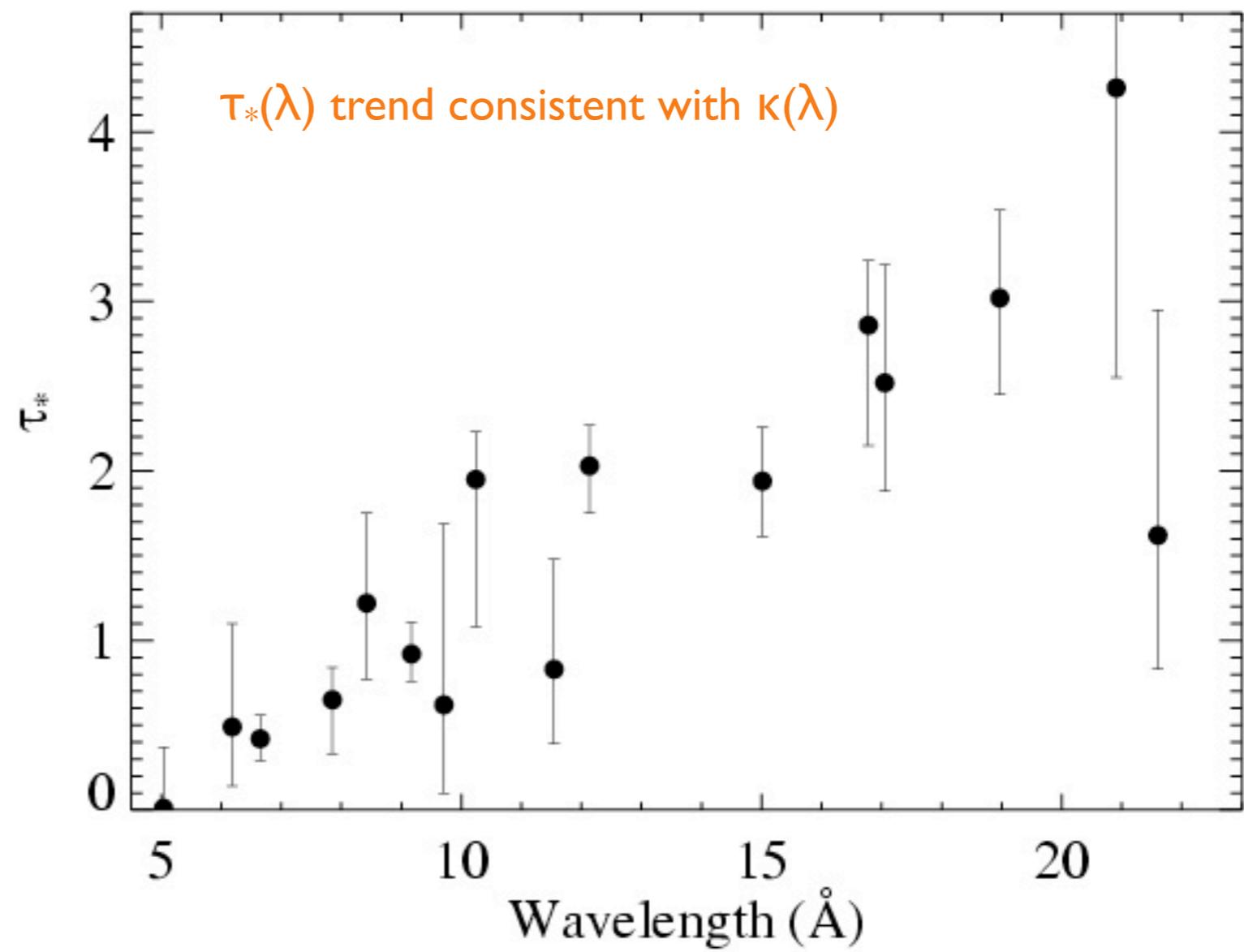
# Fits to 16 lines in the *Chandra* spectrum of $\zeta$ Pup

CNO processed



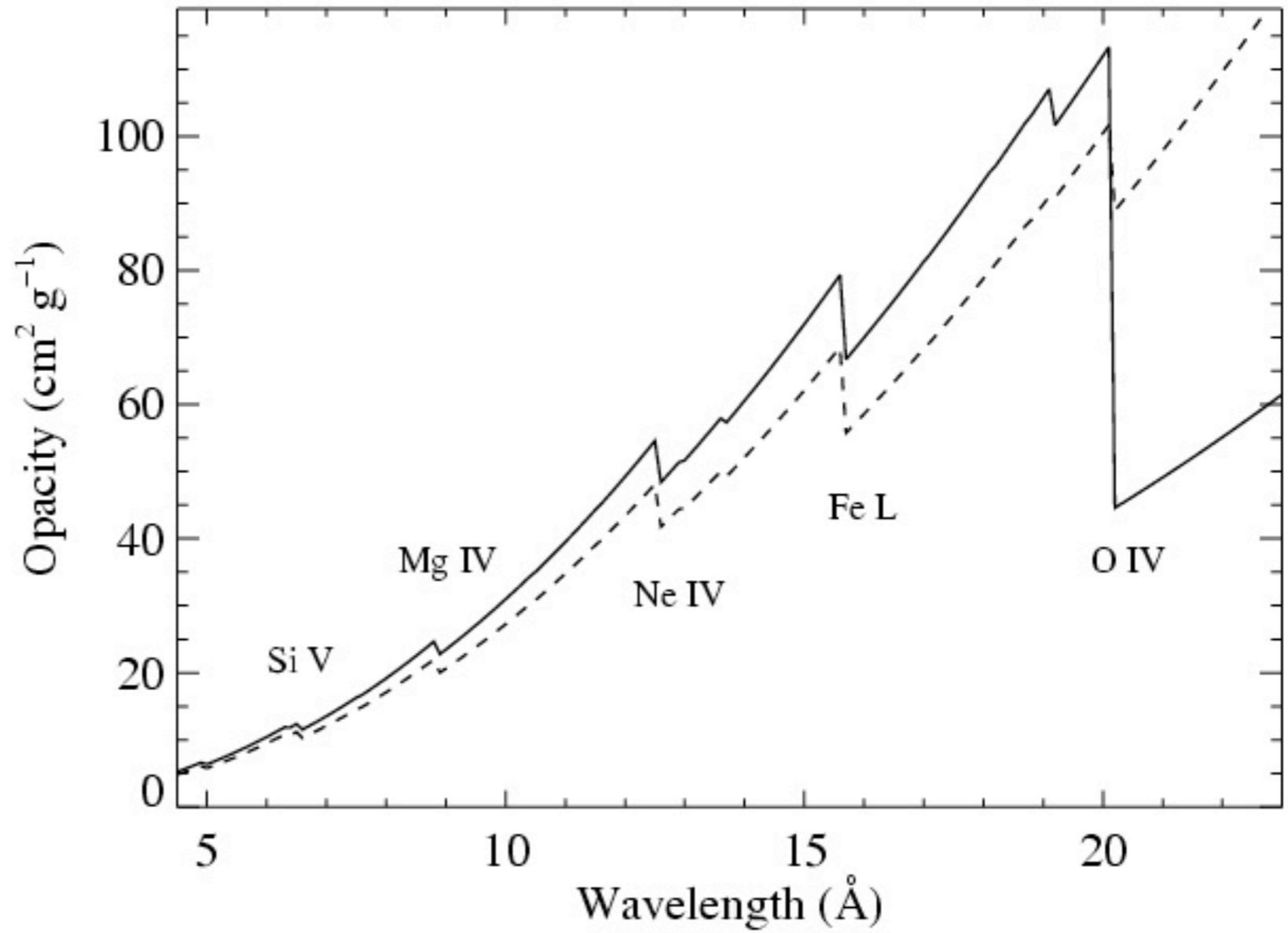
$$\tau_* \equiv \frac{\kappa \dot{M}}{4\pi R_* v_\infty}$$

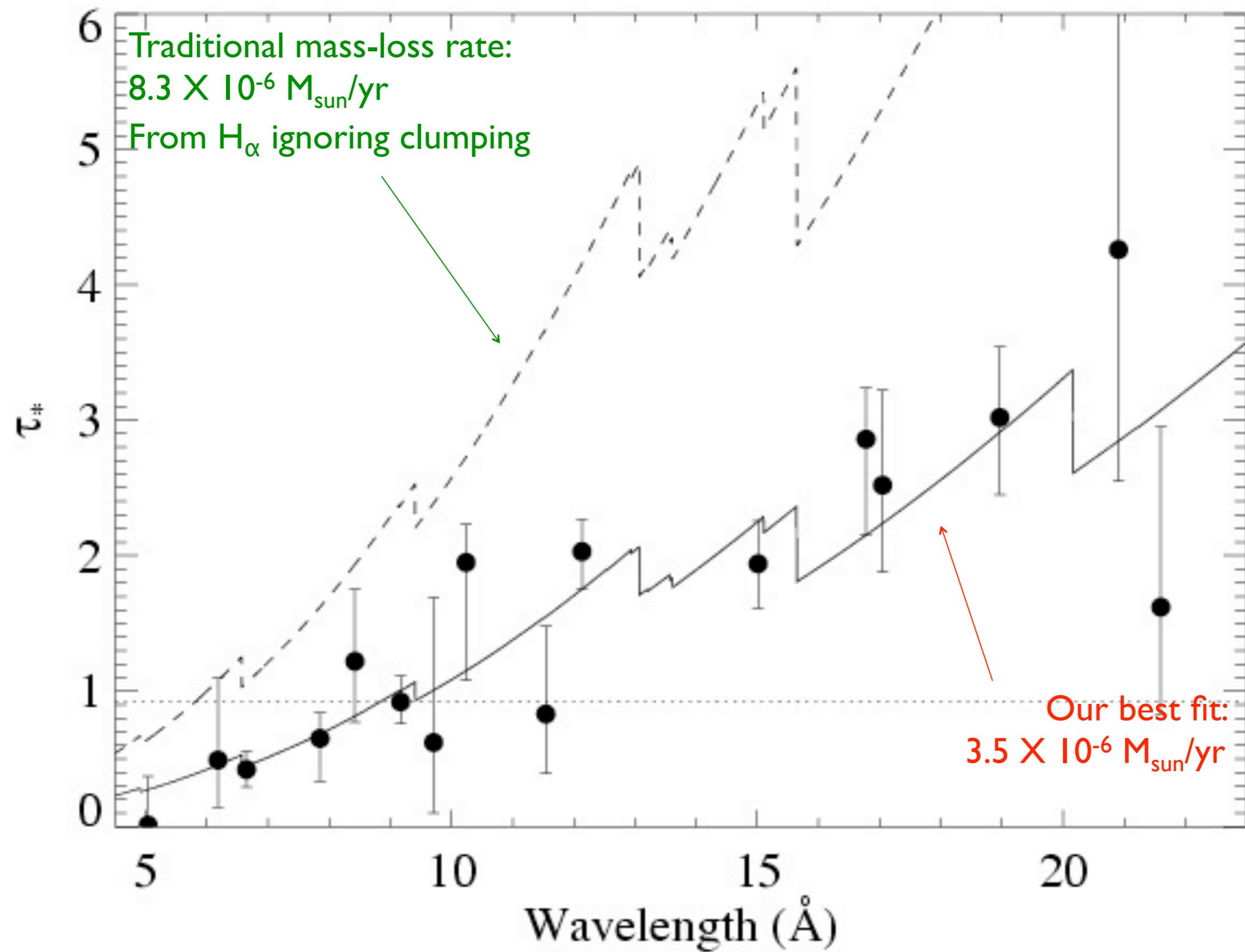
$\dot{M}$  becomes the free parameter of  
the fit to the  $\tau_*(\lambda)$  trend

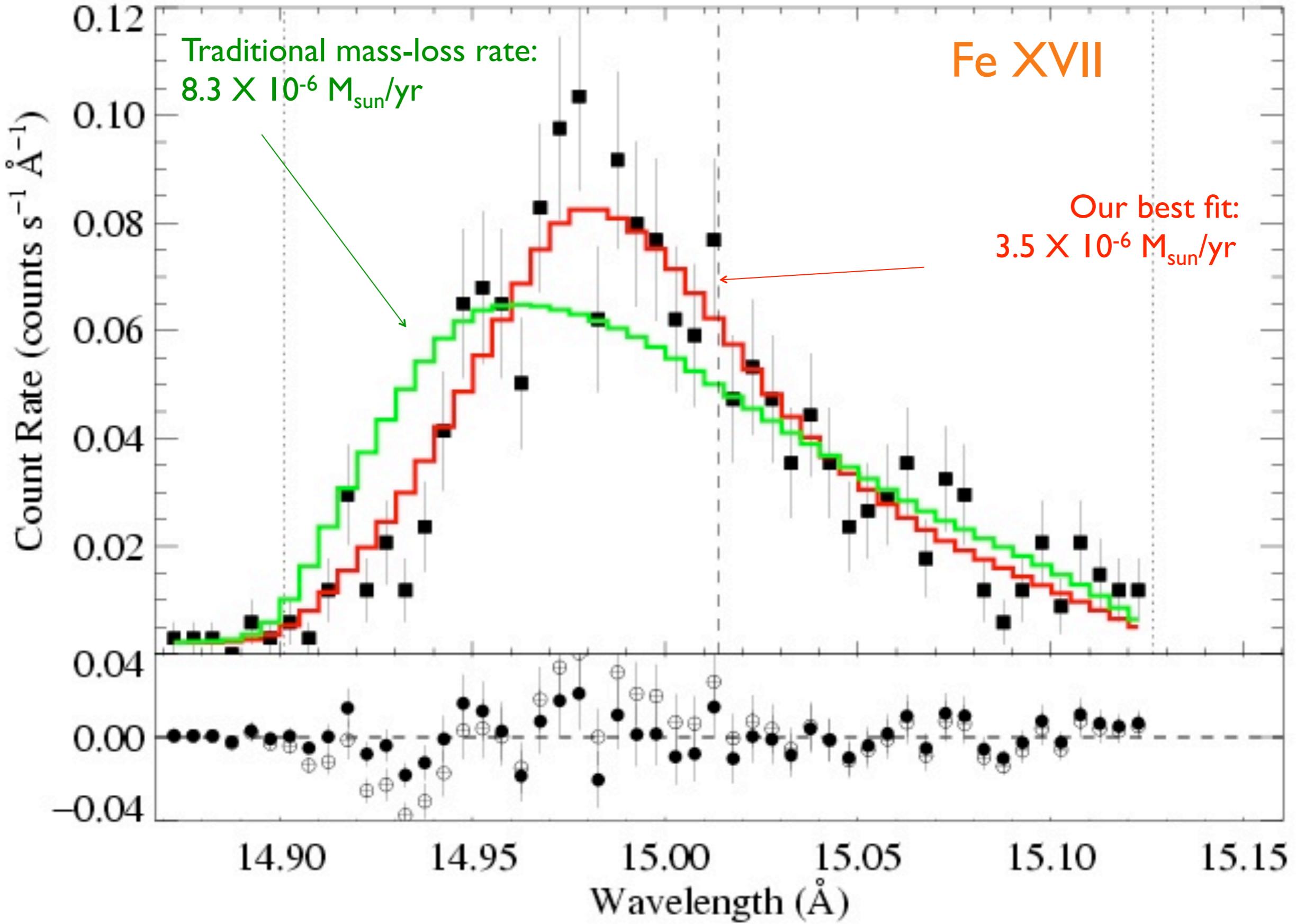


$$\tau_* \equiv \frac{\kappa \dot{M}}{4\pi R_* v_\infty}$$

$\dot{M}$  becomes the free parameter of the fit to the  $\tau_*(\lambda)$  trend







## Bright OB stars in the Galaxy

### III. Constraints on the radial stratification of the clumping factor in hot star winds from a combined H <sub>$\alpha$</sub> , IR and radio analysis\*

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<sup>5</sup> Sternberg Astronomical Institute, Universitetski pr. 13, Moscow, 119992, Russia, e-mail: taranova@sai.msu.ru

<sup>6</sup> Department of Physics and Astronomy, University College London, Gower Street, London WC1E 6BT, UK, e-mail: awxb@star.ucl.ac.uk, idh@star.ucl.ac.uk

Received; accepted

**Abstract.** Recent results strongly challenge the canonical picture of massive star winds: various evidence indicates that currently accepted mass-loss rates,  $\dot{M}$ , may need to be revised downwards, by factors extending to one magnitude or even more. This is because the most commonly used mass-loss diagnostics are affected by “clumping” (small-scale density inhomogeneities), influencing our interpretation of observed spectra and fluxes.

Such downward revisions would have dramatic consequences for the evolution of, and feedback from, massive stars, and thus robust determinations of the clumping properties and mass-loss rates are urgently needed. We present a first attempt concerning this objective, by means of constraining the radial stratification of the so-called clumping factor.

To this end, we have analyzed a sample of 19 Galactic O-type supergiants/giants, by combining our own and archival data for H <sub>$\alpha$</sub> , IR, mm and radio fluxes, and using approximate methods, calibrated to more sophisticated models. Clumping has been included into our analysis in the “conventional” way, by assuming the inter-clump matter to be void. Because (almost) all our diagnostics depends on the square of density, we cannot derive absolute clumping factors, but only factors normalized to a certain minimum.

This minimum was usually found to be located in the outermost, radio-emitting region, i.e., the radio mass-loss rates are the lowest ones, compared to  $\dot{M}$  derived from H <sub>$\alpha$</sub>  and the IR. The radio rates agree well with those predicted by theory, but are only upper limits, due to unknown clumping in the outer wind. H <sub>$\alpha$</sub>  turned out to be a useful tool to derive the clumping properties inside  $r < 3..5 R_*$ . Our most important result concerns a (physical) difference between denser and thinner winds: for denser winds, the innermost region is more strongly clumped than the outermost one (with a normalized clumping factor of  $4.1 \pm 1.4$ ), whereas thinner winds have similar clumping properties in the inner and outer regions.

Our findings are compared with theoretical predictions, and the implications are discussed in detail, by assuming different scenarios regarding the still unknown clumping properties of the outer wind.

# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

$$f_{\text{cl}} = 1 \text{ @ } r < 1.12 R_{\ast}$$

$$f_{\text{cl}} = 5.5 \text{ @ } 1.12 < r < 1.5 R_{\ast}$$

$$f_{\text{cl}} = 3.1 \text{ @ } 1.5 < r < 2 R_{\ast}$$

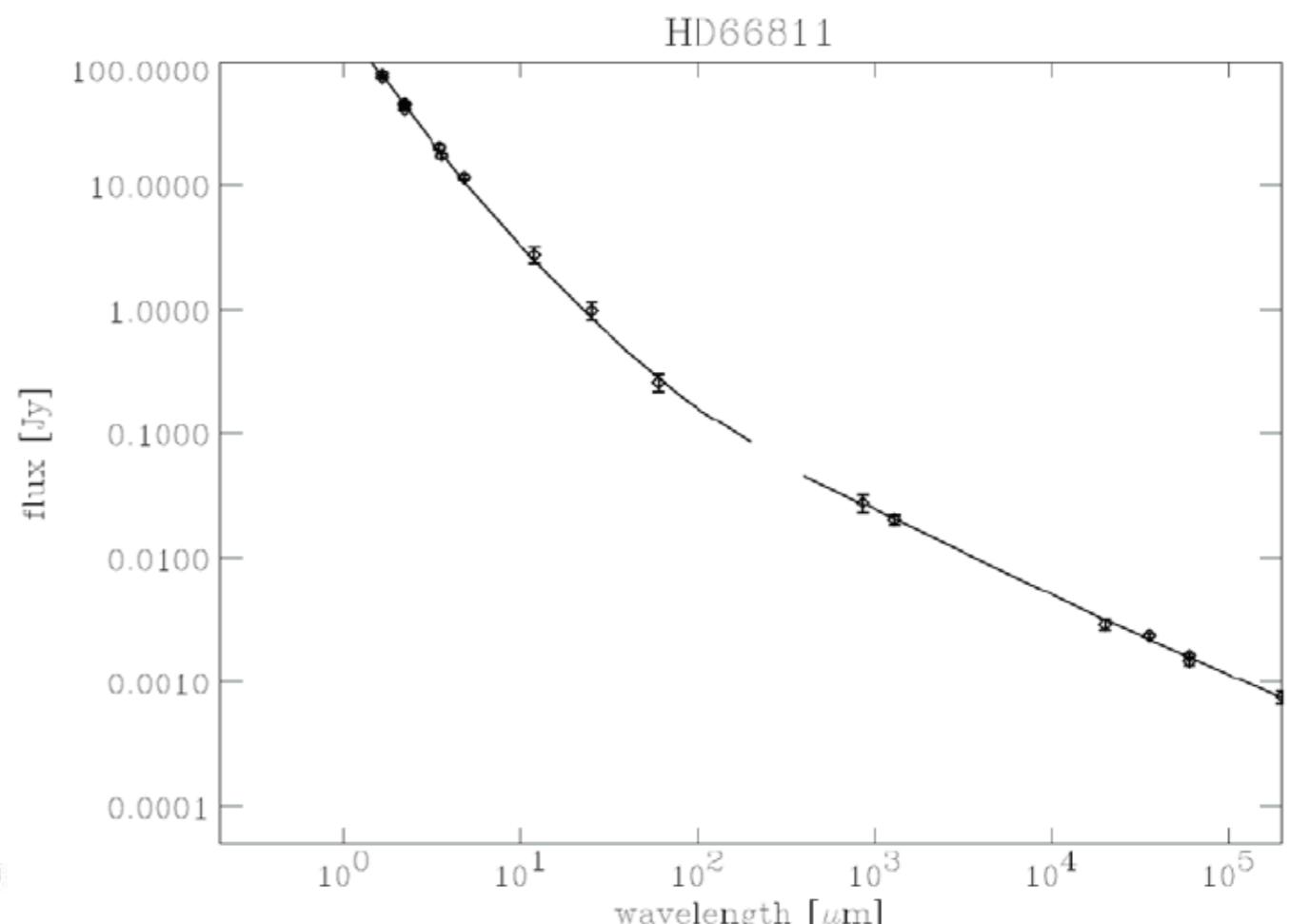
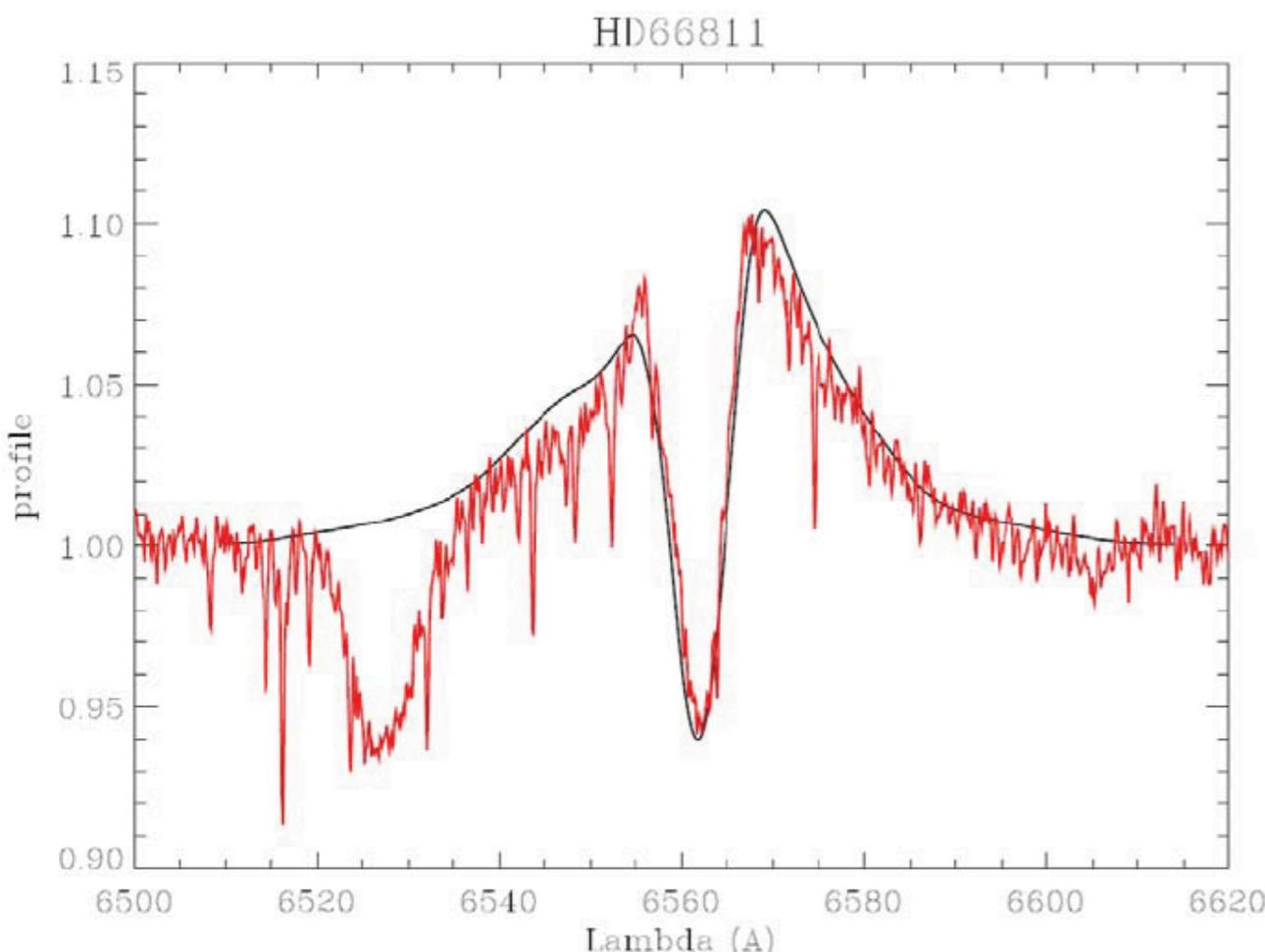
$$f_{\text{cl}} = 2 \text{ @ } 2 < r < 15 R_{\ast}$$

$$f_{\text{cl}} = 1 \text{ @ } r > 15 R_{\ast}$$

H $\alpha$

IR

radio



# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

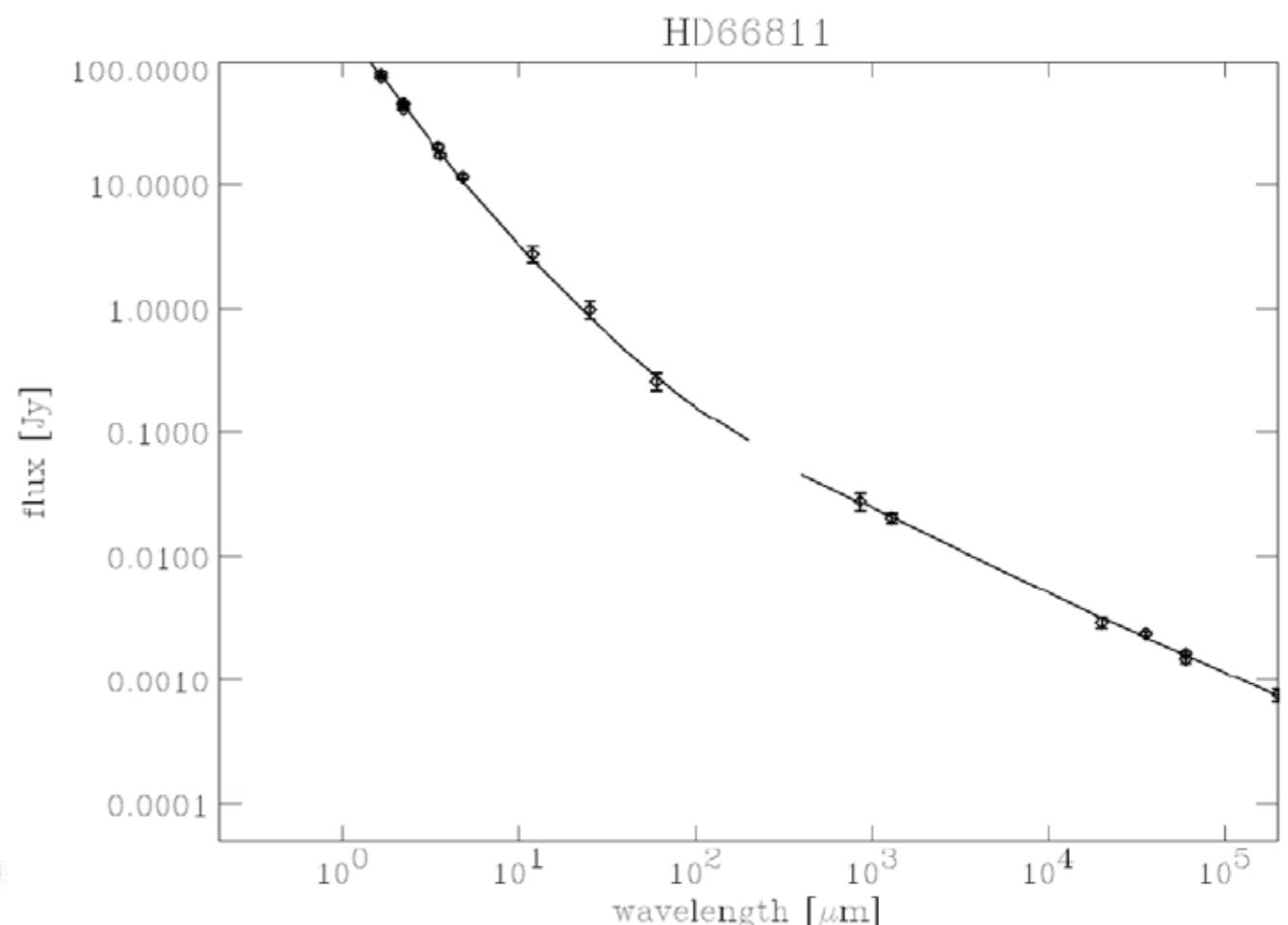
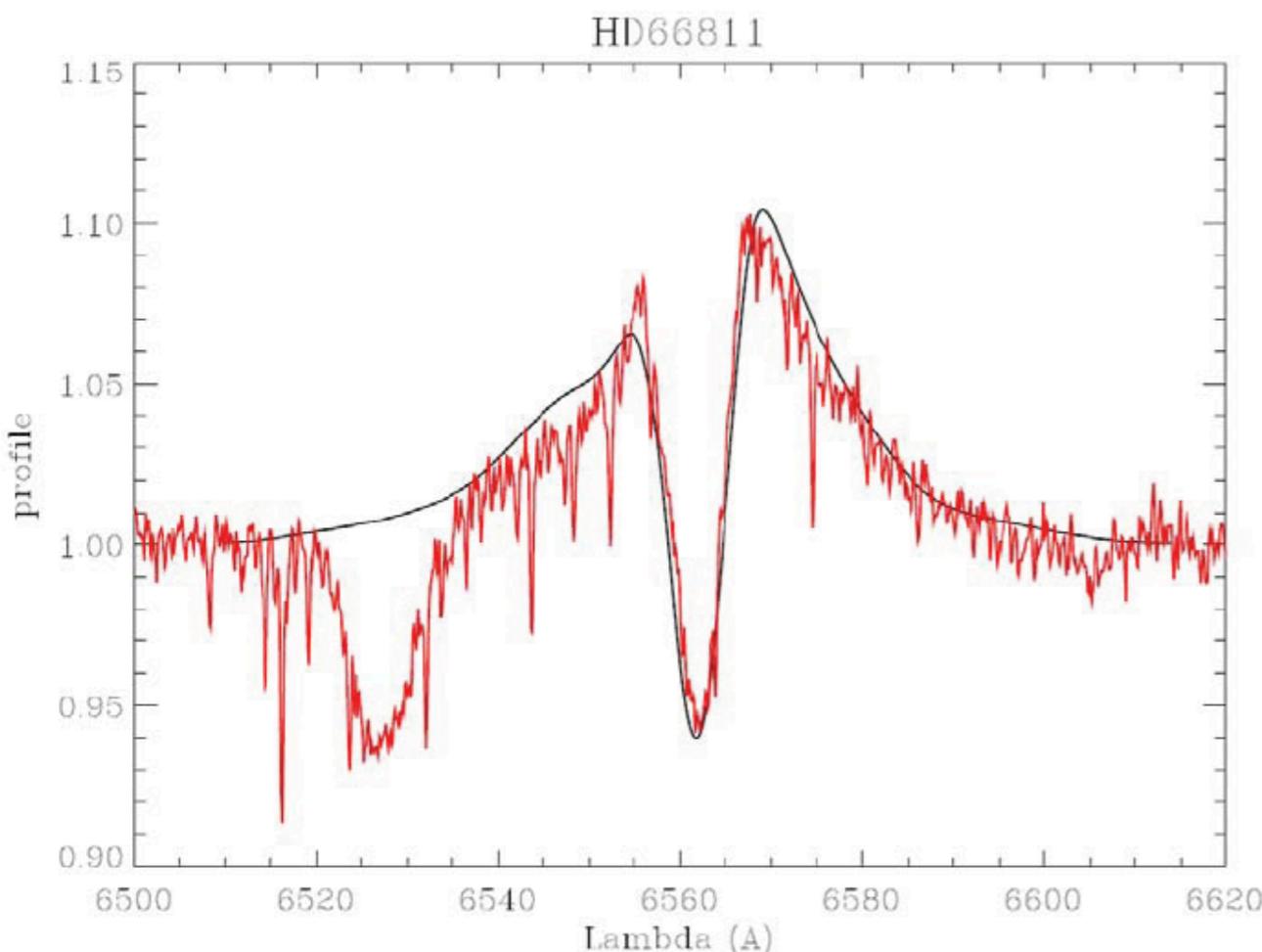
scale up slightly:  
 $f_{\text{cl}} \sim 6$  in the H $\alpha$  region

$f_{\text{cl}} = 1 @ r < 1.12 R_*$   
 $f_{\text{cl}} = 5.5 @ 1.12 < r < 1.5 R_*$   
 $f_{\text{cl}} = 3.1 @ 1.5 < r < 2 R_*$   
 $f_{\text{cl}} = 2 @ 2 < r < 15 R_*$   
 $f_{\text{cl}} = 1 @ r > 15 R_*$

H $\alpha$

IR

radio



$\zeta$  Pup

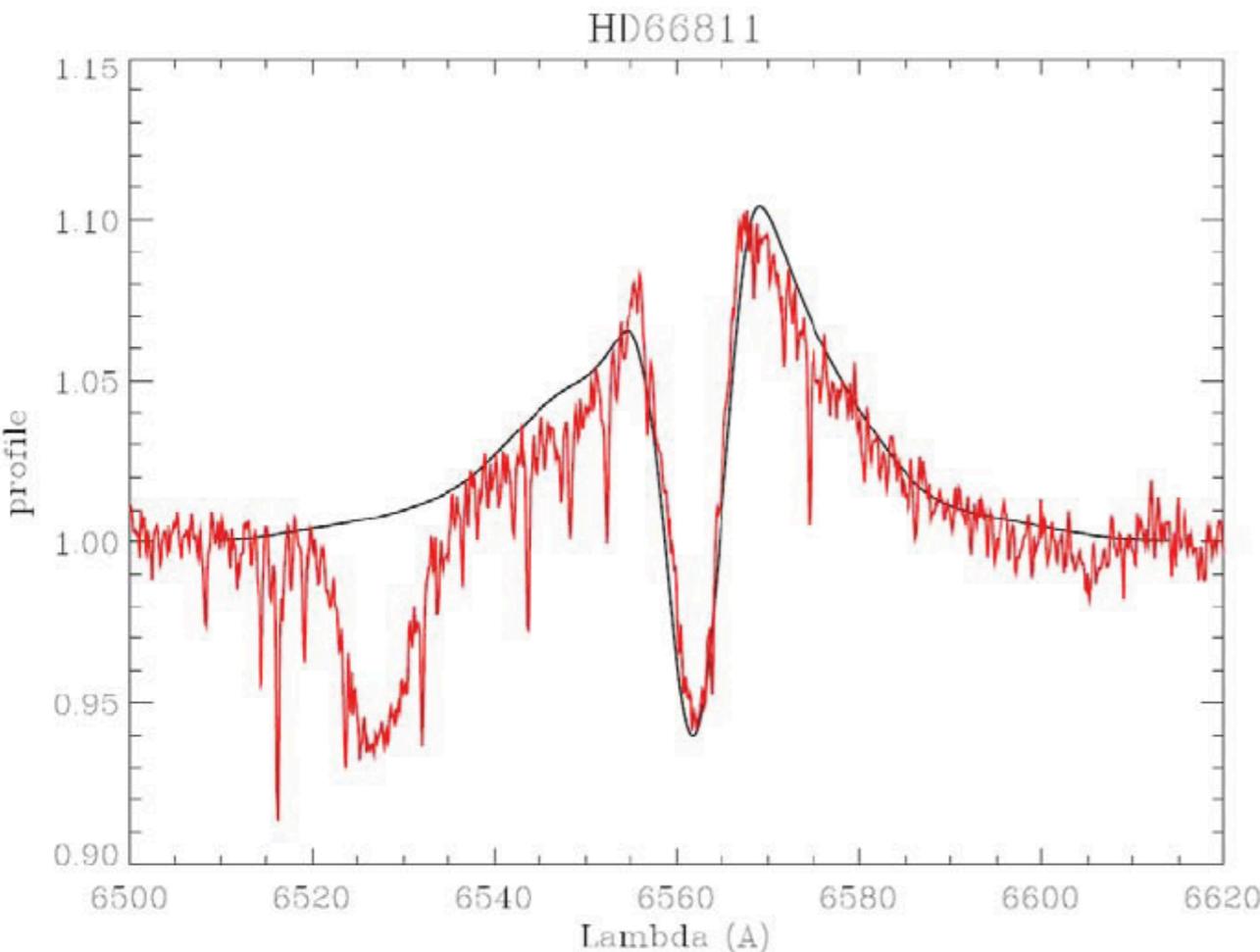
for  $\dot{M} = 3.5 \times 10^{-6} M_{\text{sun}}/\text{yr}$

scale up slightly:  
 $f_{\text{cl}} \sim 6$  in the H $\alpha$  region

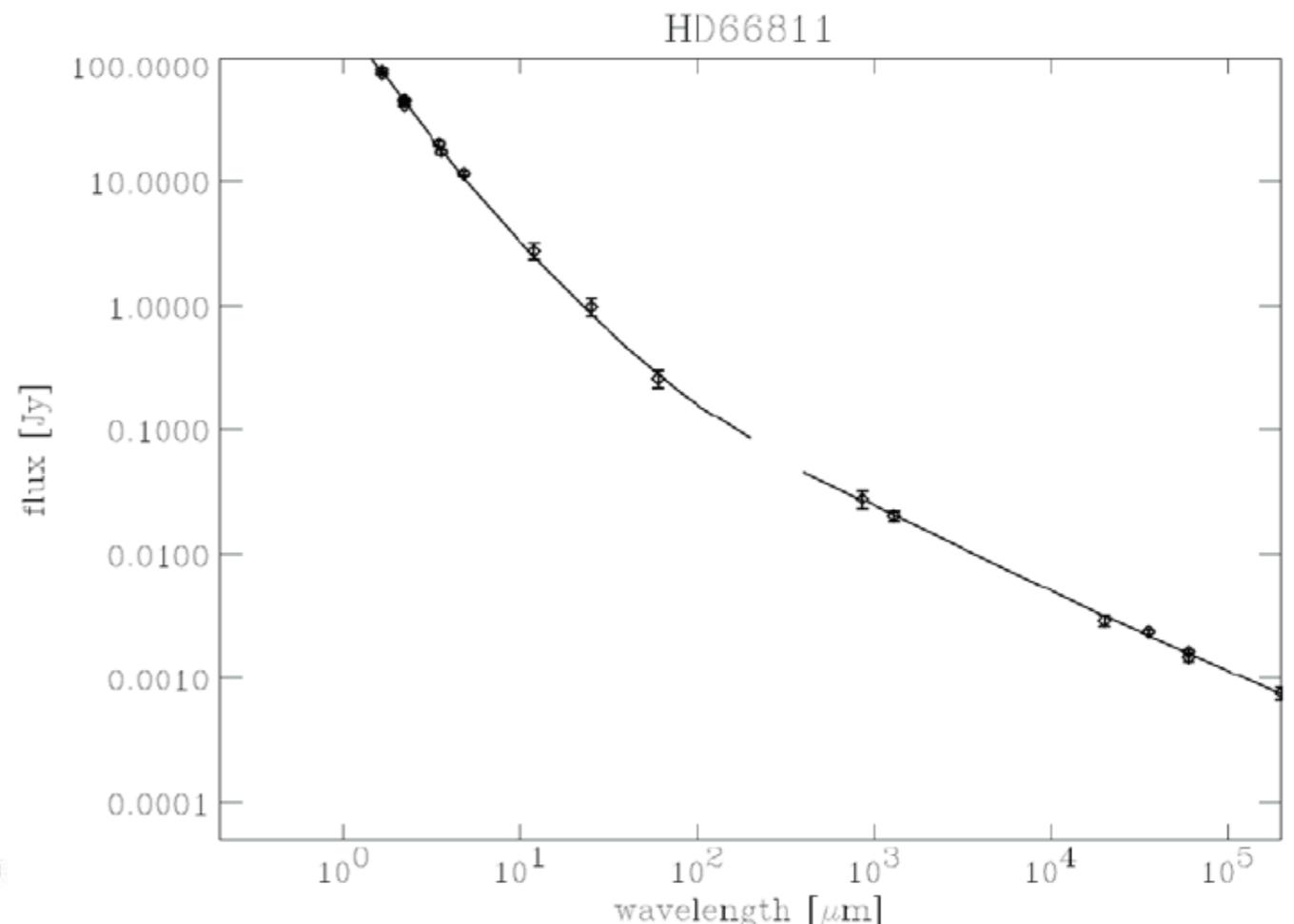
$$\dot{M}_{\text{cl}} \equiv \dot{M}_{\text{smooth}} / f_{\text{cl}}^{0.5}$$

$$3.5 \times 10^{-6} M_{\text{sun}}/\text{yr} = \\ (8.3 \times 10^{-6} M_{\text{sun}}/\text{yr})/6^{0.5}$$

H $\alpha$



IR



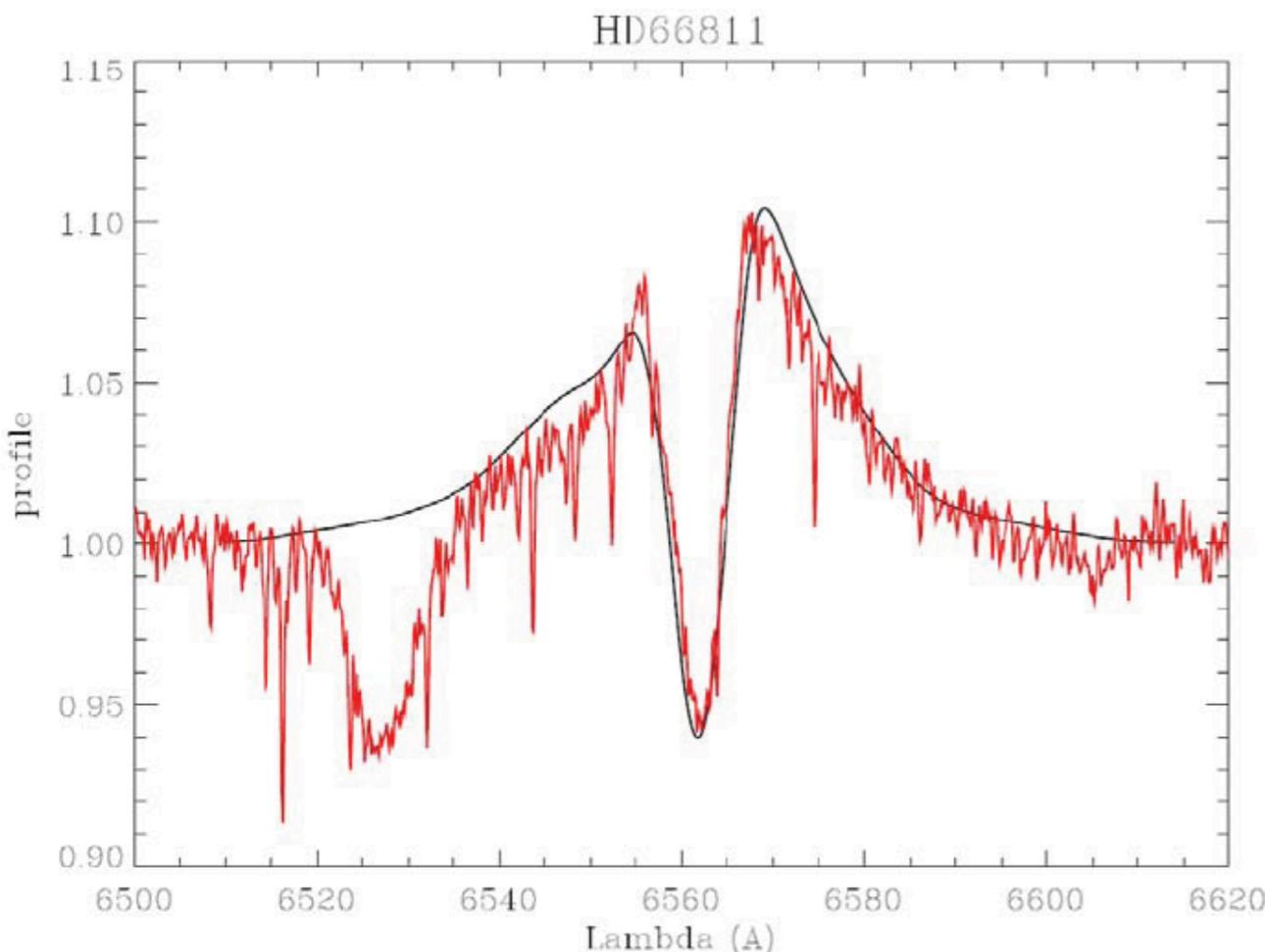
radio

# $\zeta$ Pup: radially varying clumping

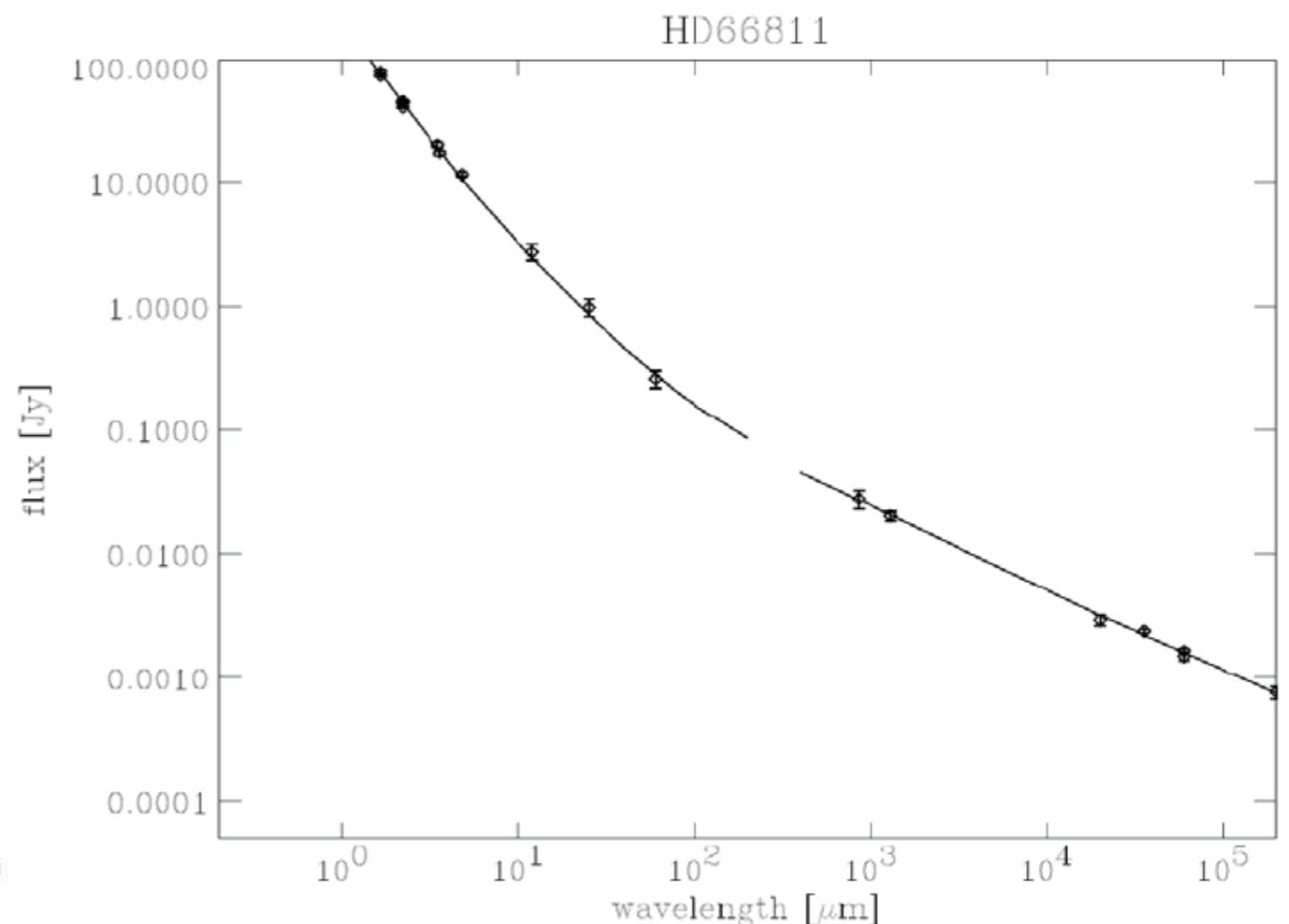
for  $\dot{M} = 3.5 \times 10^{-6} M_{\text{sun}}/\text{yr}$

- $f_{\text{cl}} = 1.3 @ r < 1.12 R_*$
- $f_{\text{cl}} = 6.0 @ 1.12 < r < 1.5 R_*$
- $f_{\text{cl}} = 3.7 @ 1.5 < r < 2 R_*$
- $f_{\text{cl}} = 2.6 @ 2 < r < 15 R_*$
- $f_{\text{cl}} = 1.3 @ r > 15 R_*$

H $\alpha$



IR



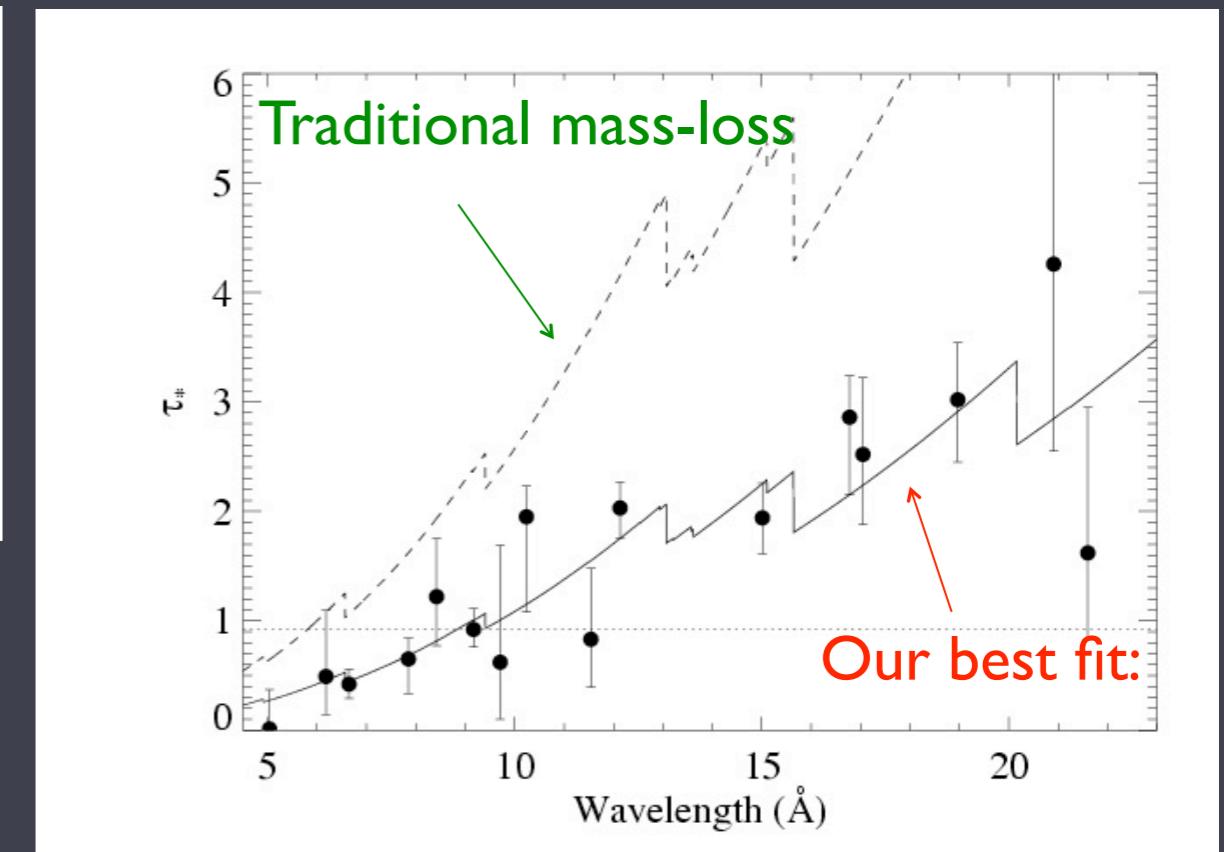
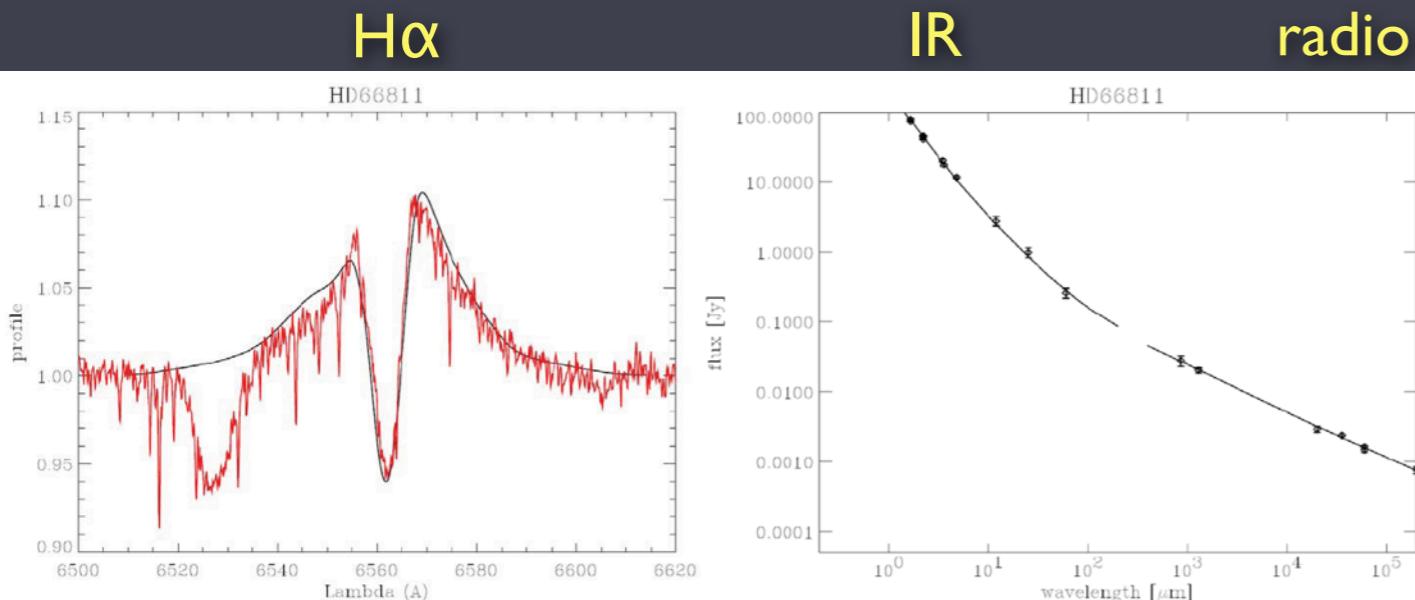
radio

# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 3.5 \times 10^{-6} M_{\text{sun}}/\text{yr}$

consistent multi-wavelength fit with a single mass-loss rate

- $f_{\text{cl}} = 1.3 @ r < 1.12 R_*$
- $f_{\text{cl}} = 6.0 @ 1.12 < r < 1.5 R_*$
- $f_{\text{cl}} = 3.7 @ 1.5 < r < 2 R_*$
- $f_{\text{cl}} = 2.6 @ 2 < r < 15 R_*$
- $f_{\text{cl}} = 1.3 @ r > 15 R_*$



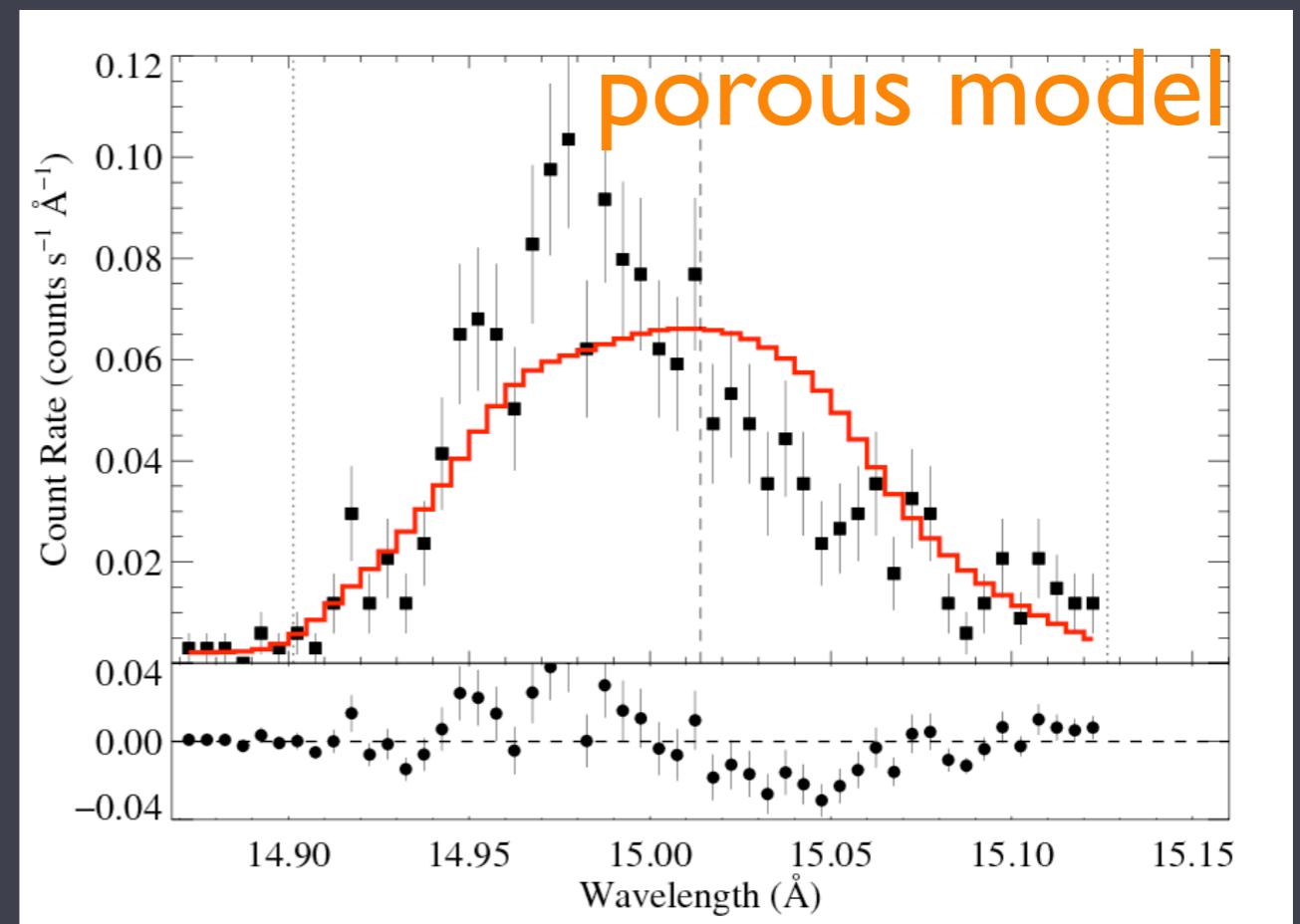
# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 3.5 \times 10^{-6} M_{\text{sun}}/\text{yr}$

consistent multi-wavelength fit with a single mass-loss rate

$h \sim 0$ ; no significant porosity

- $f_{\text{cl}} = 1.3 @ r < 1.12 R_*$
- $f_{\text{cl}} = 6.0 @ 1.12 < r < 1.5 R_*$
- $f_{\text{cl}} = 3.7 @ 1.5 < r < 2 R_*$
- $f_{\text{cl}} = 2.6 @ 2 < r < 15 R_*$
- $f_{\text{cl}} = 1.3 @ r > 15 R_*$



# Conclusions

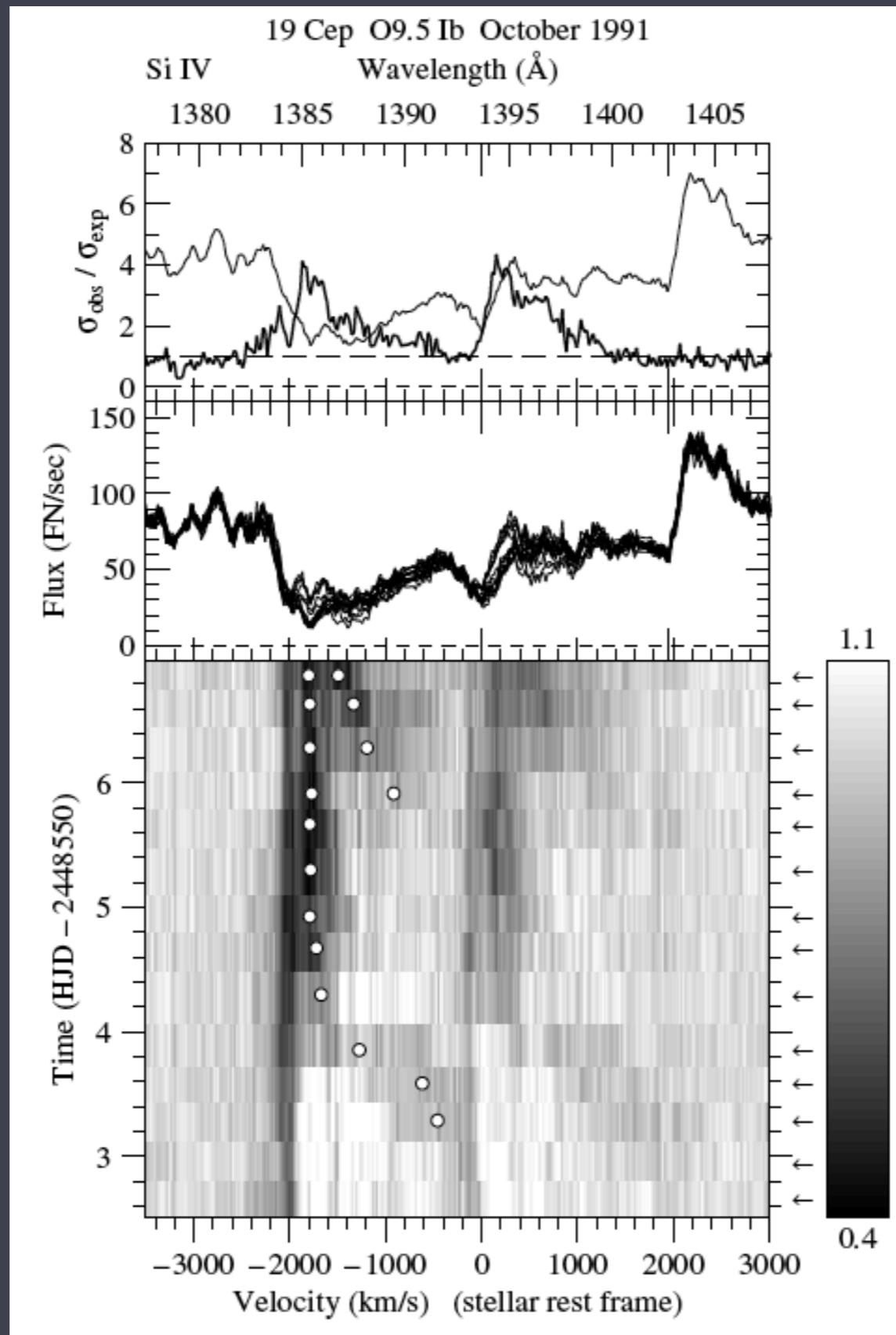
1. Clumped? Yes! Porous? No!
2. X-ray attenuation (from line profile shapes), is a good clumping-insensitive mass-loss rate diagnostic
3. For  $\zeta$  Pup,  $\dot{M} = 3.5 \times 10^{-6} M_{\text{sun}}/\text{yr}$ ;  $f_{\text{cl}} \sim 6$  (at  $r < 1.5 R_{\star}$ ); and  $h \sim 0$
4. Anisotropic porosity is ruled out by the non-detection of the Venetian blind effect
5. Isotropic porosity? Only at a level where the effect on the mass-loss rate is negligible



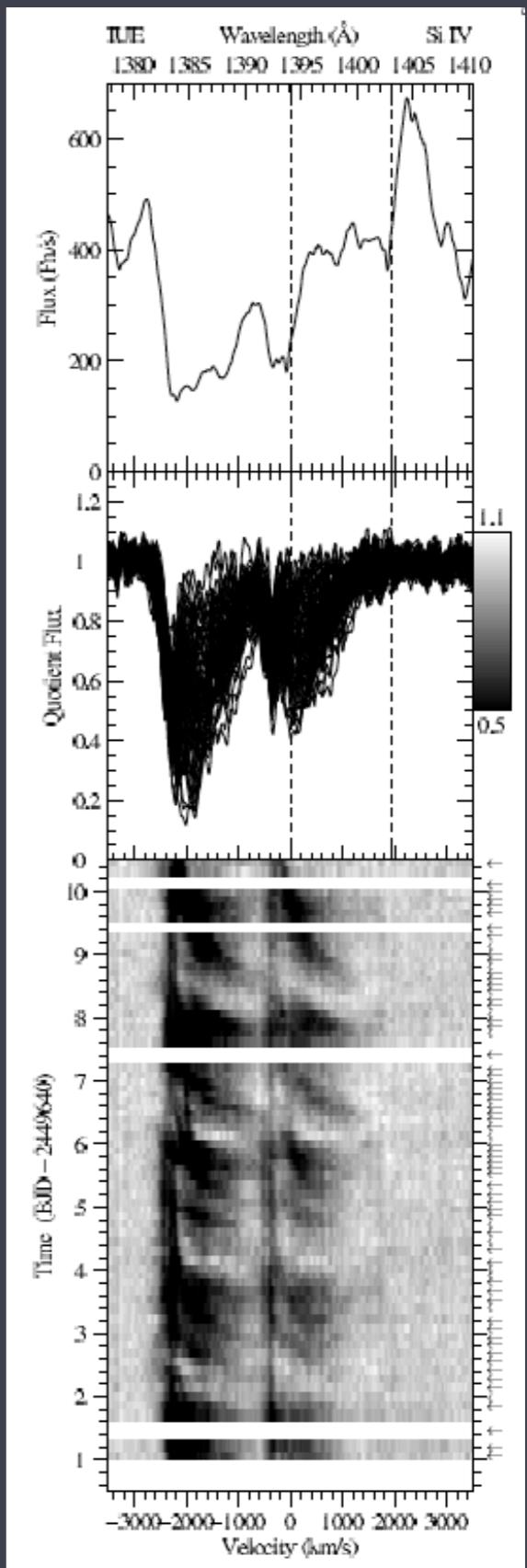
# Extra Slides

# UV variability

19 Cep (O9.5 Ib) : Si IV



$\xi$  Per (O7.5 III) : Si IV



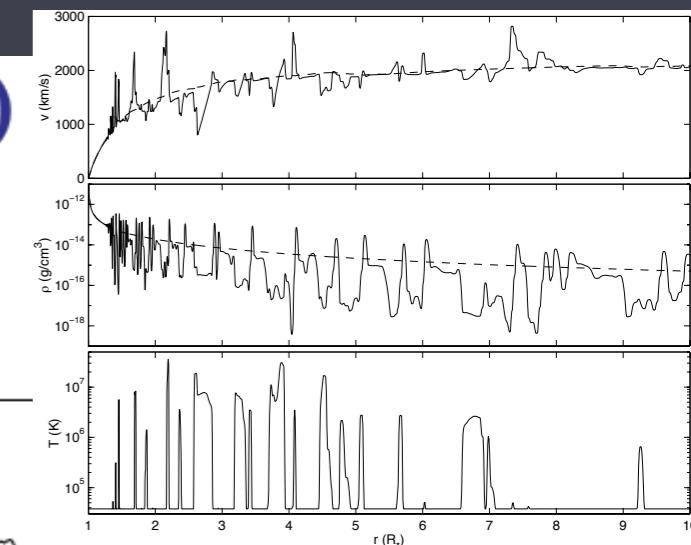
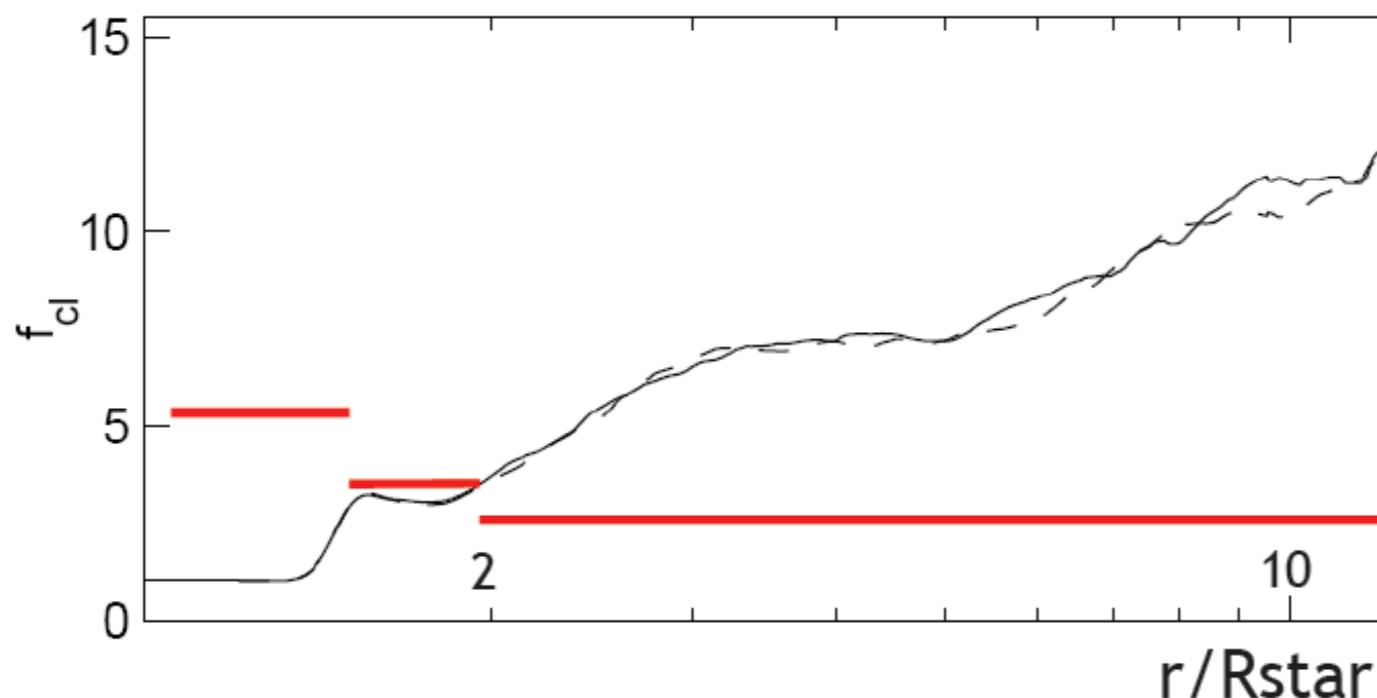
# $\zeta$ Pup: radially varying clumping

for  $\dot{M} = 4.2 \times 10^{-6} M_{\text{sun}}/\text{yr}$

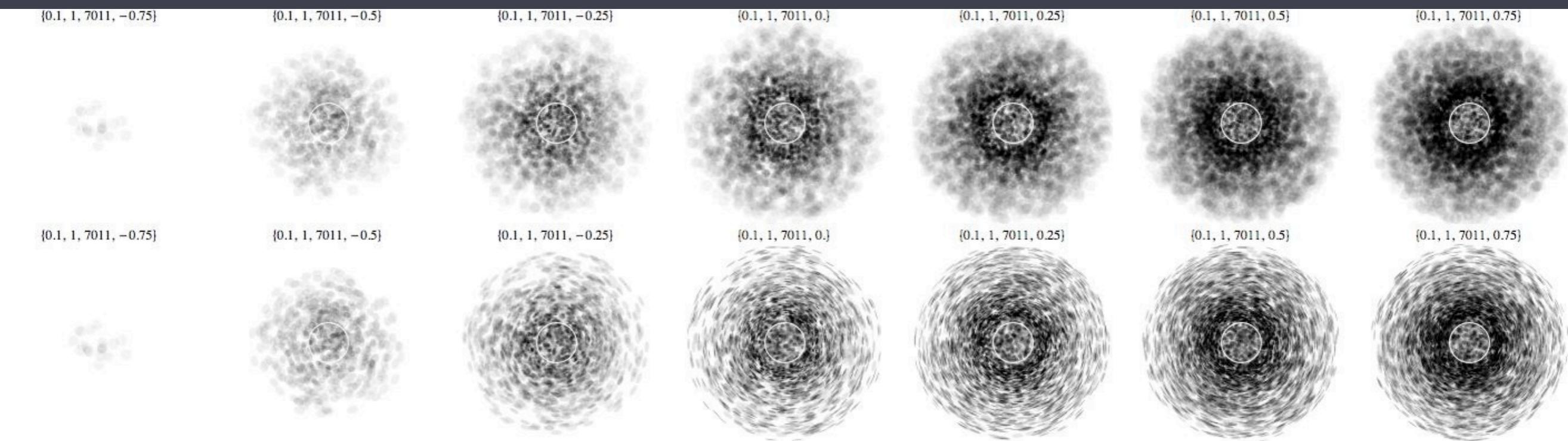
1-D hydro simulations do  
not reproduce the  
observed trend

$f_{\text{cl}} = 1 @ r < 1.12 R_*$   
 $f_{\text{cl}} = 5.5 @ 1.12 < r < 1.5 R_*$   
 $f_{\text{cl}} = 3.1 @ 1.5 < r < 2 R_*$   
 $f_{\text{cl}} = 2 @ 2 < r < 15 R_*$   
 $f_{\text{cl}} = 1 @ r > 15 R_*$

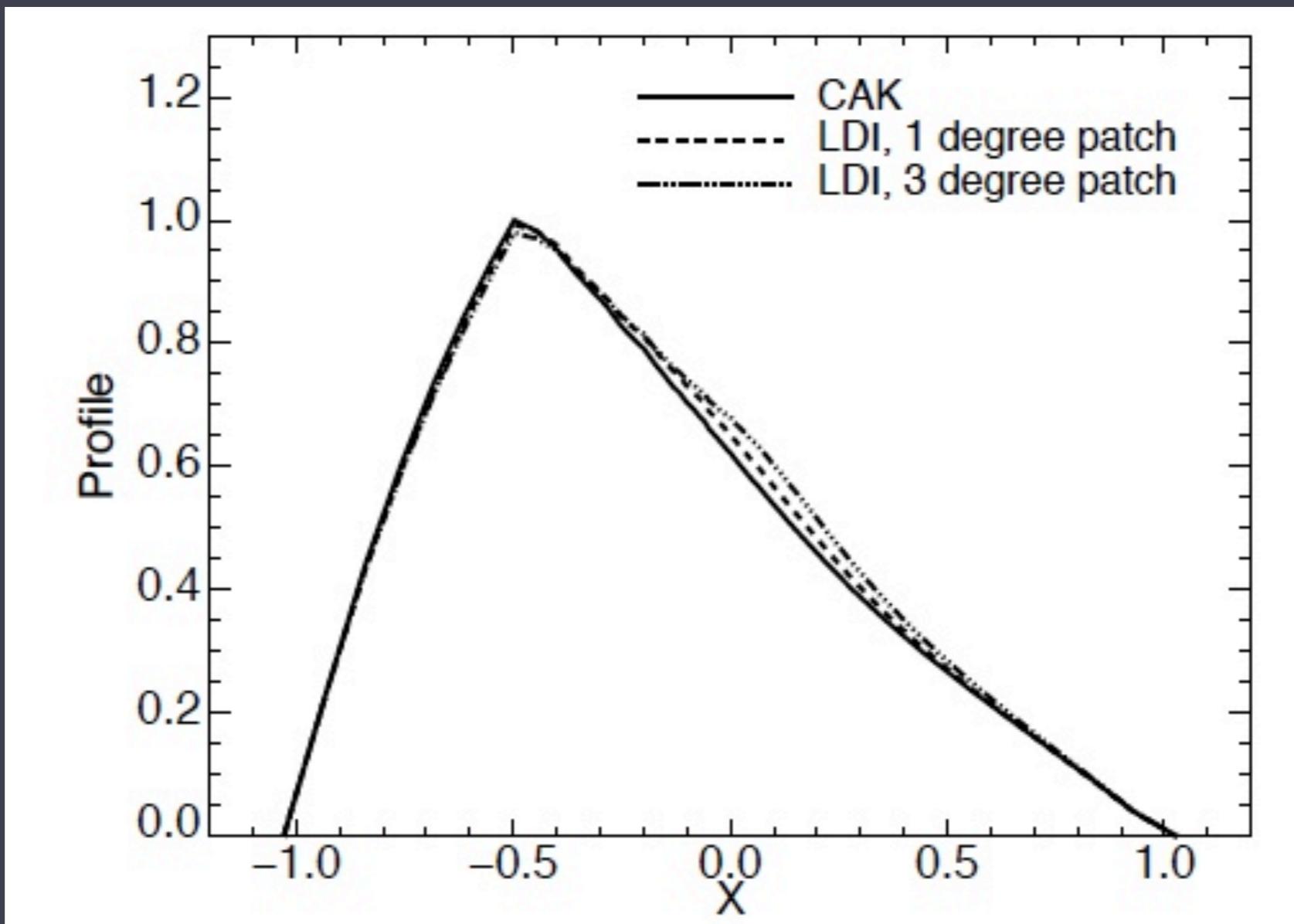
theoretical predictions from Runacres & Owocki (2003)



# Illumination from isovelocity surfaces



# X-ray line profiles can be synthesized directly from hydro simulations



**Figure 6.** Line profiles for  $\tau_{\star} = 2.5$ , calculated from a smooth CAK model and structured LDI models with patch sizes 1 and 3 degrees (see text), as labelled.